



# Reference material:

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- Tutorial material from the nuSMV web site  
<http://nusmv.fbk.eu/NuSMV/tutorial/index.html>
- Notes of prof. Alessandro Artale in Bozen:  
<http://www.inf.unibz.it/~artale/FM/fm.htm>



# Verifica dei Programmi Concorrenti 17-18

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## NuSMV

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NUSMV is a symbolic model checker developed as a joint project between the Formal Methods group at ITC-IRST, the Model Checking group at Carnegie Mellon University, the Mechanized Reasoning Group at University of Geneva and the Mechanized Reasoning Group at University of Trento.

Current version: 2.6.0

Tutorial 2.6

The input language are state machines



# nuSMV – input language

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NUSMV consists of one or more modules and one must be called **main**.

An SMV program consists of:

- Type declarations of the system variables;
- Assignments that define the valid initial states  
(e.g., `init(b0) := 0`).
- Assignments that define the transition relation  
(e.g., `next(b0) := !b0`).
- They can be **Non-Deterministic**: Several values in braces.
- CTL or LTL specifications introduced by the keywords `SPEC`, `LTLSPEC`, respectively.



# nuSMV

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- NUSMV takes the specification of a model and a set of properties (either in CTL or LTL) as input.
- NUSMV output either *True* if the properties hold or *False* with a trace showing the failure.
- The set of states correspond to the set of all possible values for the variables.
- NUSMV uses `!,&,|,->` for the boolean not, and, or, implies.
- NUSMV uses **G,F,X,U,A,E** as defined before

- NUSMV breaks a system description into *modules*.
- A module is instantiated when a variable having the module as its type is declared.
- Modules can have parameters.
- The notation `module-name.x` is used to access the variable `x` of the `module-name`.
- The keyword `DEFINE` is used to assign (the current value of) an expression to a symbol without the need to introduce a variable.
- Defined symbols refer just to an expression then they cannot be assigned non-deterministically.



# nuSMV

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- Modules, by default, are composed *synchronously*
- Each of the modules execute in parallel (e.g., the counter example).
- Using the keyword *process* modules are composed asynchronously (interleaving semantics): at each tick one of them is non-deterministically chosen and executed.
  
- The main use of NUSMV is through an *interactive* shell.
- The user has the possibility to:
  - Explore the possible executions called *Traces*;
  - Construct the Model;
  - Check specification and/or build counterexamples;



# nuSMV: first example

---

```
MODULE main
```

```
VAR
```

```
    request : boolean;
```

```
    state : {ready,busy};
```

```
ASSIGN
```

```
    init(state) := ready;
```

```
    next(state):= case
```

```
        state=ready & request=1: busy;
```

```
        TRUE                      : {ready, busy}
```

```
    esac;
```

The variable `request` is not assigned. This means that there are no constraints on its values, and thus it can assume any value. `request` is thus an unconstrained input to the system.





# nuSMV: first example

---

```
MODULE main
```

```
VAR
```

```
    request : boolean;
```

```
    state : {ready,busy};
```

```
ASSIGN
```

```
    init(state) := ready;
```

```
    next(state):= case
```

```
        state=ready & request=1: busy;
```

```
        TRUE          : {ready, busy}
```

```
    esac;
```



# nuSMV: second example

---

```
MODULE counter_cell (carry_in)
  VAR
    value : boolean;
  ASSIGN
    init(value) := 0;
    next(value) := (value + carry_in) mod 2;
  DEFINE
    carry_out := value & carry_in;
MODULE main
  VAR
    bit0 : counter_cell(1);
    bit1 : counter_cell(bit0.carry_out);
    bit2 : counter_cell(bit1.carry_out);
```

```

MODULE counter_cell (carry_in)
  VAR
    value : boolean;
  ASSIGN
    init(value) := 0;
    next(value) := (value + carry_in) mod 2;
  DEFINE
    carry_out := value & carry_in;
MODULE main
  VAR bit0 : counter_cell(1);
    bit1 : counter_cell(bit0.carry_out);
    bit2 : counter_cell(bit1.carry_out);

```

```

bit0.carry_in = 1
bit1.carry_in = bit0.value
bit2.carry_in = bit1.value & bit1.carry_in

```

```

bit0.carry_out = bit0.value
bit1.carry_out = bit1.value & bit1.carry_in
bit2.carry_out = bit2.value & bit2.carry_in

```

	value	Carry_in	Carry_out
bit0	0	1	0
bit1	0	0	0
bit2	0	0	0
bit0	1	1	0
bit1			
bit2			
bit0			
bit1			
bit2			
bit0			
bit1			
bit2			
bit0			
bit1			
bit2			



# nuSMV: asynchronous example

---

nuSMV allows for synchronous behaviour (as in previous example) as well as asynchronous, through the keyword "process"

It is implicit that if a given variable is not assigned by the process, then its value remains unchanged.



# nuSMV: asynchronous example

---

```
MODULE inverter(input)
  VAR
    output : boolean;
  ASSIGN
    init(output) := 0;
    next(output) := !input;
MODULE main
  VAR
    gate1 : process inverter(gate3.output);
    gate2 : process inverter(gate1.output);
    gate3 : process inverter(gate2.output);
```

```

MODULE inverter(input)
  VAR
    output : boolean;
  ASSIGN
    init(output) := 0;
    next(output) := !input;
MODULE main
  VAR
    gate1 : process inverter(gate3.output);
    gate2 : process inverter(gate1.output);
    gate3 : process inverter(gate2.output);

```

$gate1.output = !gate1.input = !gate3.output$   
 $gate2.output = !gate2.input = !gate1.output$   
 $gate3.output = !gate3.input = !gate2.output$

	output	input	
gate1	0	0	
gate2	0	0	
gate3	0	0	
gate1	0	0	
gate2	0	0	
gate3	1	0	
gate1	0	1	
gate2	1	0	
gate3	1	0	
gate1		1	
gate2		0	
gate3		1	
gate1			
gate2			
gate3			



# nuSMV: fairness - justice

---

In asynchronous nuSMV a process is not "forced" to move  
(and therefore also unrealistic sequences are considered)

A fairness constraints can be specified:

FAIRNESS f uguale a justice f

Implies that only paths in which formula f is infinitely often true are considered by the model-checker

Example: FAIRNESS running

Where "running" is a predefined variable associated to each process, with the obvious meaning



# Synchronous inverter and fairness

---

```
MODULE inverter(input)
  VAR
    output : boolean;
  ASSIGN
    init(output) := FALSE;
    next(output) := (!input) union output;
MODULE main
  VAR
    gate1 : inverter(gate3.output);
    gate2 : inverter(gate1.output);
    gate3 : inverter(gate2.output);
```

In this case we cannot force the inverters to be effectively active infinitely often using a fairness declaration. In fact, a valid scenario for the synchronous model is the one where all the inverters are idle and assign to the next output the current value of output.





# nuSMV: fairness - compassion

---

In NUSMV we can also specify compassion

COMPASSION p q

Implies that only paths in which GF p  $\rightarrow$  GF q is satisfied are considered by the model-checker

Example: COMPASSION ask receive  
and only paths that satisfy GF ask  $\rightarrow$  GF receive are considered for model checking



# nuSMV: semaphore

```
MODULE main
  VAR
    semaphore : boolean;
    proc1      : process user(semaphore);
    proc2      : process user(semaphore);
  ASSIGN
    init(semaphore) := 0;
MODULE user(semaphore)
  VAR
    state : {idle, entering, critical, exiting};
  ASSIGN
    init(state) := idle;
    next(state) :=
      case
        state = idle           : {idle, entering};
        state = entering & !semaphore : critical;
        state = critical       : {critical, exiting};
        state = exiting        : idle;
      1                          : state;
    esac;
    next(semaphore) :=
      case
        state = entering : 1;
        state = exiting  : 0;
      1                    : semaphore;
    esac;
  FAIRNESS
    running
```



# nuSMV: traces

---

Three simulation modes (how to select a state):

- random
- deterministic,
- interactive

In deterministic simulation mode the first state of a set (whatever it is) is chosen, while in the random one the choice is performed nondeterministically. Traces are automatically generated by NUSMV: the user obtains the whole of the trace in a time without control over the generation itself (except for the simulation mode and the number of states entered via command line).

In the third simulation mode, the user has a complete control over the trace, as it can choose the next step of the execution



# nuSMV: traces

---

For the very first example (called short.smv)

```
system_prompt> NuSMV -int short.smv
NuSMV> go
NuSMV> pick_state -r
NuSMV> print_current_state -v
Current state is 1.1
request = 0
state = ready
NuSMV> simulate -r 3
***** Starting Simulation From State 1.1 *****
NuSMV> show_traces -t
There is 1 trace currently available.
NuSMV> show_traces -v
##### Trace number: 1 #####
Trace Description: Simulation Trace
Trace Type: Simulation
-> State: 1.1 <-
    request = 0
    state = ready
-> State: 1.2 <-
    request = 1
    state = busy
```

# nuSMV: traces

```
-> State: 1.3 <-  
    request = 1  
    state = ready  
-> State: 1.4 <-  
    request = 1  
    state = busy
```

```
NuSMV> goto_state 1.4
```

The starting state for new trace is:

```
-> State 2.4 <-  
    request = 1  
    state = busy
```

```
NuSMV> simulate -r 3
```

```
***** Simulation Starting From State 2.4 *****
```

```
NuSMV> show_traces 2
```

```
##### Trace number: 2 #####
```

```
Trace Description: Simulation Trace
```

```
Trace Type: Simulation
```

```
-> State: 2.1 <-  
    request = 1  
    state = ready  
-> State: 2.2 <-  
    state = busy  
-> State: 2.3 <-  
    request = 0  
-> State: 2.4 <-
```

```
    request = 1  
-> State: 2.5 <-  
    request = 0  
-> State: 2.6 <-  
    state = ready  
-> State: 2.7 <-  
NuSMV>
```



# nuSMV: traces – choose a state

---

```
NuSMV> pick_state -i
```

```
***** AVAILABLE STATES *****
```

```
===== State =====
```

```
0) -----
```

```
    request = 1  
    state = ready
```

```
===== State =====
```

```
1) -----
```

```
    request = 0  
    state = ready
```

```
Choose a state from the above (0-1): 1 <RET>
```

```
Chosen state is: 1
```

```
NuSMV> simulate -i 1
```

```
***** Simulation Starting From State 3.1 *****
```

```
***** AVAILABLE FUTURE STATES *****
```

```
===== State =====
```

```
0) -----
```

```
    request = 1  
    state = ready
```

```
===== State =====
```

```
1) -----
```

```
    request = 1  
    state = busy
```

```
===== State =====
```

```
2) -----
```

```
    request = 0  
    state = ready
```

```
===== State =====
```

```
3) -----
```

```
    request = 0  
    state = busy
```

```
Choose a state from the above (0-3): 0 <RET>
```

```
Chosen state is: 0
```

```
NuSMV> show_traces 3
```

```
##### Trace number: 3 #####
```

```
Trace Description: Simulation Trace
```

```
Trace Type: Simulation
```

```
-> State: 3.1 <-
```

```
    request = 0  
    state = ready
```

```
-> State: 3.2 <-
```

```
    request = 1
```



# nuSMV: CTL/LTL model checking

---

A CTL specification is a CTL formula preceeded by the keyword SPEC

A LTL specification is a LTL formula preceeded by the keyword LTLSPEC

If the formula is not true a trace that provides a counter example is shown (for A quantifiers, since for existential does not make sense)



# nuSMV: CTL model checking of semaphore

```
MODULE main
  VAR
    semaphore : boolean;
    proc1      : process user(semaphore);
    proc2      : process user(semaphore);
  ASSIGN
    init(semaphore) := 0;
  SPEC AG ! (proc1.state = critical & proc2.state = critical)
  SPEC AG (proc1.state = entering -> AF proc1.state = critical)
MODULE user(semaphore)
  VAR
    state : {idle, entering, critical, exiting};
  ASSIGN
    init(state) := idle;
    next(state) :=
      case
        state = idle           : {idle, entering};
        state = entering & !semaphore : critical;
        state = critical       : {critical, exiting};
        state = exiting        : idle;
        1                       : state;
      esac;
    next(semaphore) :=
      case
        state = entering : 1;
        state = exiting  : 0;
        1                 : semaphore;
      esac;
  FAIRNESS
    running
```

# nuSMV: CTL model checking

```
system_prompt> NuSMV semaphore.smv
```

we obtain the following output:

```
-- specification AG (!(proc1.state = critical & proc2.state = critical))
-- is true
-- specification AG (proc1.state = entering -> AF proc1.state = critical)
-- is false
-- as demonstrated by the following execution sequence
-> State: 1.1 <-
    semaphore = 0
    proc1.state = idle
    proc2.state = idle
-> Input: 1.2 <-
    _process_selector_ = proc1
-- Loop starts here
-> State: 1.2 <-
    proc1.state = entering
-> Input: 1.3 <-
    _process_selector_ = proc2
-> State: 1.3 <-
    proc2.state = entering
-> Input: 1.4 <-
    _process_selector_ = proc2
-> State: 1.4 <-
    semaphore = 1
    proc2.state = critical
```

```
-> Input: 1.5 <-
    _process_selector_ = proc1
-> State: 1.5 <-
-> Input: 1.6 <-
    _process_selector_ = proc2
-> State 1.6 <-
    proc2.state = exiting
-> Input: 1.7 <-
    _process_selector_ = proc2
-> State 1.7 <-
    semaphore = 0
    proc2.state = idle
```



# CTL: Syntax

---

AP, set of atomic proposition.  $p \in AP$ .

CTL formulae:

$$\varphi ::= p \mid \neg\varphi \mid \varphi \vee \varphi \mid EX\varphi \mid E[\varphi U \varphi] \mid A[\varphi U \varphi]$$

**E**: "for some path"

**A**: "for all paths"

**EX**: "for some path next"

**U**: until

Note: syntactically correct formulas quantifiers and temporal operators are in strict alternation



# Derived operators

---

- $EF\varphi \equiv E[\text{true} \cup \varphi]$  “ $\varphi$  holds potentially” - “ $\varphi$  is possible”
- $AF\varphi \equiv A[\text{true} \cup \varphi]$  “ $\varphi$  is inevitable (unavoidable)”
- $EG\varphi \equiv \neg AF\neg\varphi$  “potentially always  $\varphi$ ” – “globally along some path”
- $AG\varphi \equiv \neg EF\neg\varphi$  “invariantly  $\varphi$ ”
- $AX\varphi \equiv \neg EX\neg\varphi$  “for all paths next”



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End of nuSMV