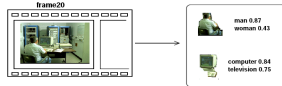


## Shape

- Segmentation/tiling (based on color or illumination)



- A *segmentation* of image  $I$  is a set  $\{R_1, \dots, R_n\}$  of regions such that:
  - $R_1 \cup \dots \cup R_n = I$
  - $R_i \cap R_j = \emptyset$  for all  $1 \leq i, j \leq n$
  - $H(R_i) = \text{true}$  for all  $1 \leq i \leq n$
  - If  $R_i, R_j$  are adjacent, then  $H(R_i \cup R_j) = \text{false}$ . $H$  is an homogeneity predicate

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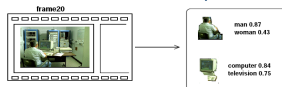
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## Shape

- Segmentation/tiling (based on color or illumination)



- Hough transform of edges
  - **Global features**
    - Roundness
    - Aspect ratio (ratio between the width of the image and the height of the image)
    - Major axis orientation
  - **Local features**
    - Size and orientation of consecutive boundary segments



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## Spatial queries

- ...fingerprint detection
  - spatial distribution
    - positions of features relative to each other
      - ..their angles
      - ..their distances from each other



<http://www.sphinxtech.com.sg/fingerfeatures.jpg>



<http://www.informatik.htw-dresden.de/~iwi/Belege/Poetzsch/>

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## Spatial relationships

- How do we represent the spatial relationships among these objects?

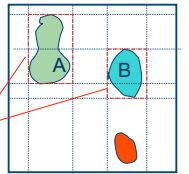
- to the left, to the right

A is to the left of B

- above of, below of

A is above/below B?

Minimum Bounding Rectangles (MBR)



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## Nine-directional Lower Triangular Matrix (9DLT)

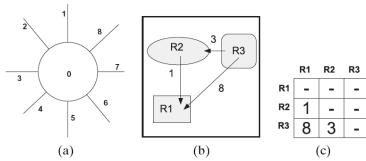


Figure 2.35. (a) The nine directions between two regions (0 means "at the same place") [Chang, 1991]. (b) An image with three regions and their relationships (for convenience, the relationships are shown only in one direction). (c) The corresponding 9DLT matrix.

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## Nine-intersection Matrix

$$\begin{pmatrix} o_1^o \cap o_2^o & o_1^o \cap \delta o_2 & o_1^o \cap o_2^- \\ \delta o_1 \cap o_2^o & \delta o_1 \cap \delta o_2 & \delta o_1 \cap o_2^- \\ o_1^- \cap o_2^o & o_1^- \cap \delta o_2 & o_1^- \cap o_2^- \end{pmatrix}$$

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## Nine-intersection Matrix

$$\begin{pmatrix} o_1^o \cap o_2^o & o_1^o \cap \delta o_2 & o_1^o \cap o_2^- \\ \delta o_1 \cap o_2^o & \delta o_1 \cap \delta o_2 & \delta o_1 \cap o_2^- \\ o_1^- \cap o_2^o & o_1^- \cap \delta o_2 & o_1^- \cap o_2^- \end{pmatrix}$$

$$\begin{pmatrix} \geq 1 & \geq 1 & \geq 1 \\ 0 & \geq 1 & \geq 1 \\ 0 & 0 & \geq 1 \end{pmatrix}, \quad \begin{pmatrix} \geq 1 & \geq 1 & \geq 1 \\ \geq 1 & \geq 1 & \geq 1 \\ \geq 1 & \geq 1 & \geq 1 \end{pmatrix}$$

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## Spatial orientation graph

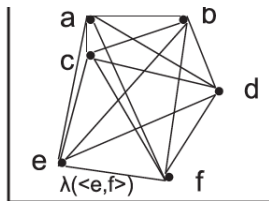


Figure 2.36. A sample spatial orientation graph.

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## Converting a region into a set of points

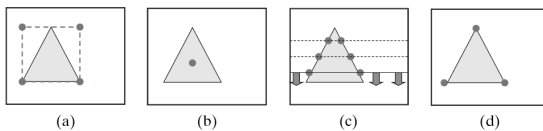


Figure 2.37. Converting a region into a set of points: (a) minimum bounding rectangle, (b) centroid, (c) line sweep, and (d) corners.

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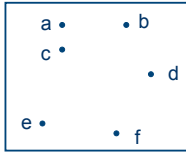
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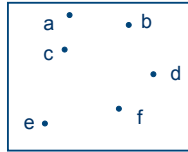
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## Compare space = compare string



(e<a=c<f=b<d; a=b<c<d<e<f)



(e<c<a<f=b<d; a<b<c<d<f<e)

- Instead of comparing spatial composition directly, we can compare the corresponding 2Dstrings

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## How do we compare strings??

(e<a=c<f=b<d; a=b<c<d<e<f) vs. (e<c<a<f=b<d; a<b<c<d<f<e)

- Edit distance:
  - "table" vs. "cable": 1 (replace "t" with "c")
  - "table" vs. "bale": 2 (delete "t"; swap "a" and "b")

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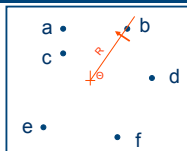
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## OR string



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## String representations of space

- 2D string
  - Use centroids (points)
  - 3 operators
- 2D Estring
  - Use intervals
  - Compare intervals
  - More operators
    - Contain, meet, begin, end, overlap, equal, less than, overlap, inverse

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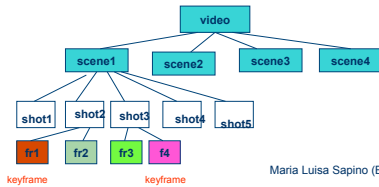
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## Video (temporal structure!!!!)

- Time (as in audio) + objects and motion
- Frame by frame representation is too costly (30f per second)
- Shot detection (video segmentation) gives a set of frames which are atomic



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## Motion

- Camera motion
  - Zooming (varying the focus distance)
  - Tilting (down/up - camera vertical rotation)
  - Panning (right/left - camera horizontal rotation)
  - Tracking (horizontal transverse movement)
  - Booming (vertical transverse movement)
  - Dollying (toward/away - horizontal lateral movement)
- Object motion
- Scene change
- Problem: if you don't know about camera motion ahead in time, then it is harder to distinguish between object motion and camera motion

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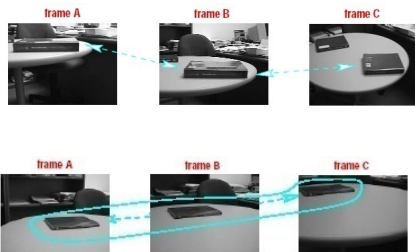
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## Object tracking



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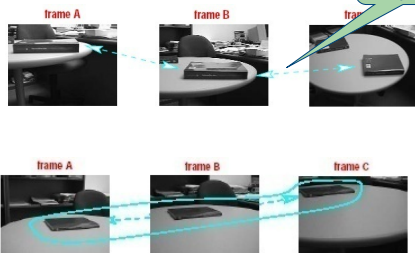
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## Object identity



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## Time

- What is time?
- How do we represent time?
- How do we represent actions and events?
- How do we ask queries about time?

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## Video queries



Object queries

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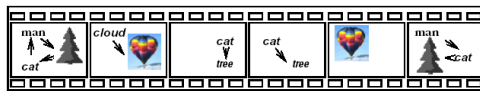
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## Video queries



Frame queries

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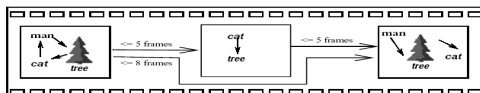
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## Video queries



Simple action queries

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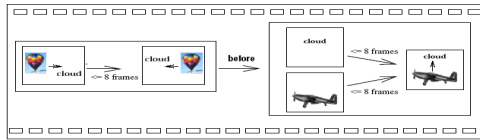
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## Video queries



Composite action queries

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## Time Models

- Instants

- 3 instant based relations:  $<$ ,  $=$ ,  $>$



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## Time Models

- Instants

- 3 instant based relations:  $<$ ,  $=$ ,  $>$



- Intervals

- 13 interval based relations



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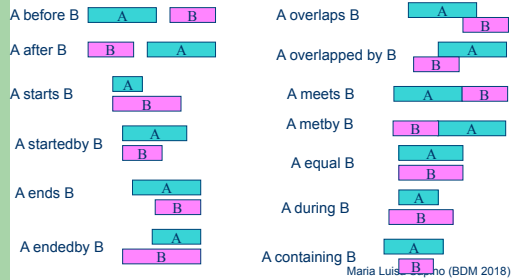
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## Intervals...




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## Temporal Logic; Axioms

- $\text{before}(I_1, I_2) \text{ and } \text{before}(I_2, I_3) \rightarrow \text{before}(I_1, I_3)$
- $\text{meets}(I_1, I_2) \text{ and } \text{during}(I_2, I_3) \rightarrow \text{overlaps}(I_1, I_3) \text{ or } \text{during}(I_1, I_3) \text{ or } \text{meets}(I_1, I_3)$

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## Definitions

- $\text{before}(I_1, I_2) \text{ and } \text{before}(I_2, I_3) \rightarrow \text{before}(I_1, I_3)$
- $\text{meets}(I_1, I_2) \text{ and } \text{during}(I_2, I_3) \rightarrow \text{overlaps}(I_1, I_3) \text{ or } \text{during}(I_1, I_3) \text{ or } \text{starts}(I_1, I_3)$
- $\text{in}(I_1, I_2) \leftrightarrow \text{during}(I_1, I_2) \text{ or } \text{starts}(I_1, I_2) \text{ or } \text{finishes}(I_1, I_2)$

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## Rules

- $\text{before}(I1,I2)$  and  $\text{before}(I2,I3) \rightarrow \text{before}(I1,I3)$
- $\text{meets}(I1,I2)$  and  $\text{during}(I2,I3) \rightarrow \text{overlaps}(I1,I3)$  or  $\text{during}(I1,I3)$  or  $\text{starts}(I1,I3)$
- $\text{in}(I1,I2) \leftrightarrow \text{during}(I1,I2)$  or  $\text{starts}(I1,I2)$  or  $\text{finishes}(I1,I2)$
- $\text{holds}(p,I) \leftrightarrow \text{forall } i (\text{in}(i,I) \rightarrow \text{holds}(p,i))$
- $\text{holds}(\text{and}(p,q),I) \leftrightarrow \text{holds}(p,I)$  and  $\text{holds}(q,I)$
- $\text{holds}(\text{not}(p),I) \leftrightarrow \text{forall } i (\text{in}(i,I) \rightarrow \text{not holds}(p,i))$

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## Interval Algebra

- Predicates: 13 relationships between intervals
- Operators: and, or
- Result: all relationships that hold between every pair of intervals

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## Interval Algebra

- Predicates: 13 relationships between intervals
- Operators: and, or
- Result: all relationships that hold between every pair of intervals
- $\text{overlaps}(a,b)$  and  $\text{starts}(a,b)$  and  $\text{meets}(b,c)$ 
  - what else can you deduce from these facts?????

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## Minimal Labeling Problem

- NP-hard
- Special cases: if there are no “or”s, this can be solved in  $O(n^3)$  time
  - constraint propagation algorithm

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## Point algebra

- Use “instants” instead of “intervals”
- Use “before”, “equal”, and “after” instead of the 13 interval relationships
- (similar to situation calculus)

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## Instants vs intervals

- Each interval can be described by two instants **st** and **et**

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## Instants vs intervals

- Each interval can be described by two instants **st** and **et**
- If there are no disjunctions, interval algebra = instant algebra
- $\text{during}(A,B) =$   
 $\text{st}(A) > \text{st}(B)$  and  $\text{et}(A) < \text{et}(B)$  and  
 $\text{st}(A) < \text{et}(A)$  and  $\text{st}(B) < \text{et}(B)$

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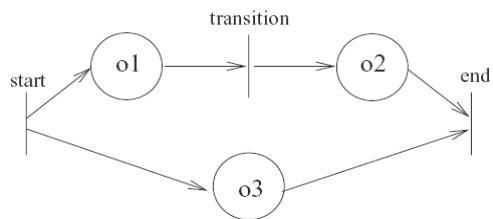
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## Object Composition Petri Nets



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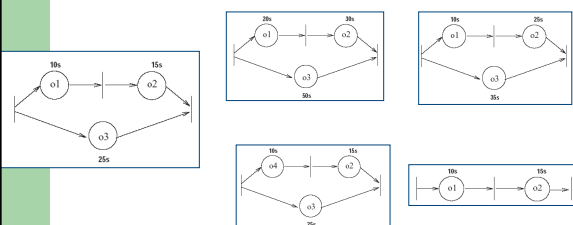
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## How to compare OCPNs



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