

ARC<sup>2</sup>S Group

Applied Research on Computational Complex Systems

# Hierarchical Data and Graph Visualization

Prof. Giancarlo **Ruffo**

“Analisi e Visualizzazione di Reti Complesse” (9 credits)

Laurea Magistrale in **Informatica**

Università degli Studi di Torino

A.A. 2017/18

@giaruffo



# **INTRODUCTION**

## Hierarchical Data Visualization

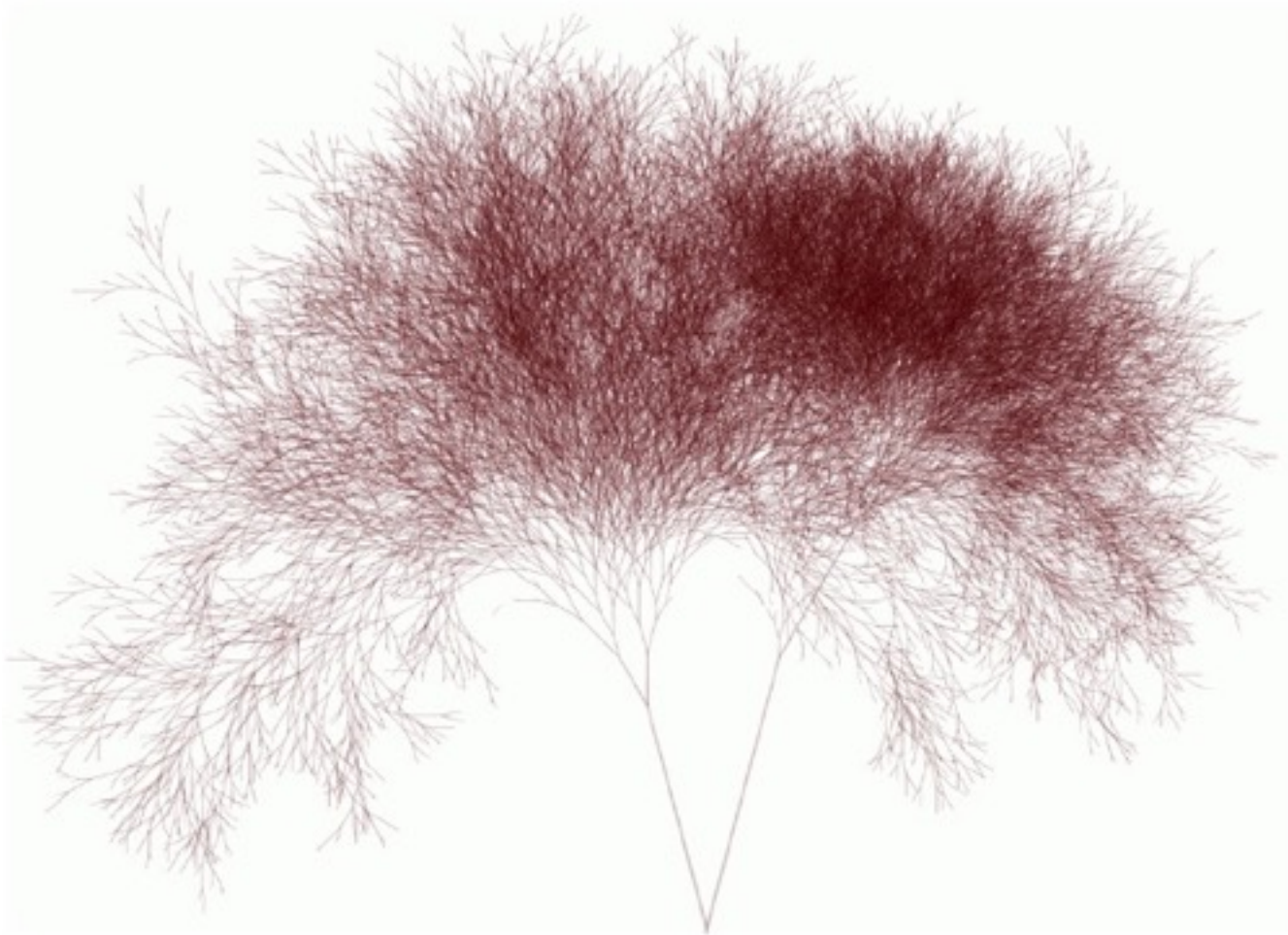
# Hierarchical Data

- Any data with some sort of hierarchy
  - *"Group of objects ranked so that everyone but the top most is subordinate to one above it."*
- Example hierarchy
  - Country: Italy
  - Region: Piedmont
  - Area: Turin
  - City: Turin
  - Municipal District: Madonna di Campagna

# Examples of Hierarchical Data

- Evolutionary Tree
- Dendrograms
- File Directory Structure
- Dewey Decimal System
- Family History
- Organization Charts
- Outlines

# Tree Structures



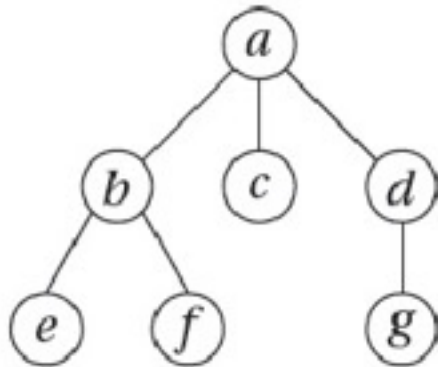
<http://drunkenworkhere.org/219>

# Tree Structures

- Used to model hierarchical data
- Special type of graph
  - Must be **acyclic**, i.e. has no cycles or loops
  - Must be **undirected**, i.e. arrow-less edges
  - Usually **rooted** (a single node at top)
  - Each **subgraph** is also a tree (**subtree**)

# Tree Terminology

FIGURE 2.8: TREE TERMINOLOGY AND NOTATION



$G = (N, E)$  where

$$N = \{ a, b, c, d, e, f, g \}$$

$$E = \{ (a, b), (a, c), (a, d) \\ (b, e), (b, f), (d, g) \}$$

Example tree  $G = (N, E)$ . Some observations: Each node has a unique label. Node  $a$  is the root node. Nodes  $a$ ,  $b$ , and  $d$  are internal nodes. Nodes  $c$ ,  $e$ ,  $f$ , and  $g$  are leaf nodes. Node  $d$  is a parent node to node  $g$ , and node  $g$  is a child node to  $d$ . Nodes  $e$  and  $f$  share the same parent node  $b$  and are considered siblings.

# Tree Visualization

- Node-Link Diagrams
  - Traditional node-link diagram
  - Dendograms
  - Hyperbolic trees
- Space-Filling Diagrams
  - Treemaps
  - Sunbursts



# Considerations

- Is the hierarchical structure visible?
- What is the level of a specific node?
- What is the height of the tree?
- How many nodes on level  $x$ ?
- Are the labels readable? All nodes visible?
- What type of interaction is supported?
  - Focus + Context
  - Overview + Detail
  - Zoom + Filter

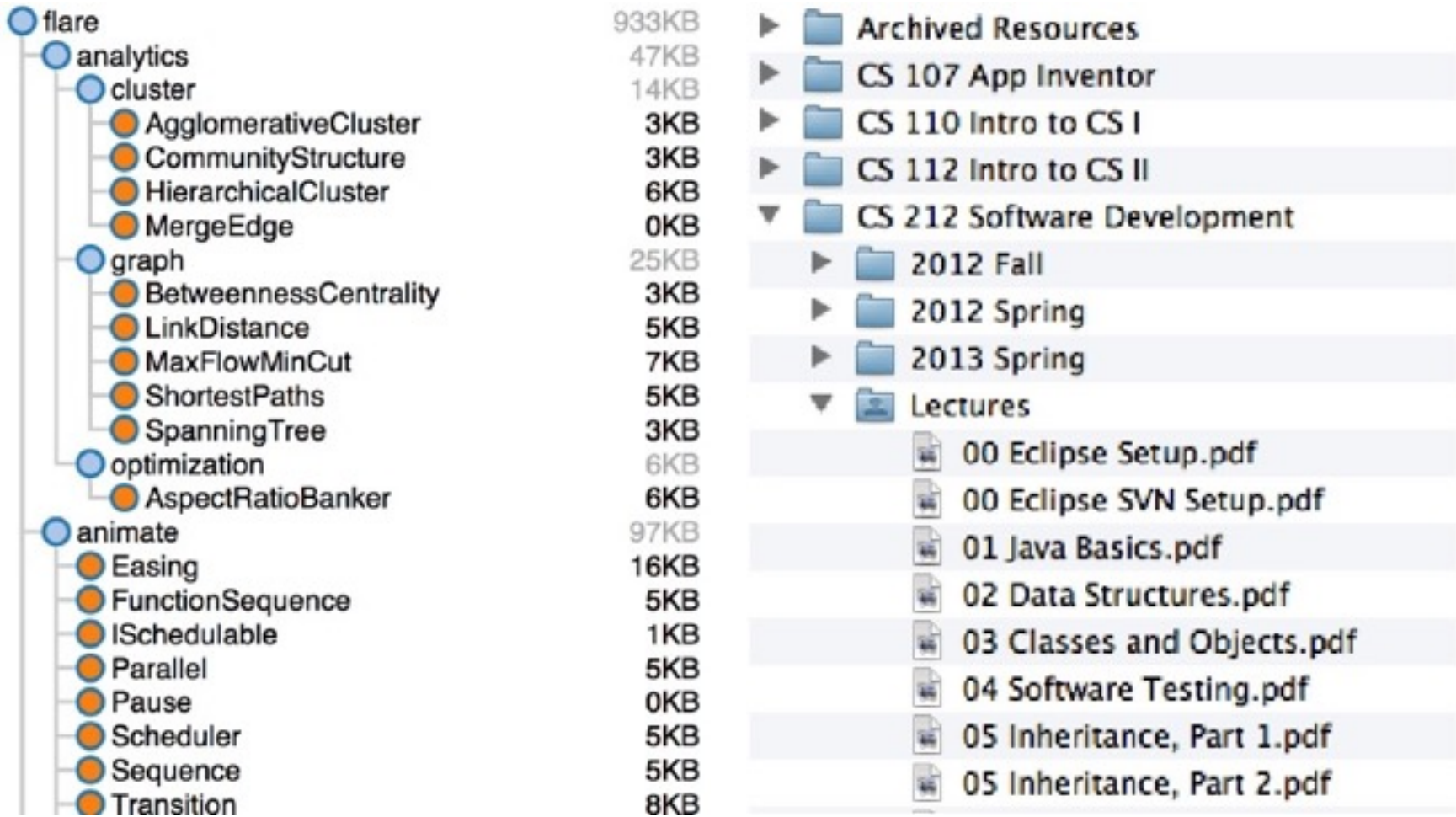
# **NODE-LINK DIAGRAMS**

Tree Visualization

# Node-Link Diagrams

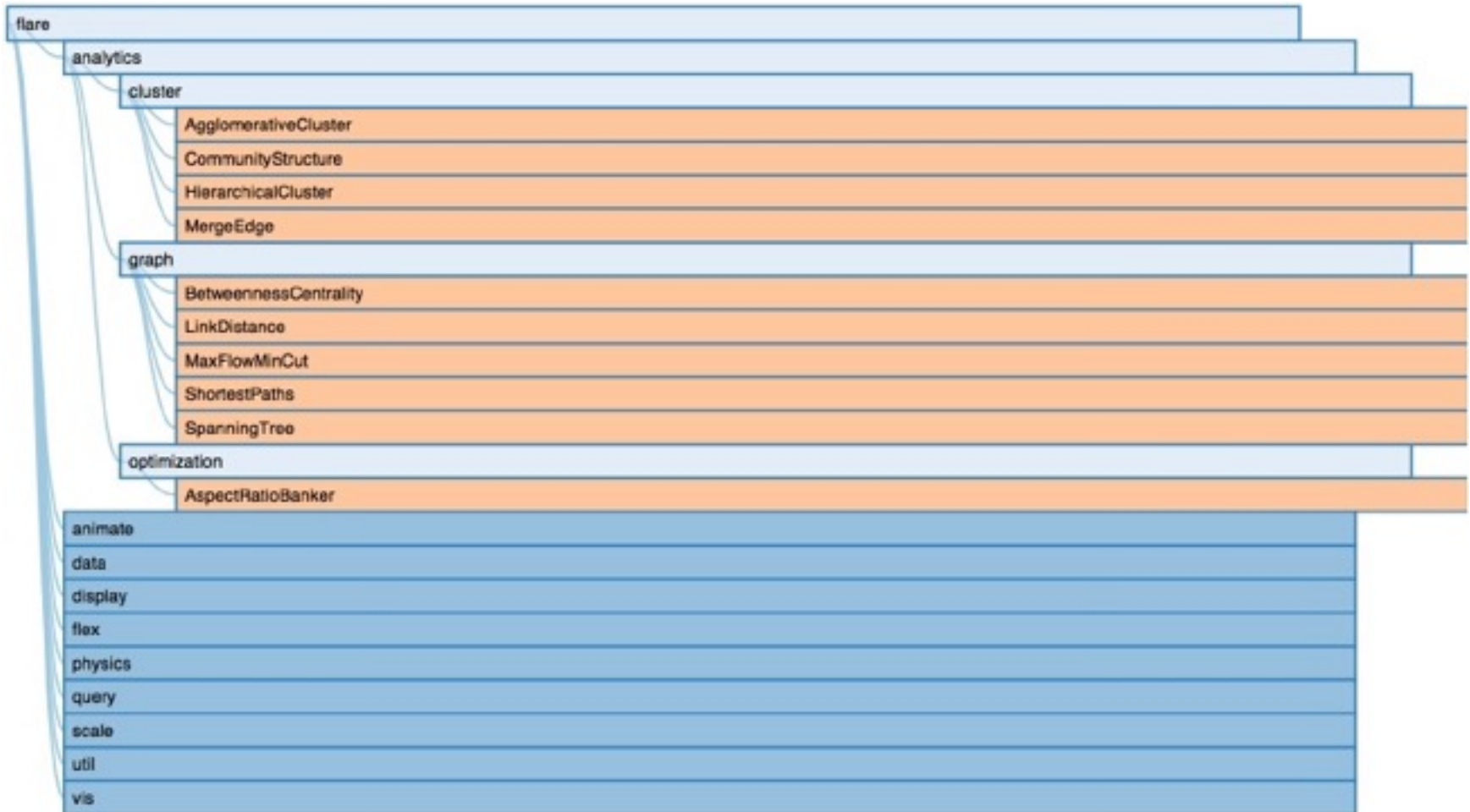
- Indented Layout
  - Child nodes placed below parent and indented
  - Compact width
  - Height expands and shrinks
  - Often used to navigate file systems
  - Difficult to see all nodes of a specific level

# Indented Layout



<http://mbostock.github.io/protovis/ex/indent.html>

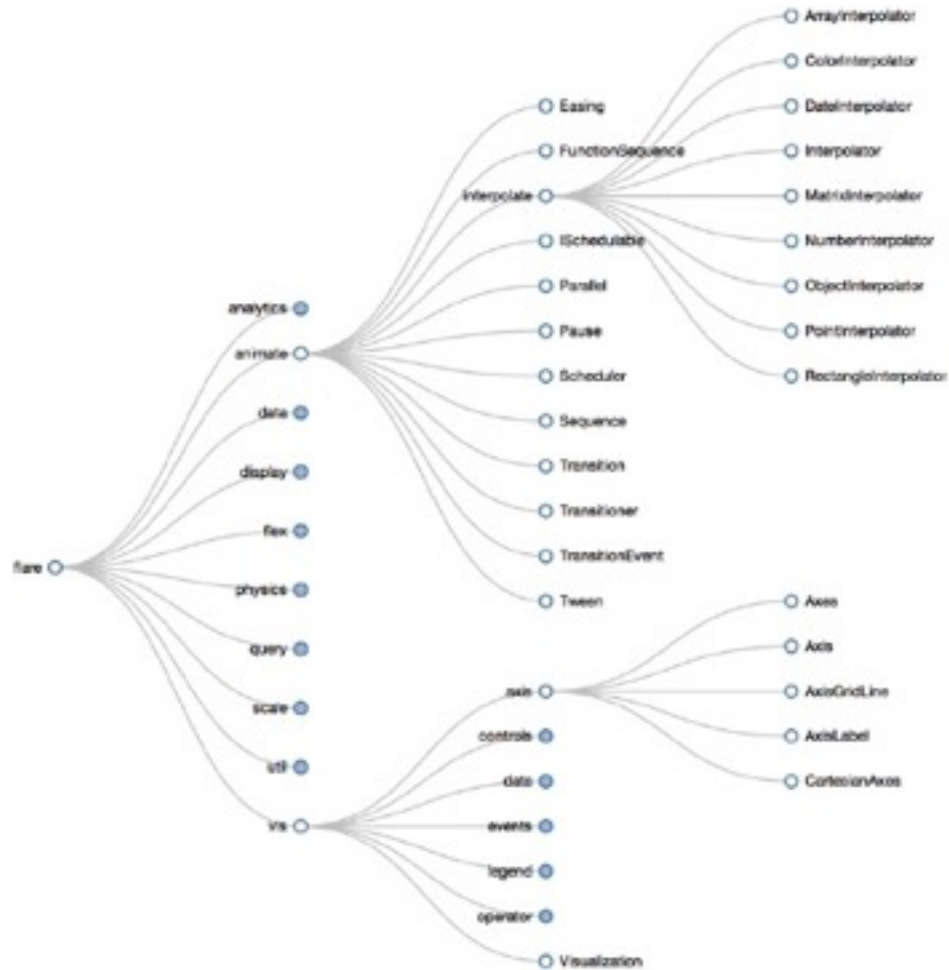
# Indented Layout



# Node-Link Diagrams

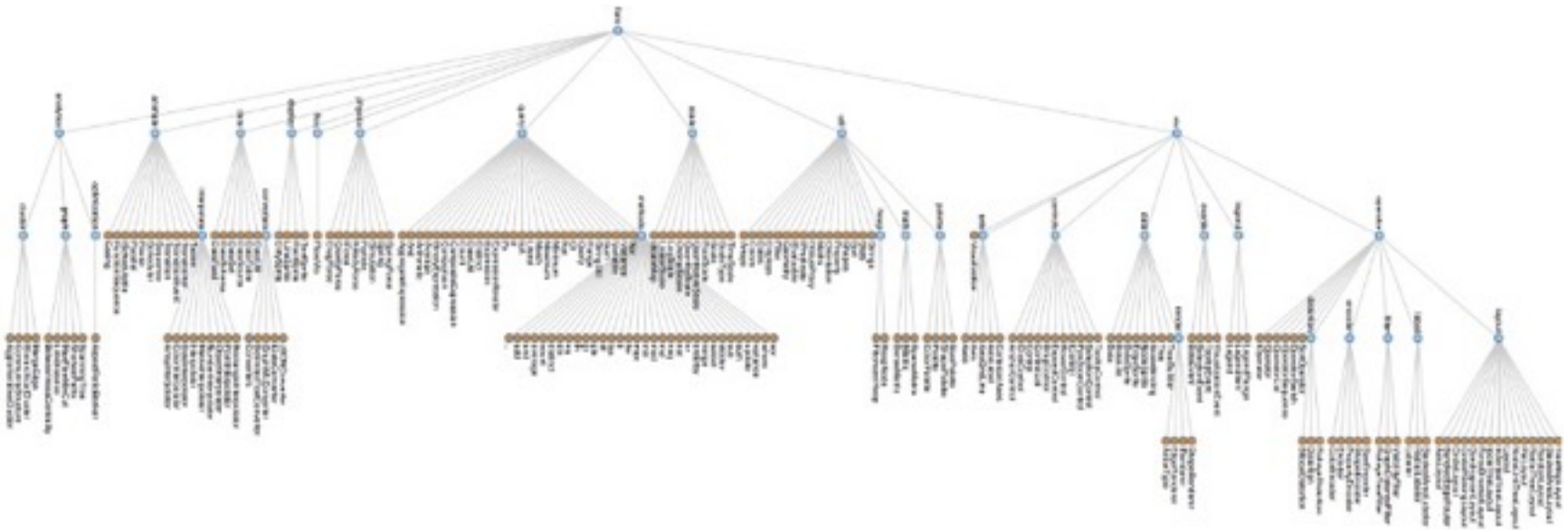
- Traditional Layout
  - Nodes laid out by level, root at top
  - Edges connect adjacent nodes
- Dendrogram
  - All leaves at bottom of diagram
  - Edges usually drawn with sharp corners
  - Often used to show clusters  
*(sometimes called cluster layout)*

# Traditional Layout



<http://mbostock.github.io/d3/talk/20111018/tree.html>

# Traditional Layout



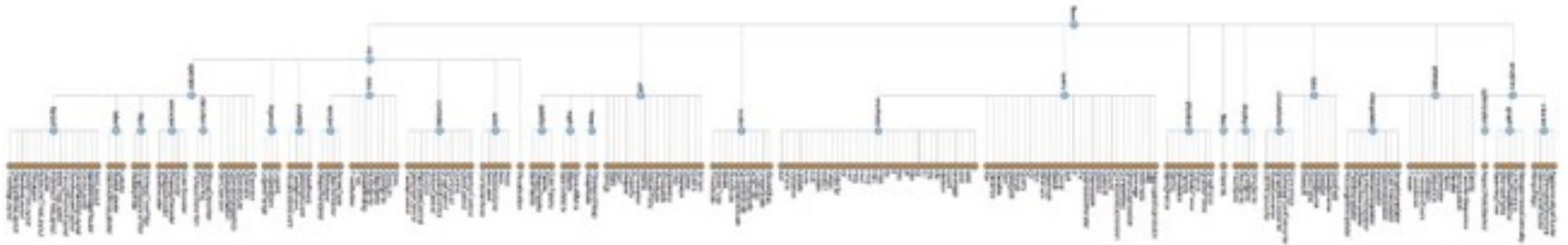
The Flare package tree laid out in horizontal layers. All the nodes in a given layer are at the same package depth.

Source: Flare Visualization Toolkit

<http://hci.stanford.edu/jheer/files/zoo/ex/hierarchies/tree.html>

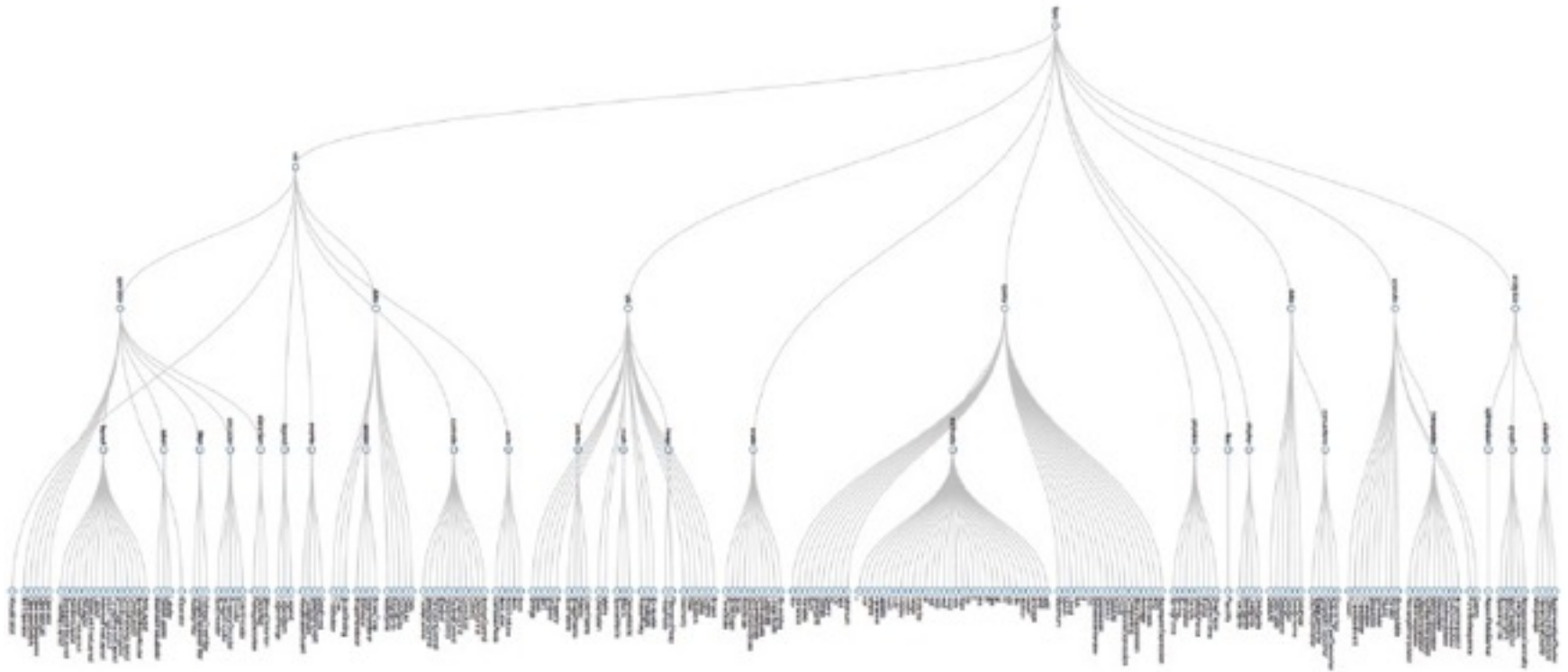


# Dendrogram



<http://mbostock.github.io/protovis/ex/dendrogram.html>

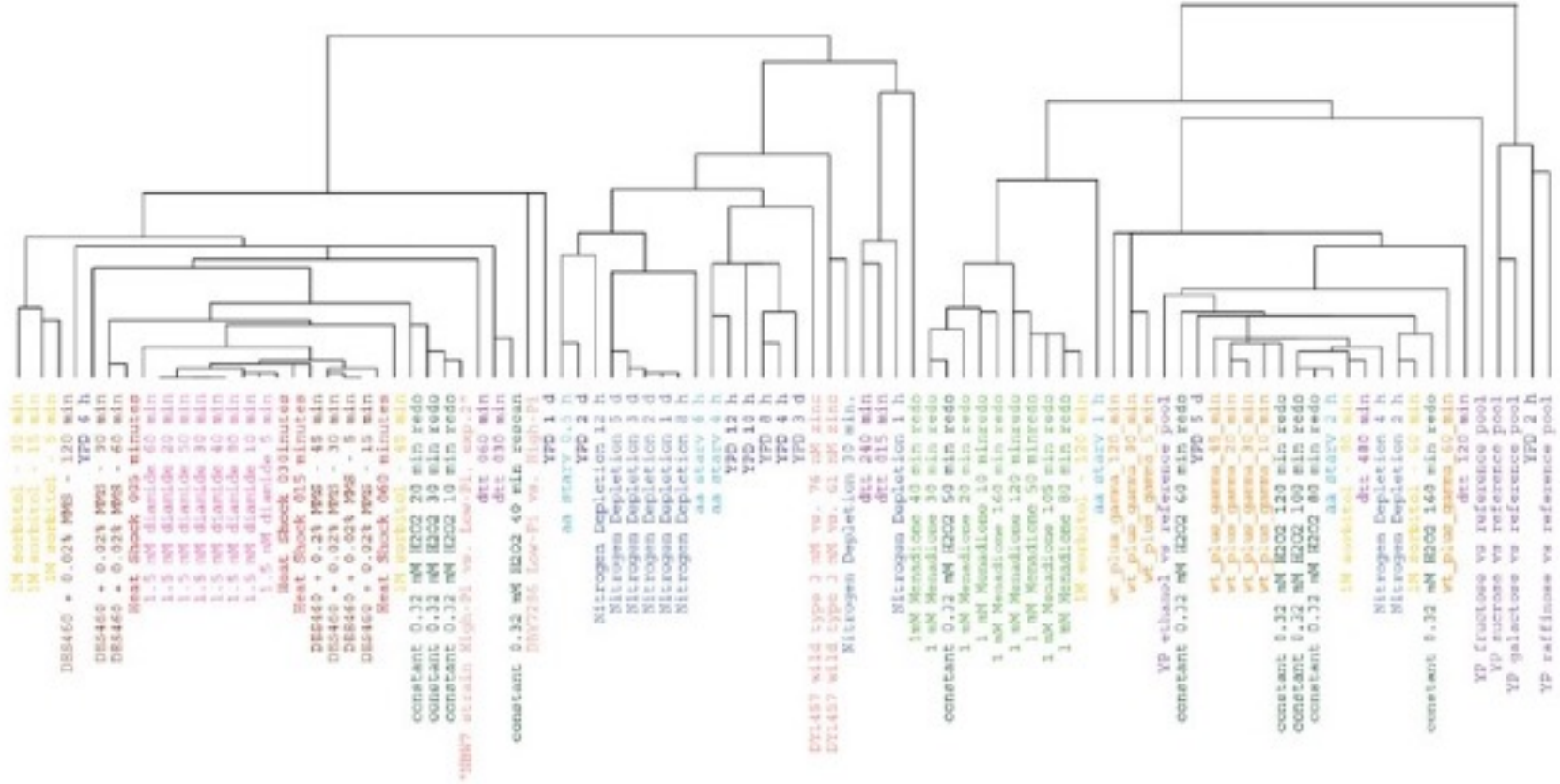
# Dendrogram



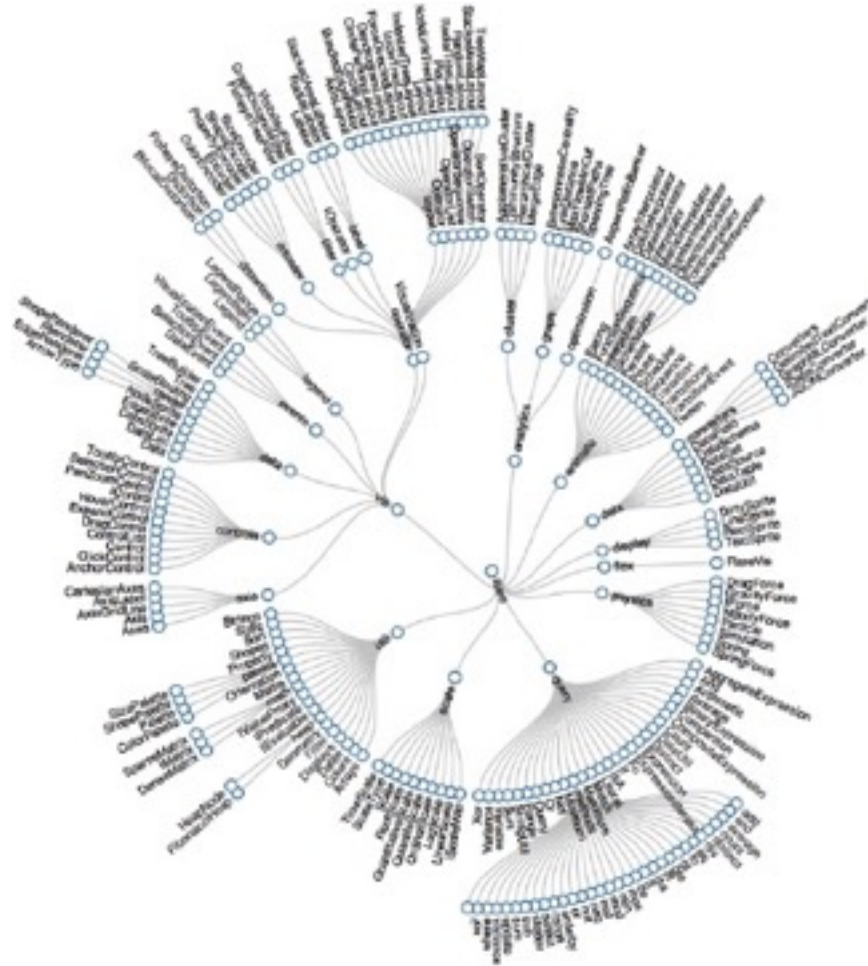
<http://mbostock.github.io/protovis/ex/dendrogram.html>

# Dendrogram

Cluster 11: protein folding chaperones

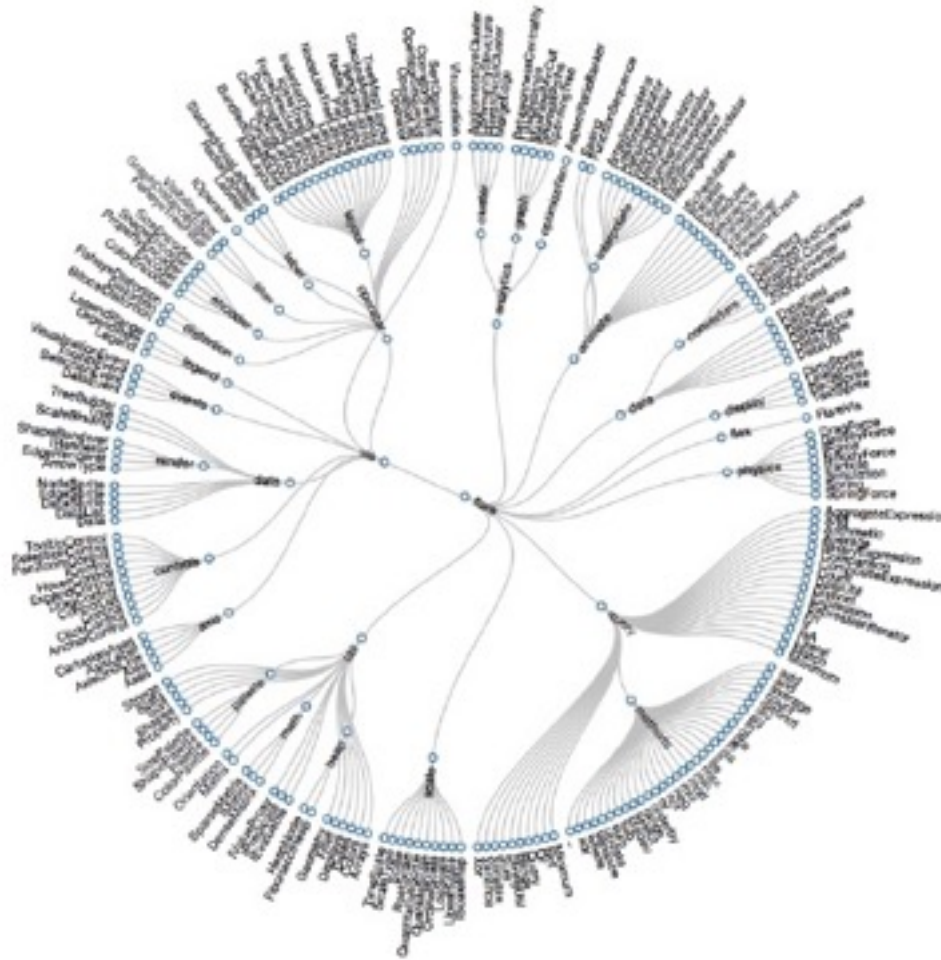


# Circular Layout



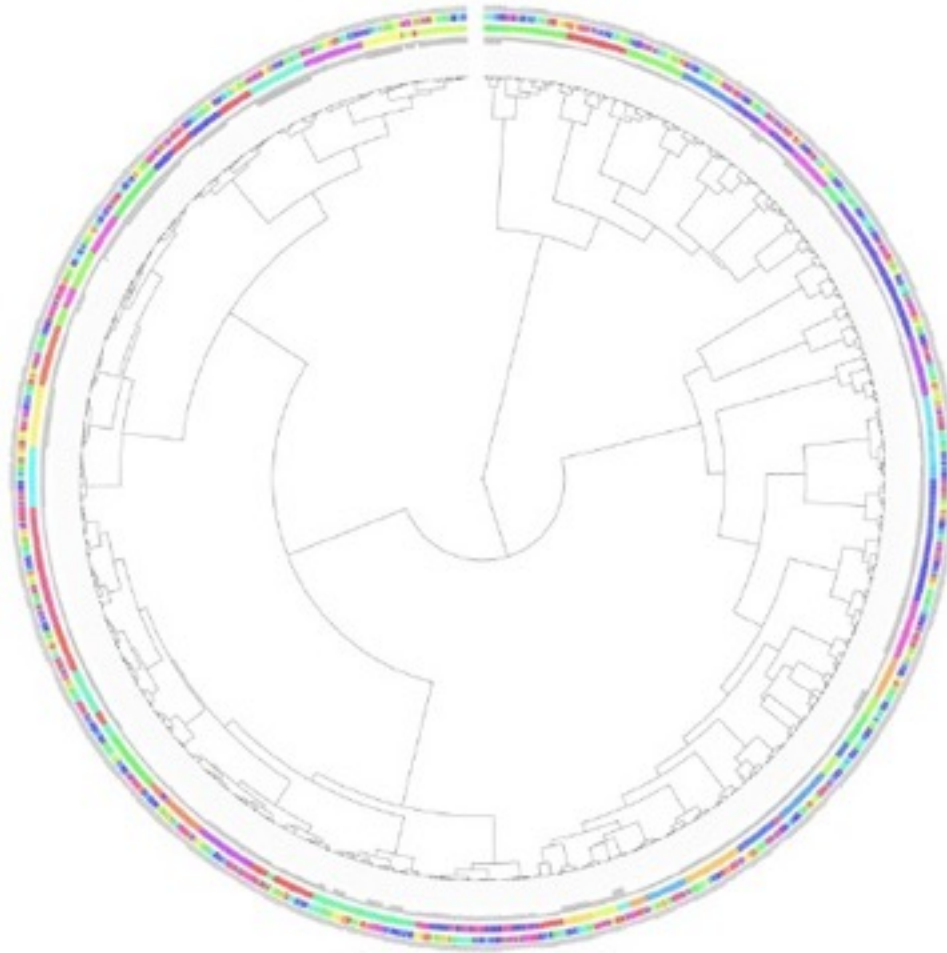
<http://bl.ocks.org/mbostock/4063550>

# Circular Dendrogram



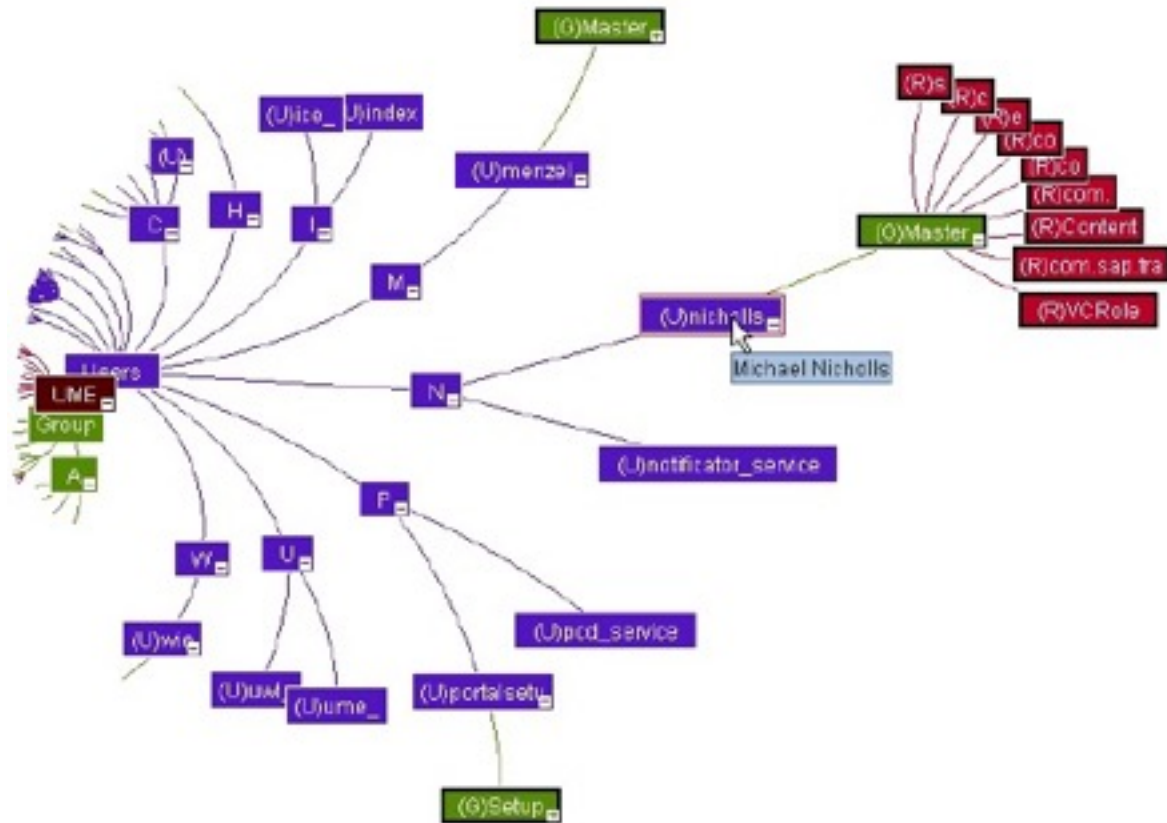
<http://mbostock.github.io/d3/talk/20111018/cluster.html>

# Circular Dendrogram



<http://cs.jhu.edu/~razvanm/fs-expedition/2.6.x.html>

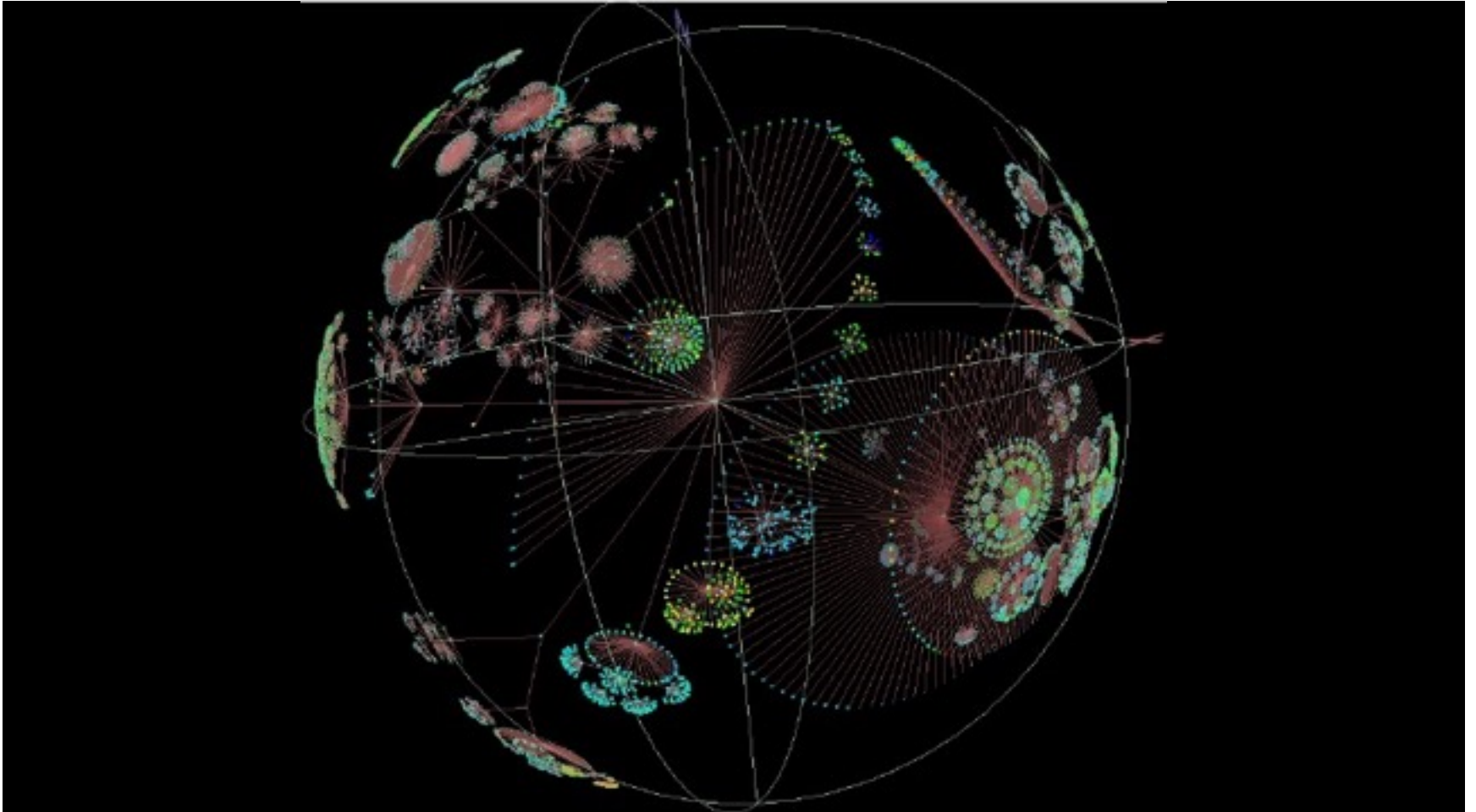
# Hyperbolic Tree



<http://wiki.sdn.sap.com/wiki/display/EmTech/StarTree+examples>



# Hyperbolic Tree (3D)



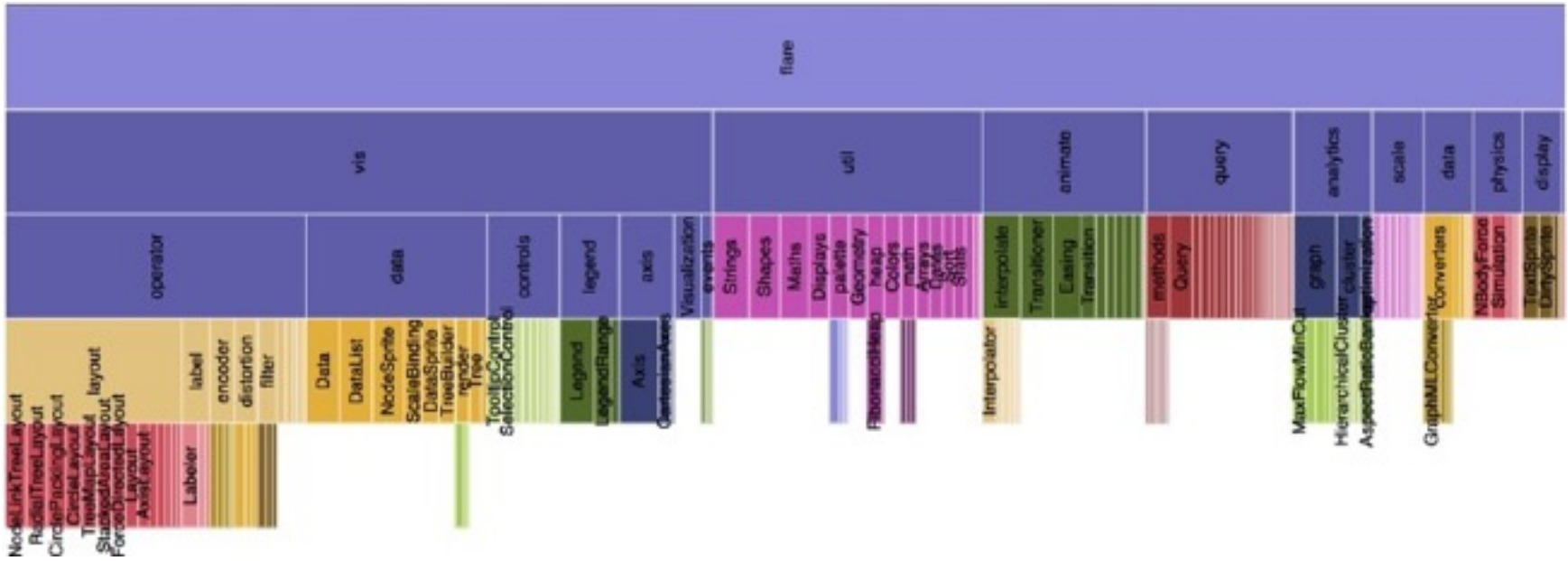
<http://www.caida.org/tools/visualization/walrus/>



# **SPACE-FILLING DIAGRAMS**

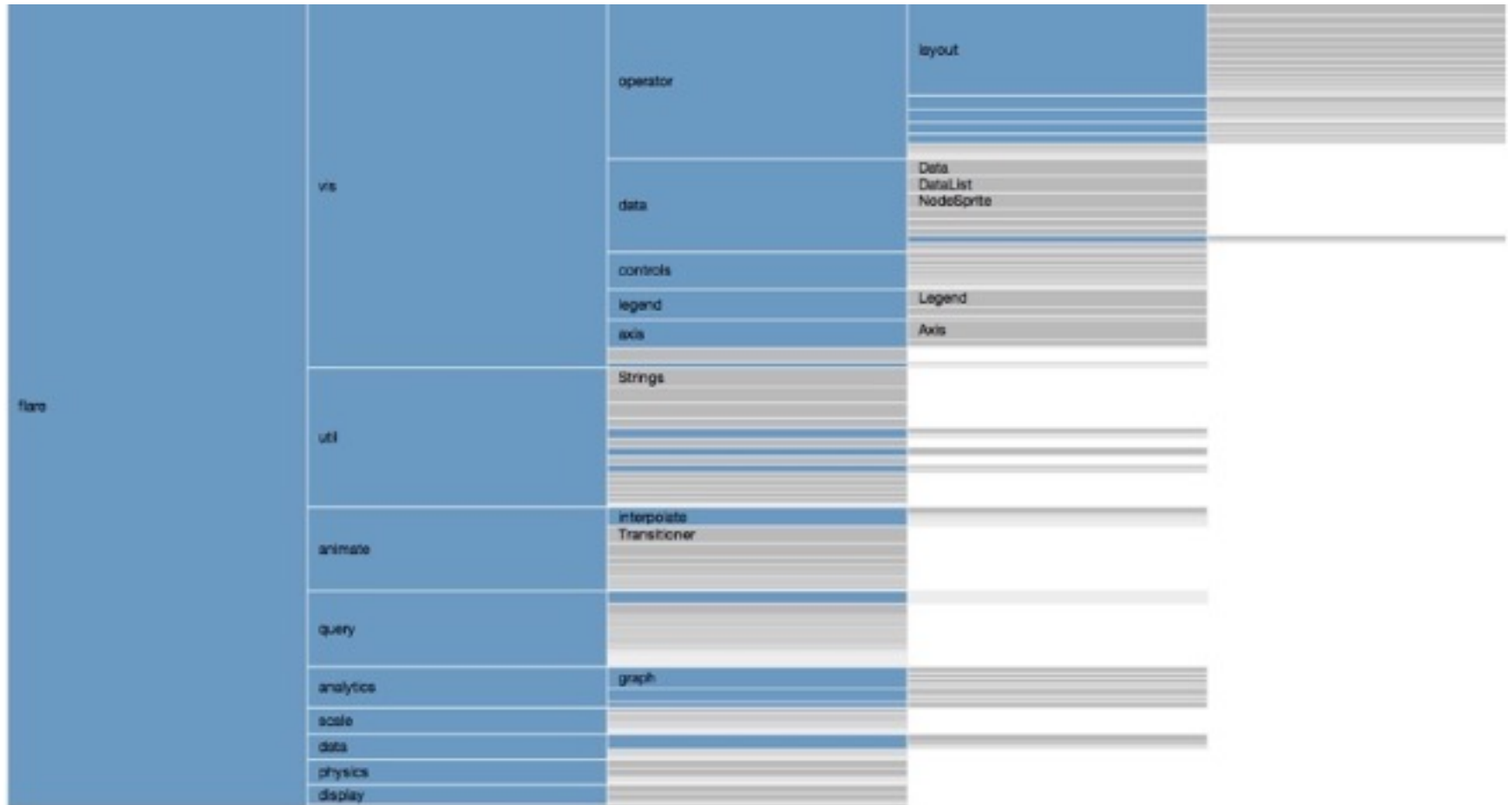
Tree Visualization

# Icicle Diagram



<http://mbostock.github.io/protovis/ex/icicle.html>

# Icicle Diagram



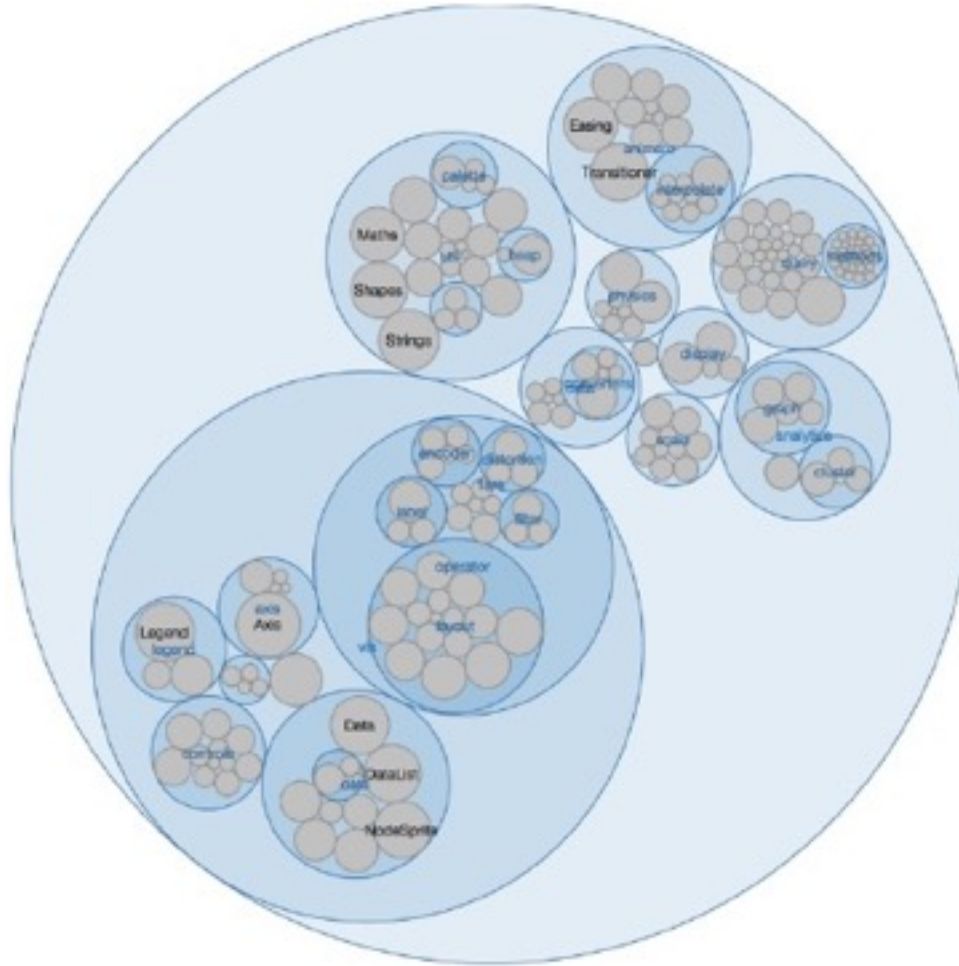
<http://mbostock.github.io/d3/talk/20111018/partition.html>

# Sunburst Diagram



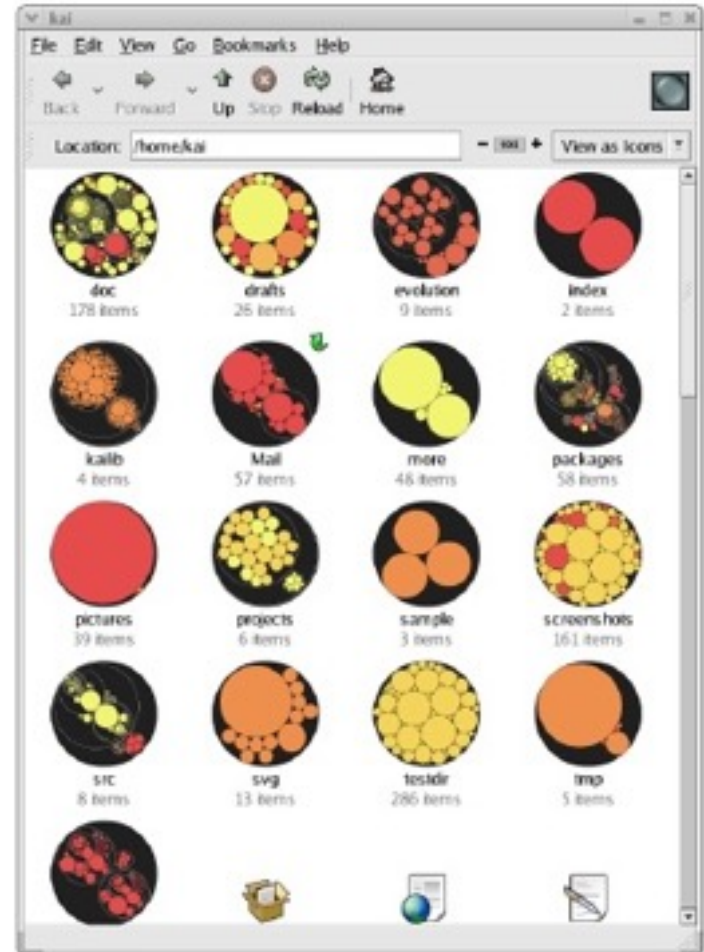
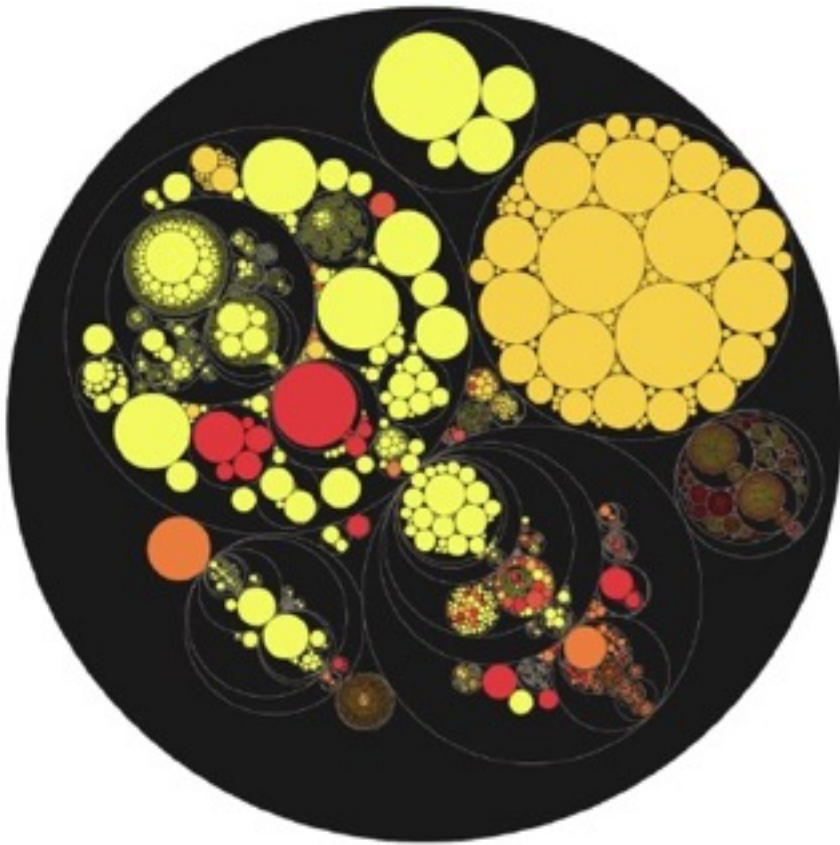
<http://bl.ocks.org/mbostock/4063423>

# Circle Packing



<http://mbostock.github.io/d3/talk/20111116/pack-hierarchy.html>

# Pebbles File Manager



<http://lip.sourceforge.net/ctreemap.html>

# PRTG Network Monitor



[https://prtg.paessler.com/help/general\\_layout.htm](https://prtg.paessler.com/help/general_layout.htm)

# TREEMAPS

Space-Filling Diagrams



# Treemaps

- Root is entire rectangle
- Recursively divide rectangles to show levels
- Two common visualization tasks
  - Promote comparison
  - Visualize hierarchy
- Task affects encoding
  - Use of color, outlines, shading, etc.
- See <http://www.cs.umd.edu/hcil/treemap-history/>

# Treemaps



<http://bl.ocks.org/mbostock/4063582>

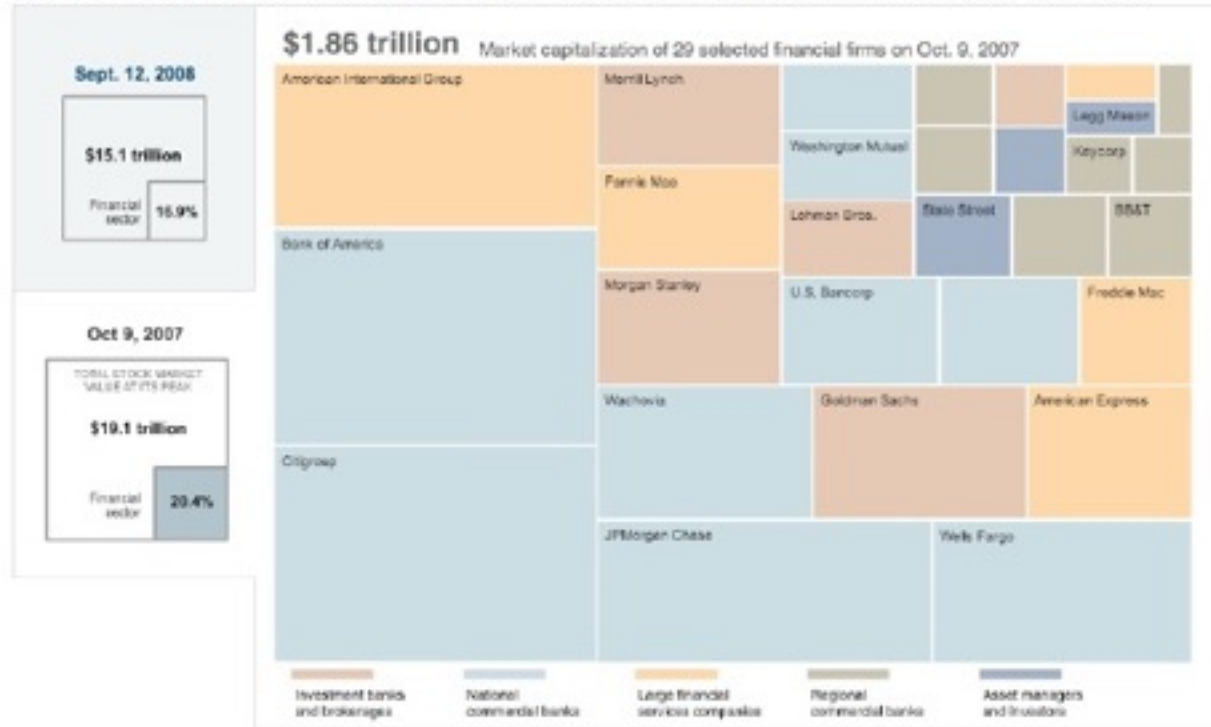
# A Year of Heavy Losses

September 15, 2008

SIGN IN TO E-MAIL OR SAVE THIS | FEEDBACK

## A Year of Heavy Losses

A year ago, financial companies were flying high. But as problems in the mortgage and credit markets have grown, the stocks of many Wall Street firms have been hard hit. Some of the biggest companies have been bought out, taken over by the government or gone bankrupt.



These two snapshots of the U.S. stock market and the financial sector are based on the Dow Jones Wilshire 5000 index, the market's broadest measure. Each box represents the market value of one company, which is found by multiplying the number of a company's shares outstanding by its stock price.

Source: Wilshire Associates

Kevin Quinlan and Dylan Loeb McClain / The New York Times

<http://www.nytimes.com/interactive/2008/09/15/business/20080916-treemap-graphic.html>

# How the Giants of Finance Shrank



<http://www.nytimes.com/interactive/2009/09/12/business/financial-markets-graphic.html>

# Billion-Dollar-O-Gram



<http://www.informationisbeautiful.net/visualizations/the-billion-dollar-o-gram-2009/>

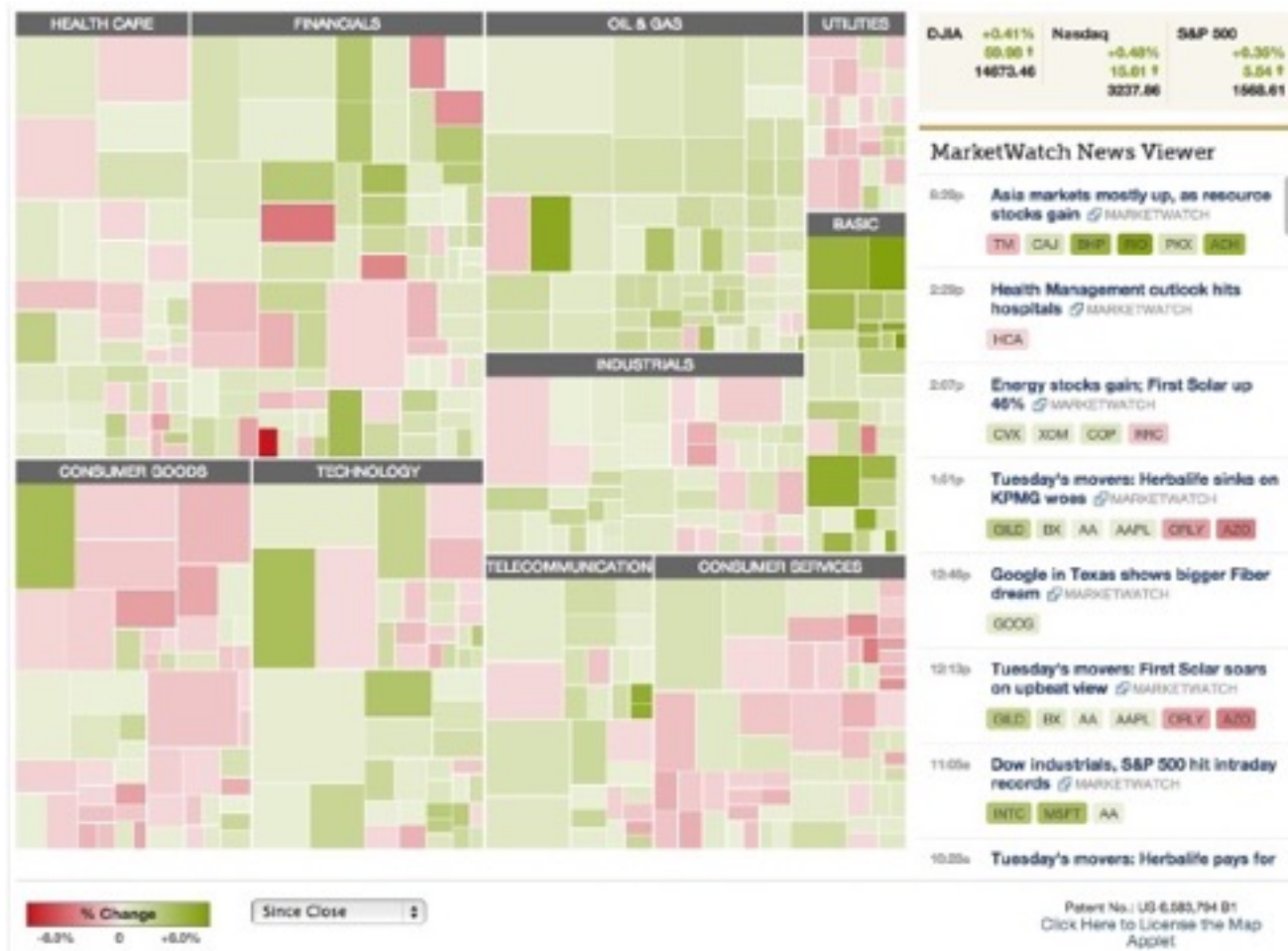
# Billion-Dollar-O-Gram

\$11,900 Worldwide cost of financial crisis



<http://www.informationisbeautiful.net/visualizations/the-billion-dollar-o-gram-2009/>

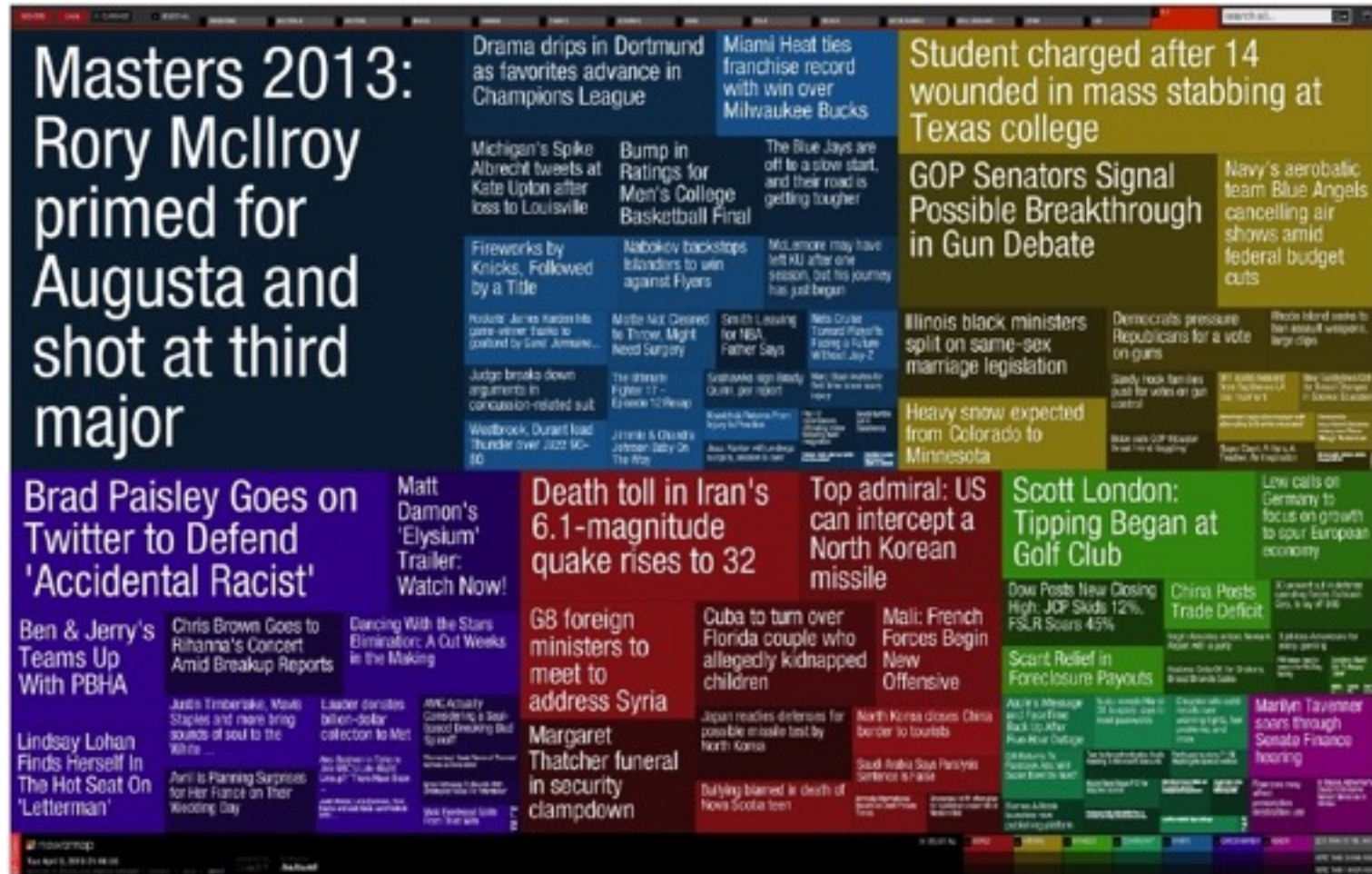
# Map of the Market



<http://www.smartmoney.com/map-of-the-market/>



# News Map



<http://newsmap.jp/>



# Cushion Treemap

## Cushion TreeMaps

In this example a static JSON tree is loaded into a Cushion Treemap.

Left click to set a node as root for the visualization.

Right click to set the parent node as root for the visualization.

You can choose a different tiling algorithm below:

- Squarified
- Strip
- SliceAndDice

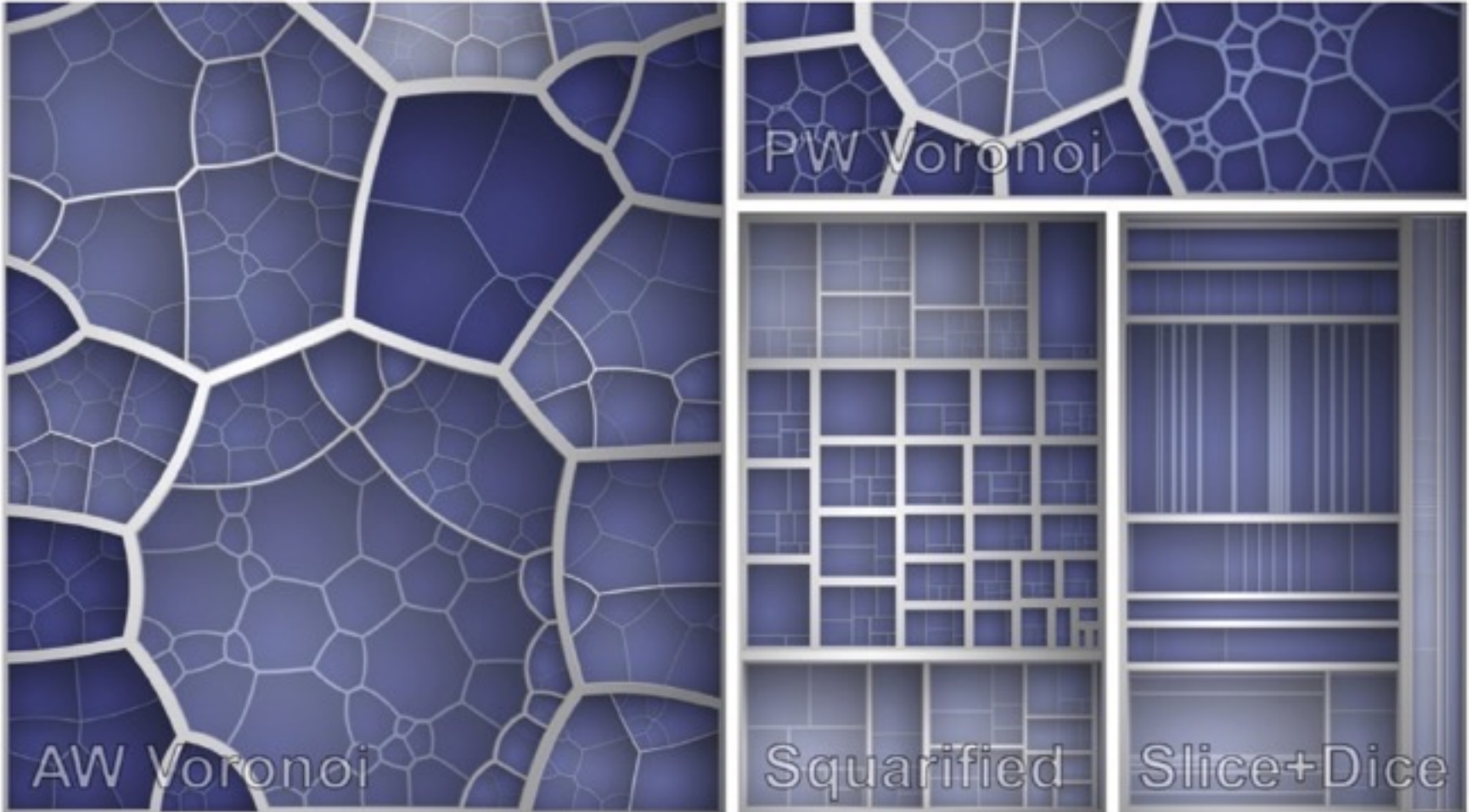
Go to Parent

[See the Example Code](#)

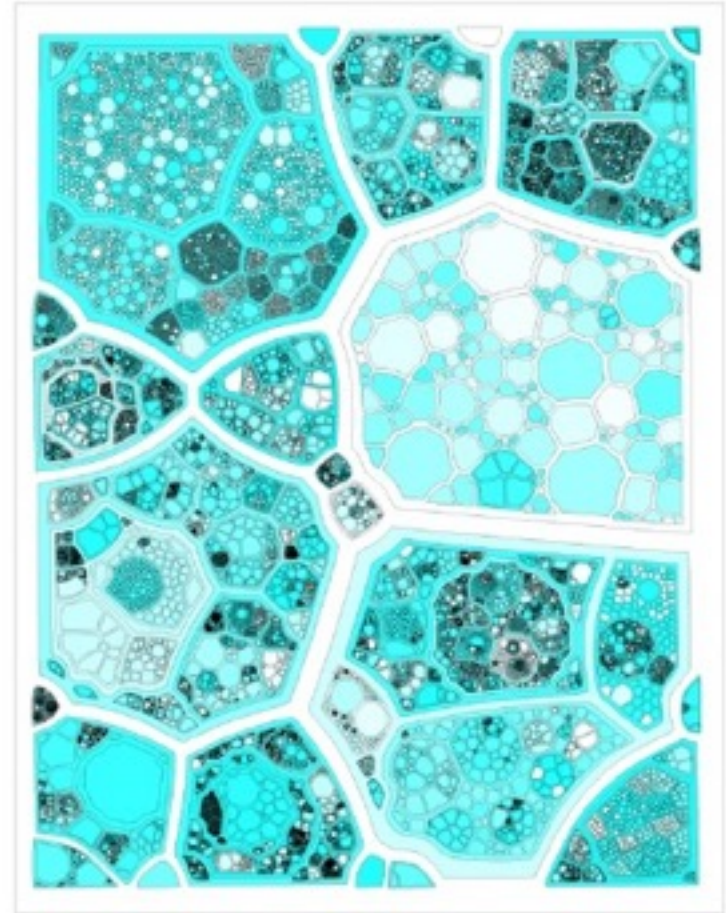
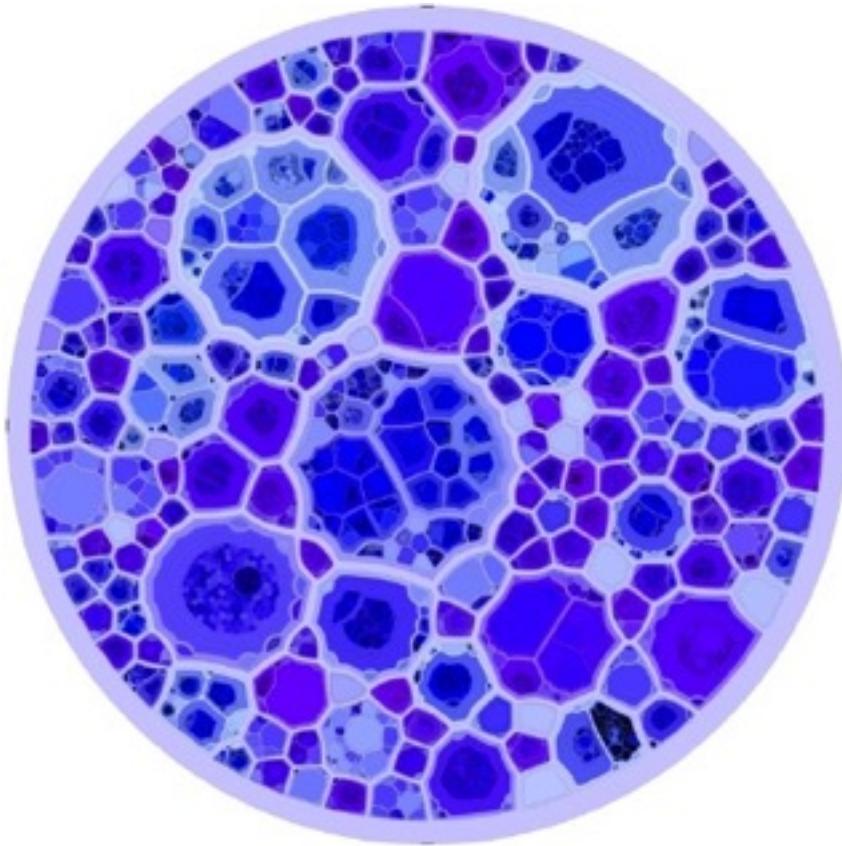


<http://philogb.github.io/jit/static/v20/Jit/Examples/Treemap/example3.html>

# Voronoi Treemaps



# Voronoi Treemaps



<http://graphics.uni-konstanz.de/~deussen/php/voronoitreemaps.php>

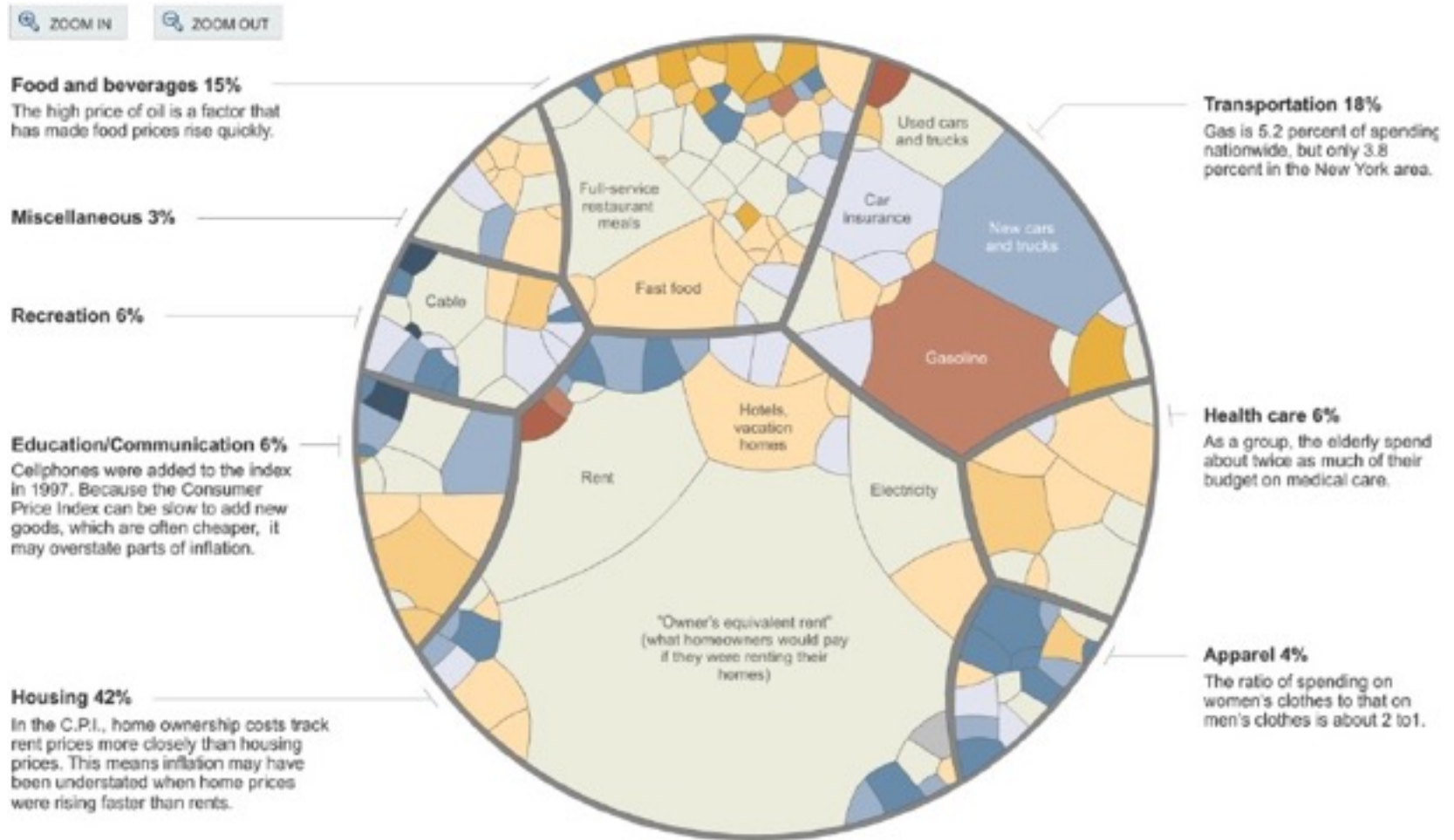


# KEGG-Orthology Treemap



<http://www.nature.com/ncomms/journal/v1/n9/full/ncomms1137.html>

# All of Inflation's Little Parts



[http://www.nytimes.com/interactive/2008/05/03/business/20080403\\_SPENDING\\_GRAPHIC.html](http://www.nytimes.com/interactive/2008/05/03/business/20080403_SPENDING_GRAPHIC.html)

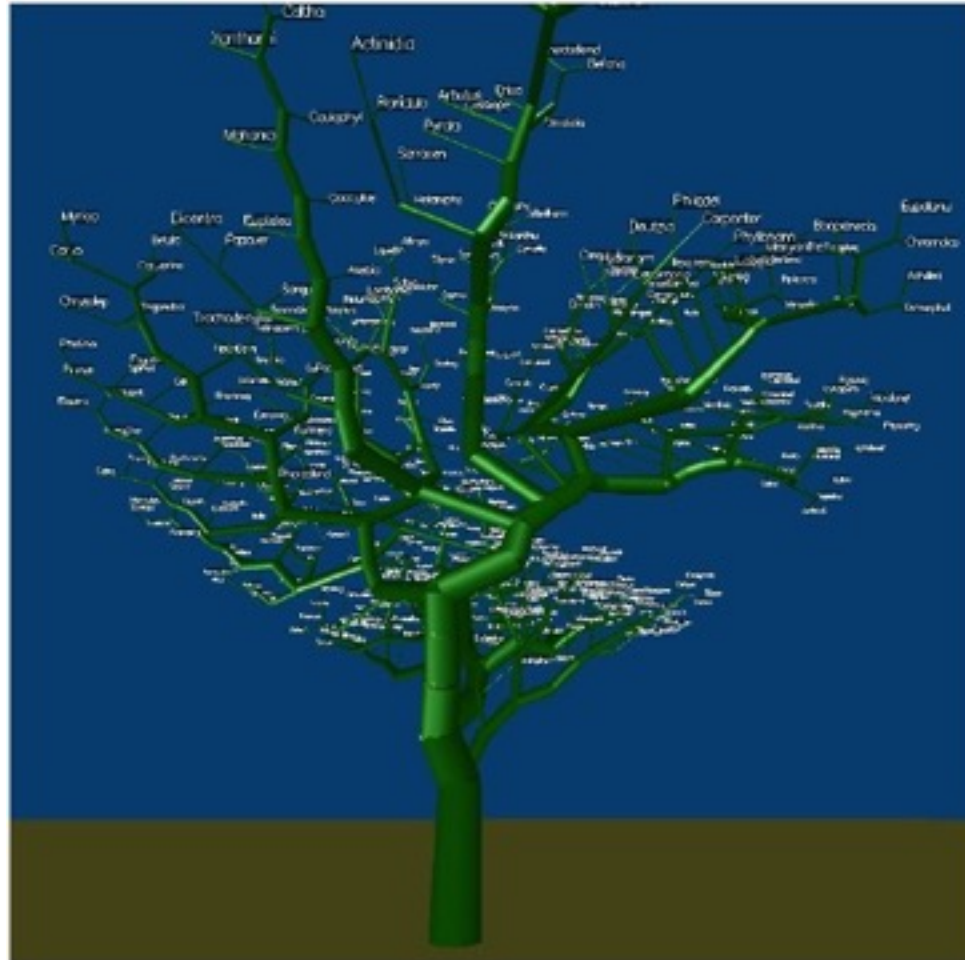
# **TREE OF LIFE**

## Case Study

# Tree of Life

- Specifically phylogenetic tree of life
  - Evolutionary tree, showing where species branch
- Can be thousands to tens of thousands of nodes
- Many tools for the ToL exist using different visualization techniques
- See <http://tolweb.org/tree/phylogeny.html>

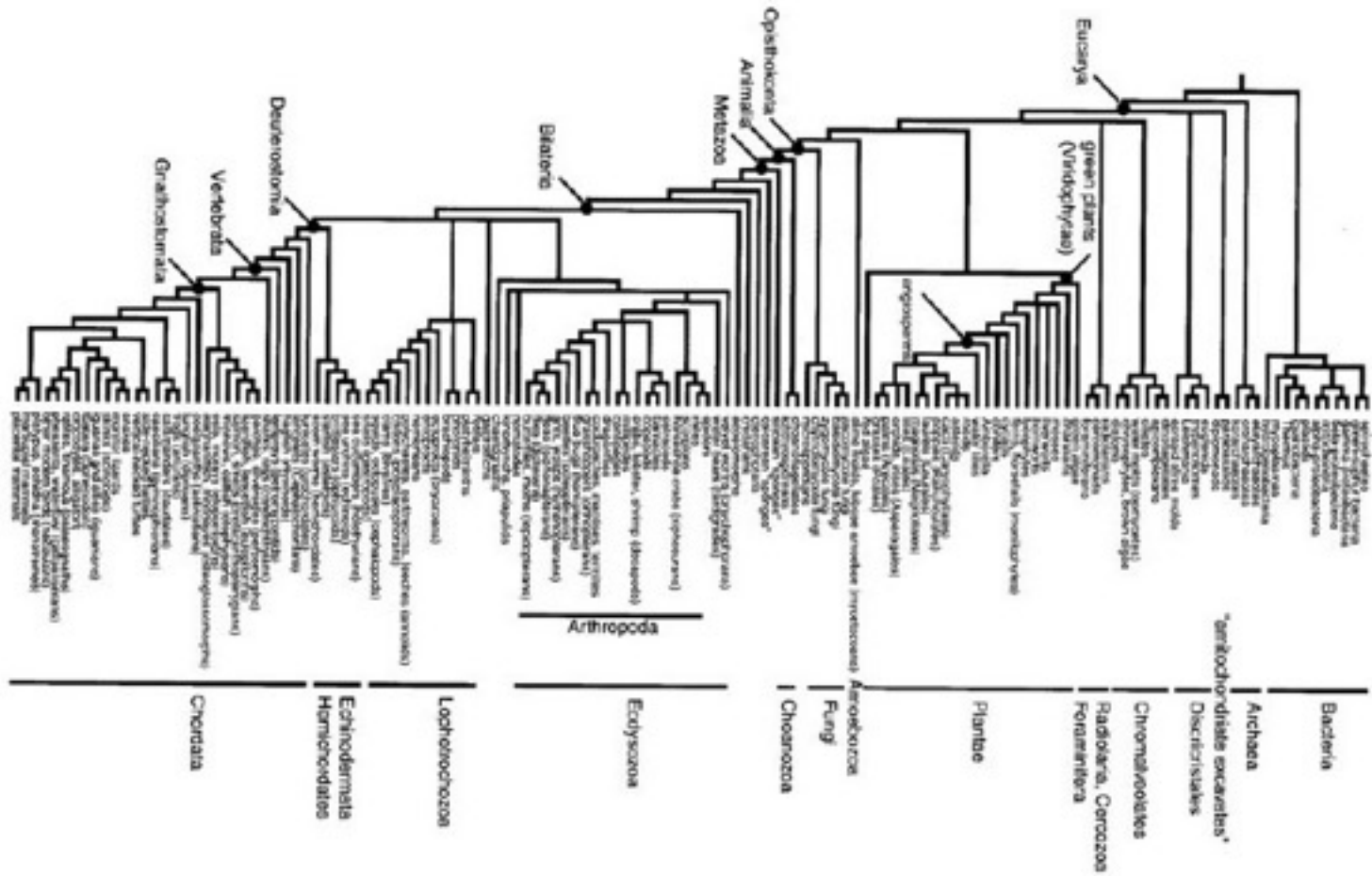
# Paloverde



<http://loco.biosci.arizona.edu/paloverde/paloverde.html>

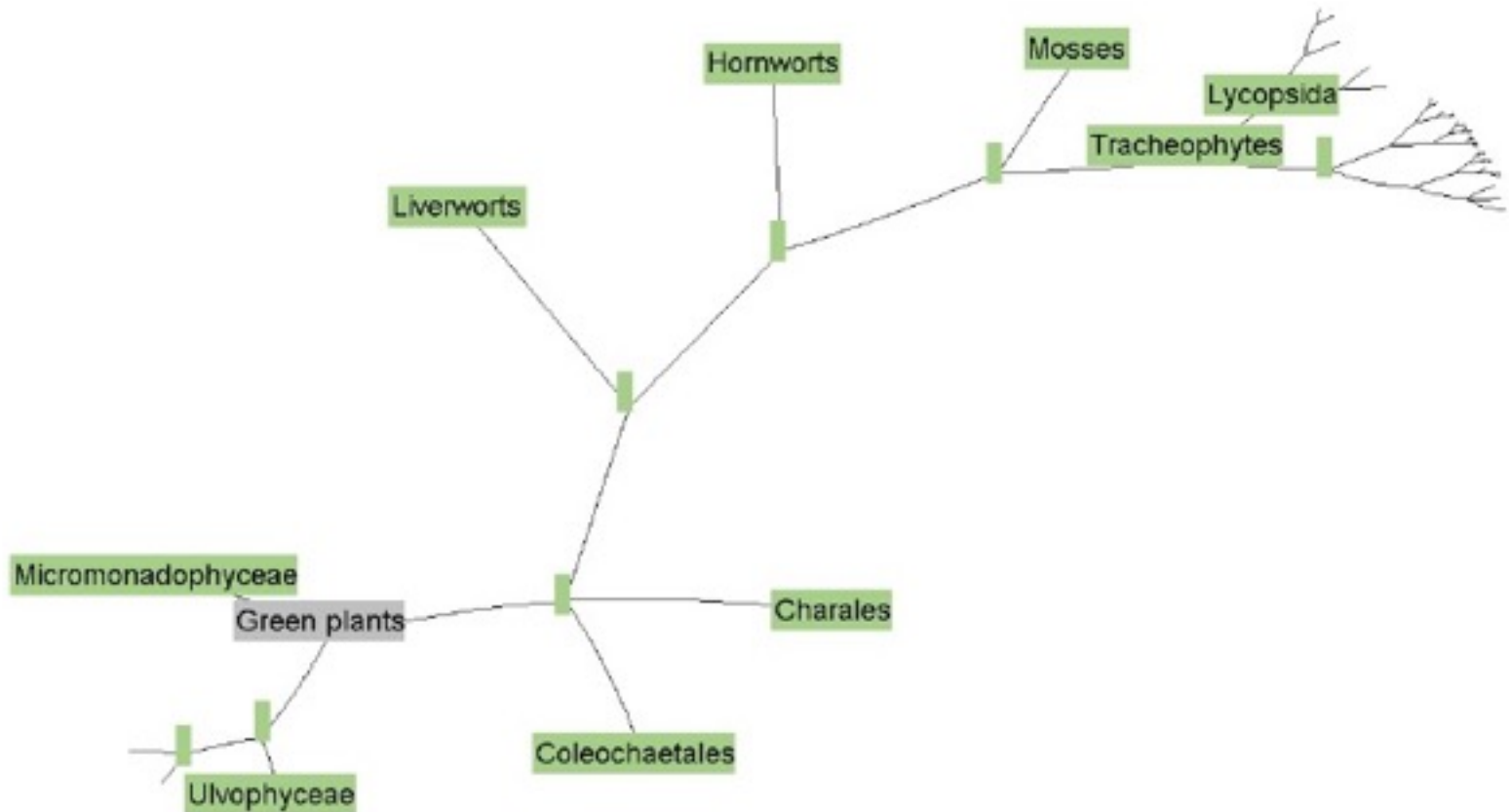


# Teachable ToL



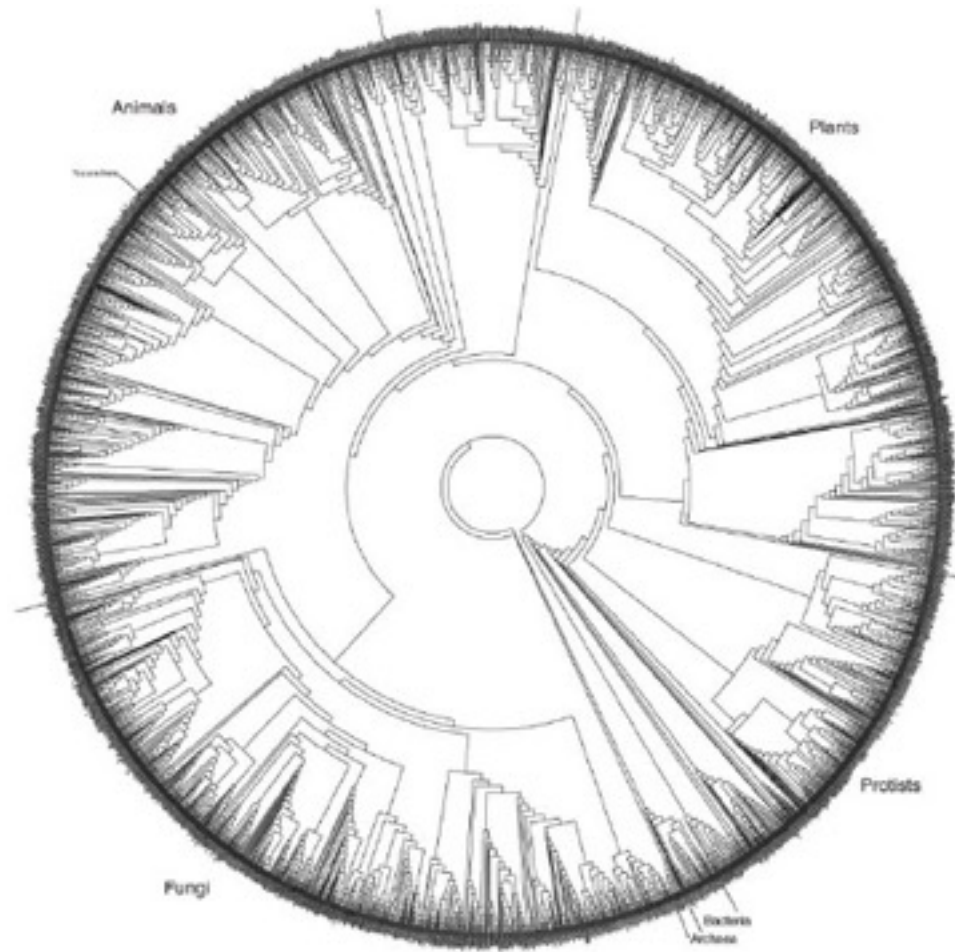
<http://www.rebeccashapley.com/cipres/telescoping.htm>

# Hyperbolic ToL (Plants Only)



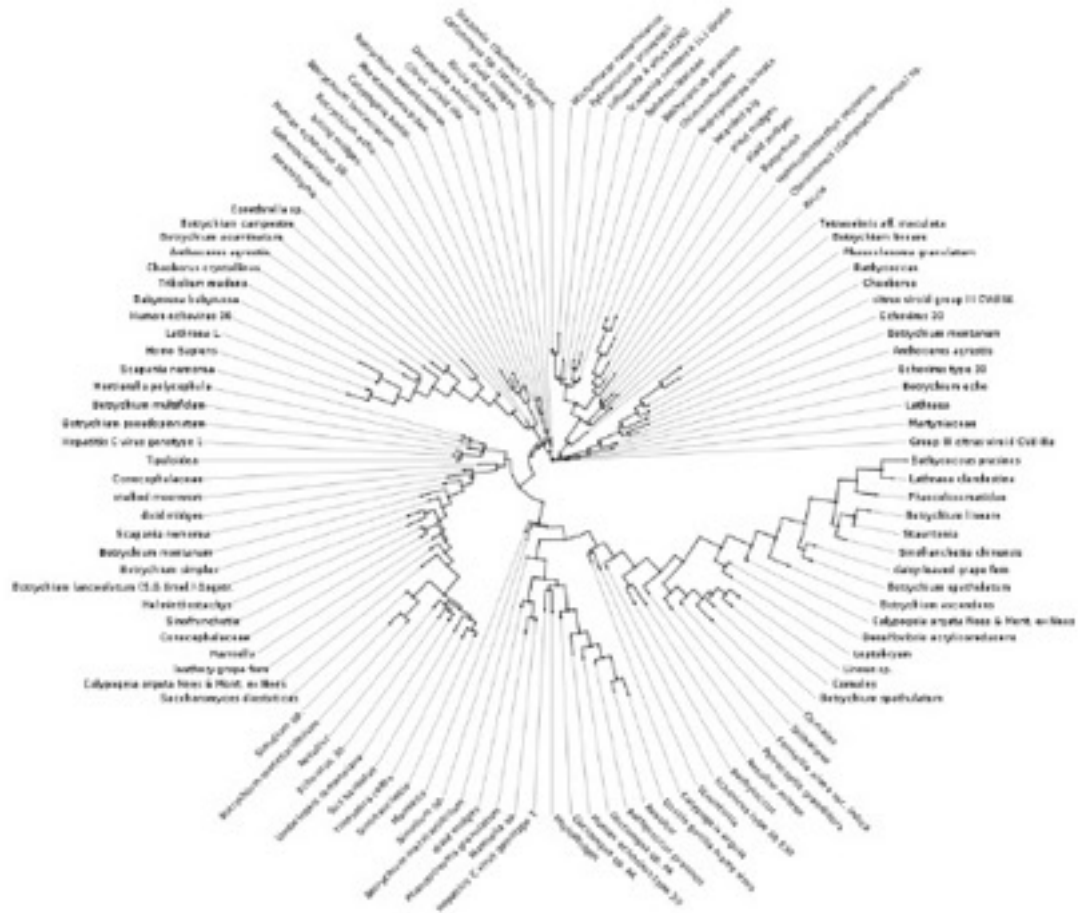
<http://ucjeps.berkeley.edu/TreeofLife/hyperbolic.php>

# Subset of 3,000 Species



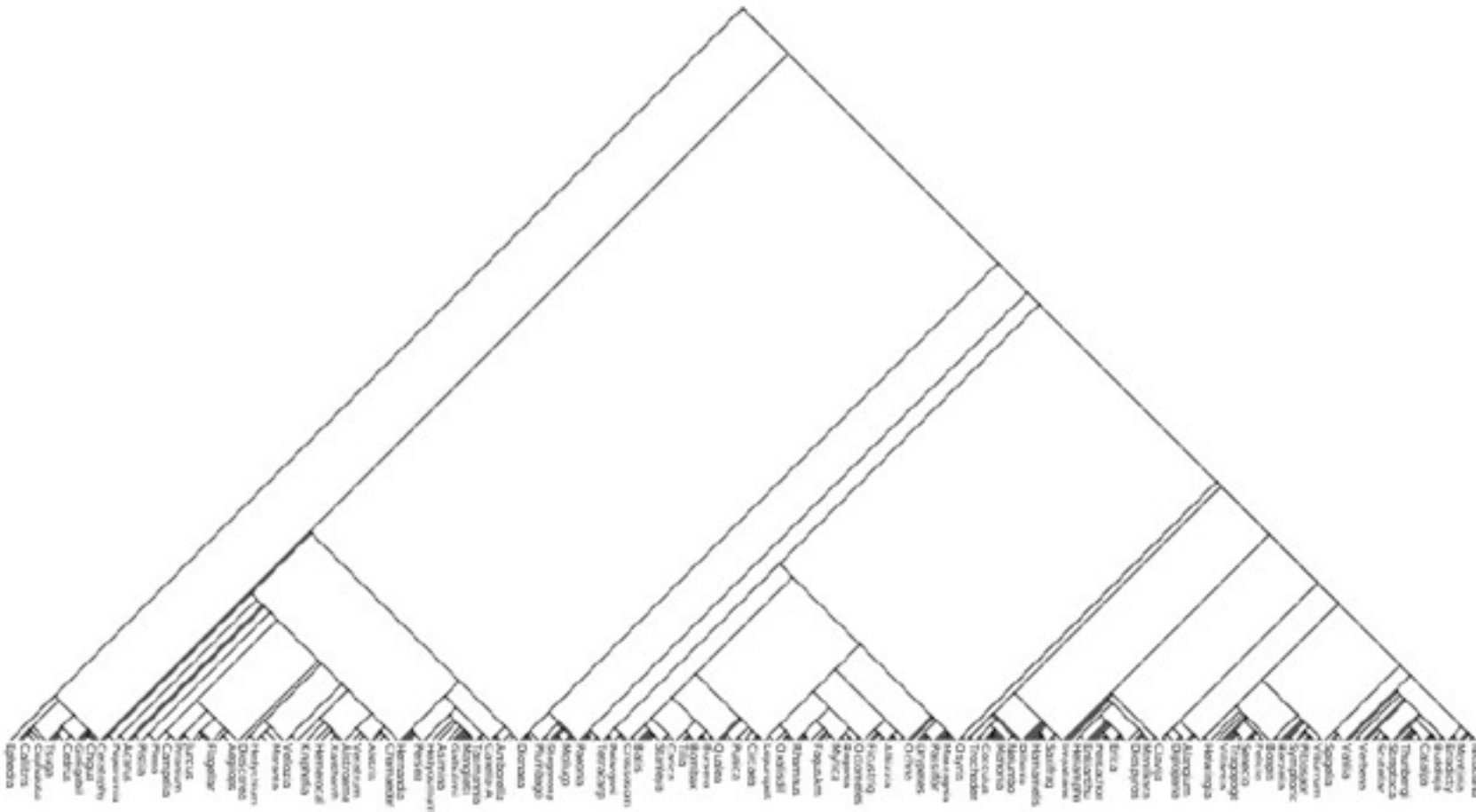
<http://www.zo.utexas.edu/faculty/antisense/DownloadfilesToL.html>

# PhyloWidget



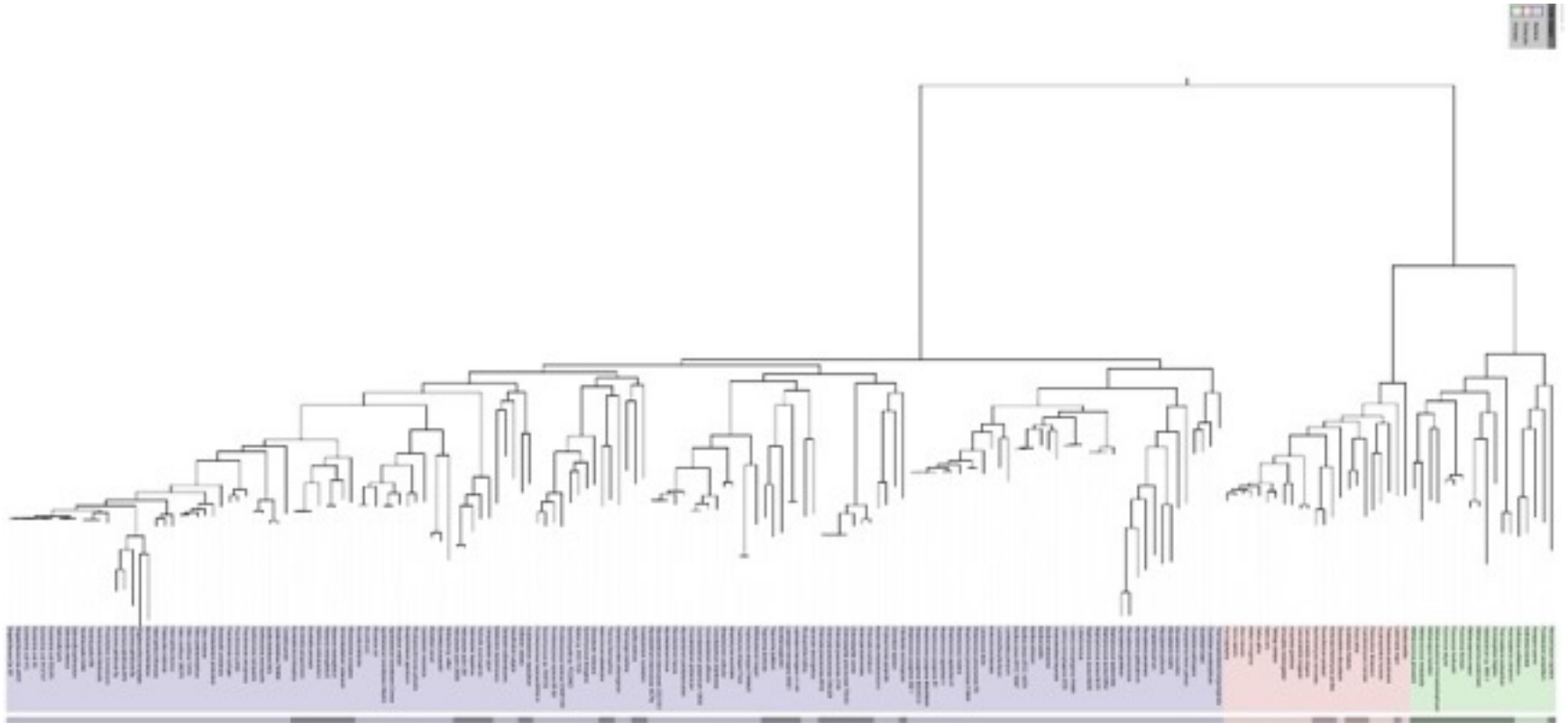
<http://www.phylowidget.org/>

# Phylo Widget



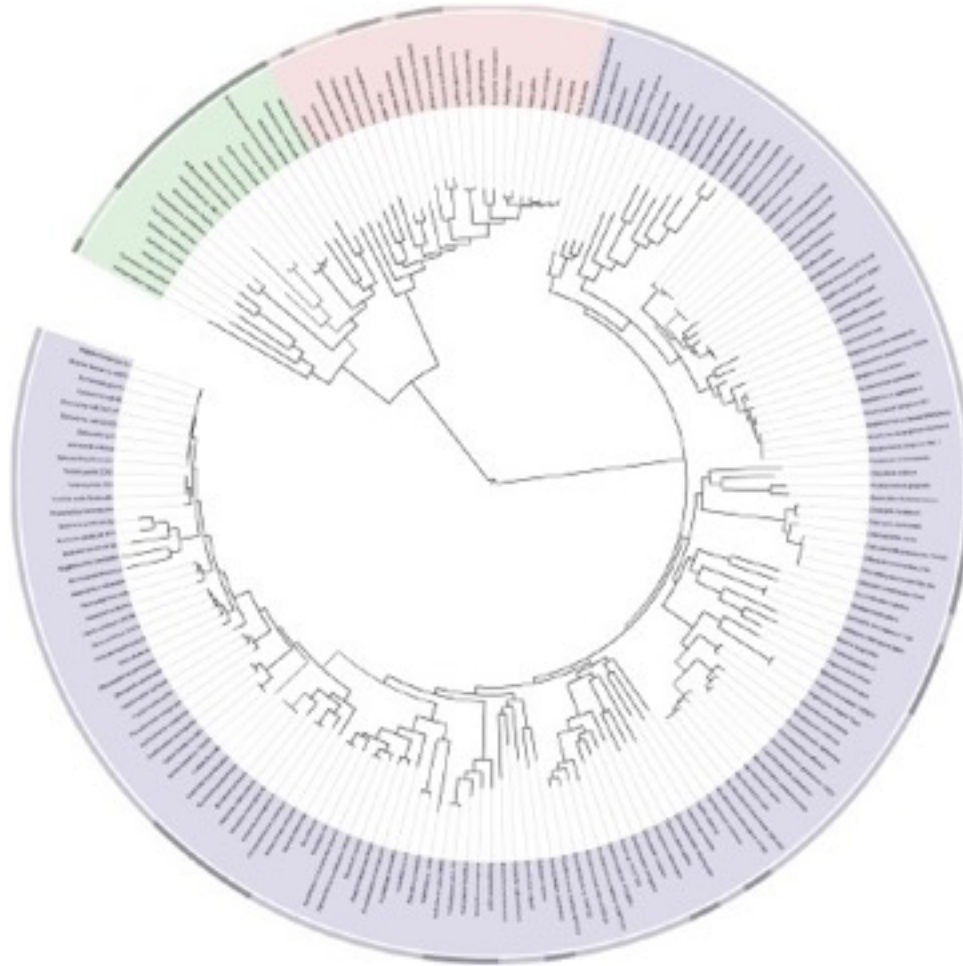
<http://www.phylowidget.org/>

# Interactive ToL



<http://itol.embl.de/>

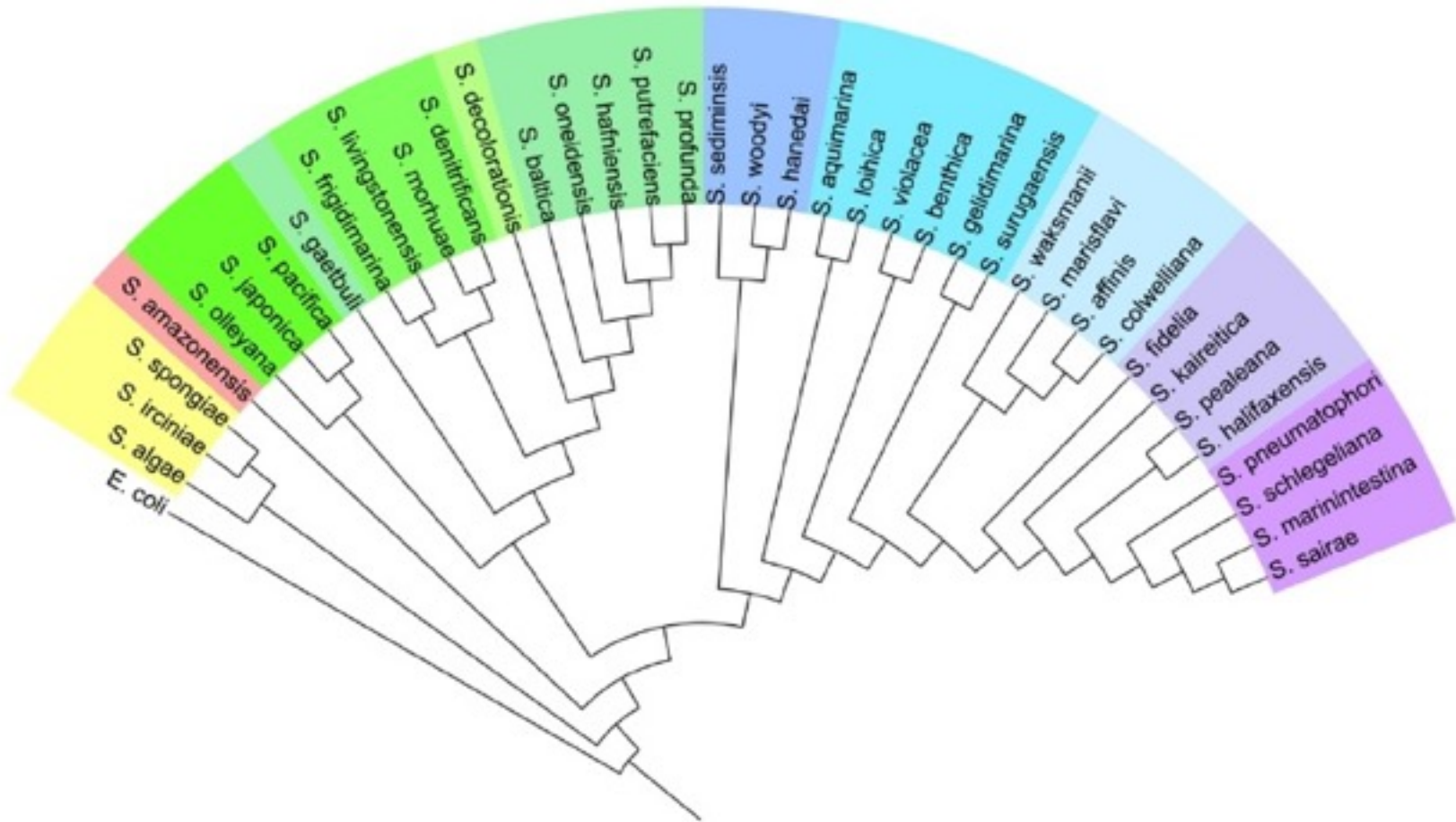
# Interactive ToL



<http://itol.embl.de/>



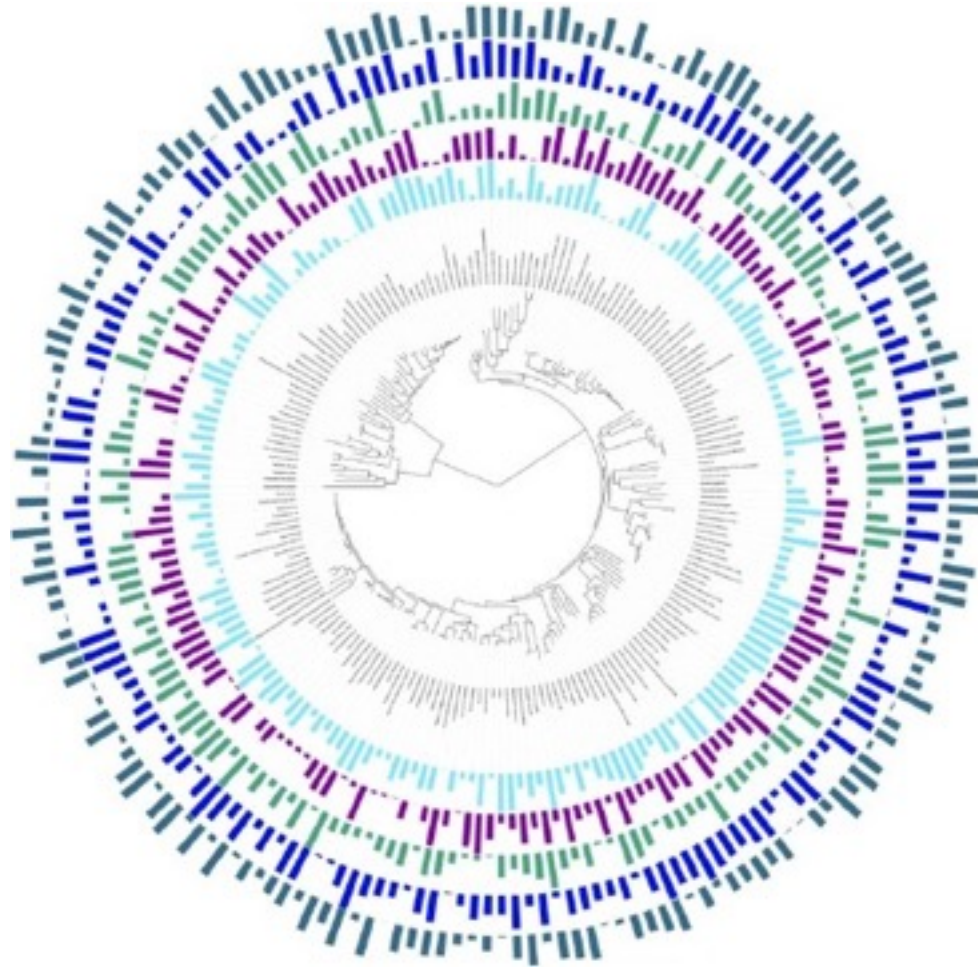
# Interactive ToL



<http://itol.embl.de/>

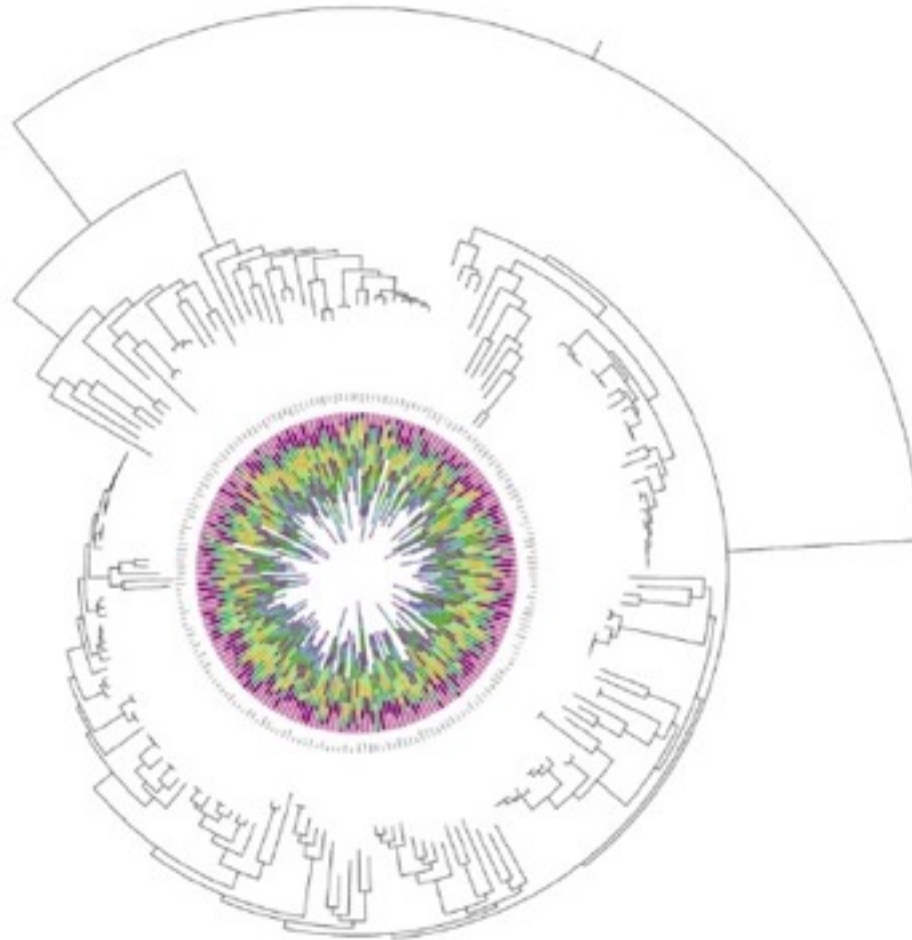


# Interactive ToL



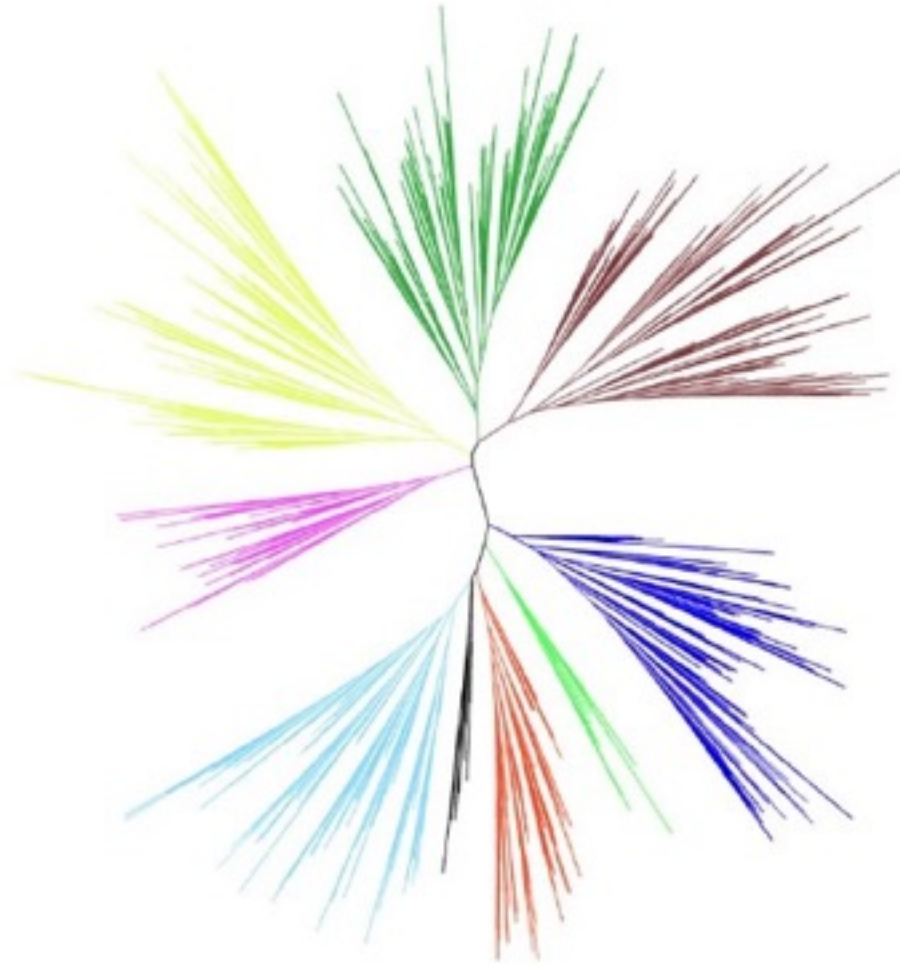
<http://itol.embl.de/>

# Interactive ToL



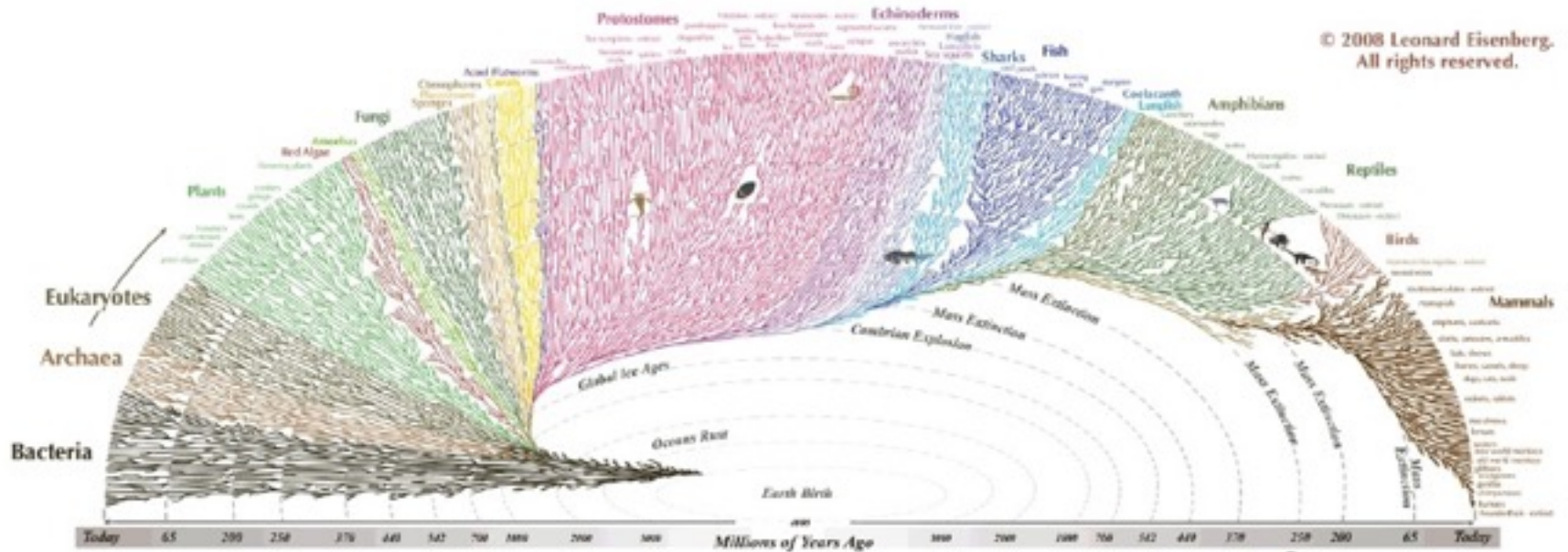
<http://itol.embl.de/>

# Interactive ToL



<http://itol.embl.de/>

# Illustration

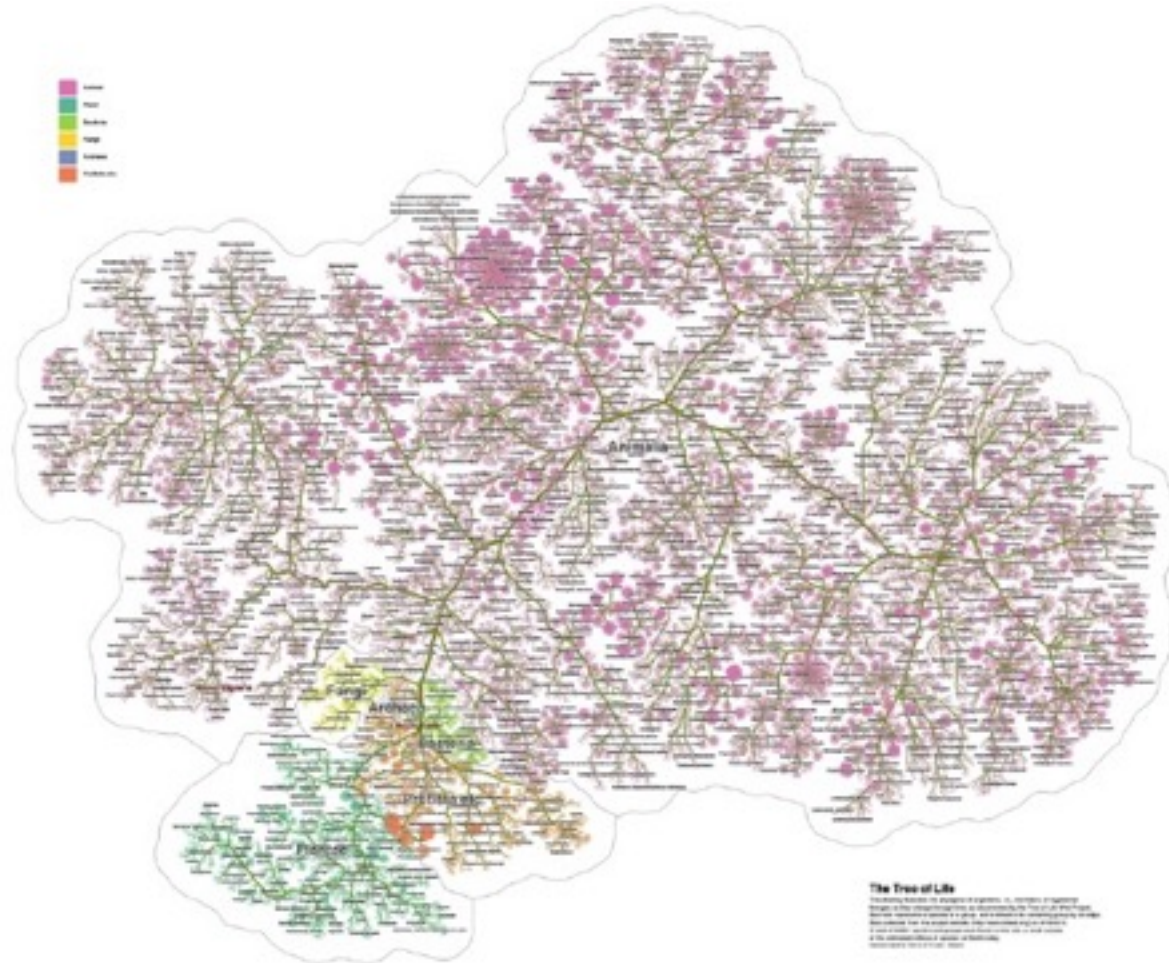


All the major and many of the minor living branches of life are shown on this diagram, but only a few of those that have gone extinct are shown. Example: Dinosaur - extinct  © 2008 Leonard Eisenberg. All rights reserved. <http://www.evogeneao.com/>

<http://www.evogeneao.com/>

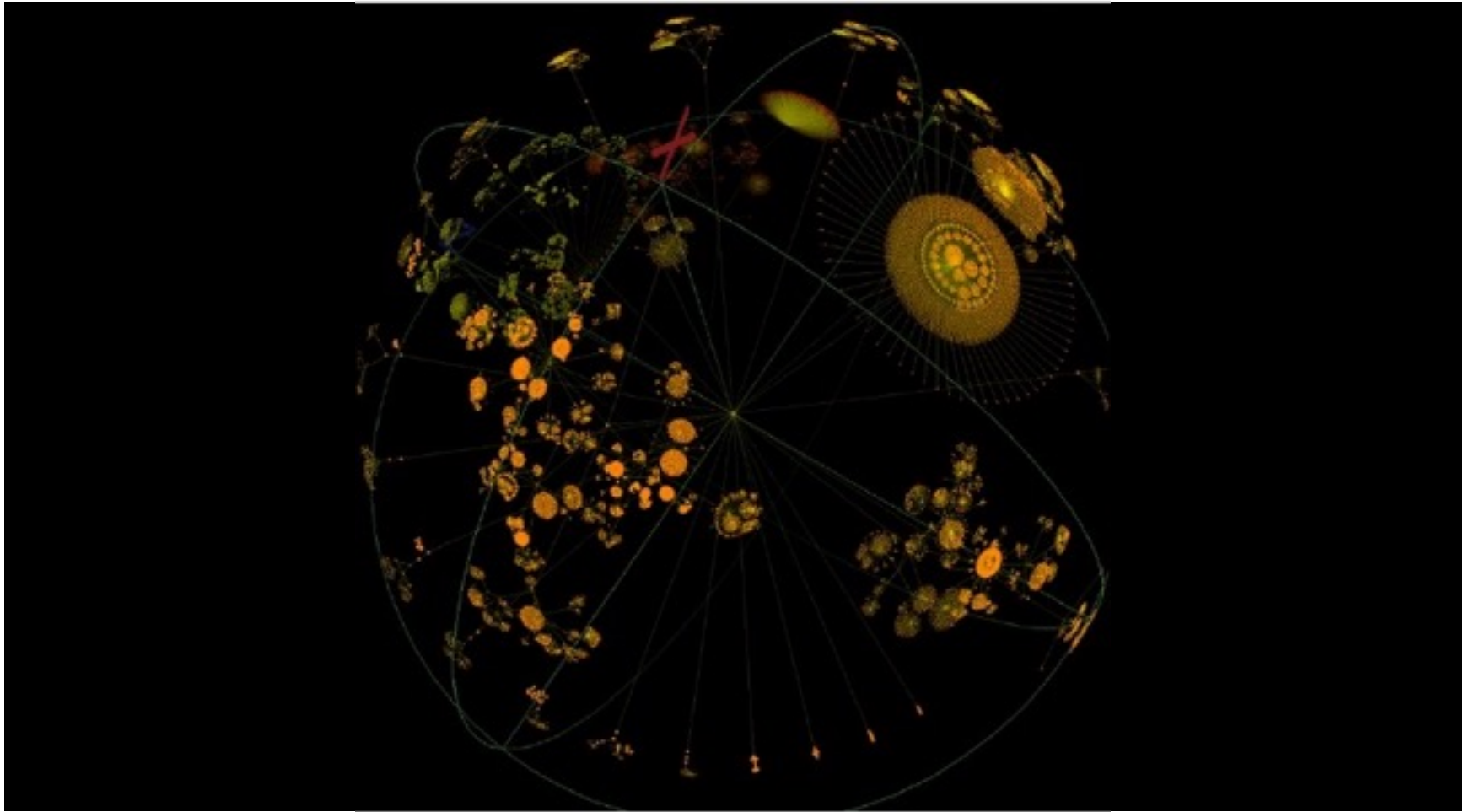


# Interactive ToL (2)



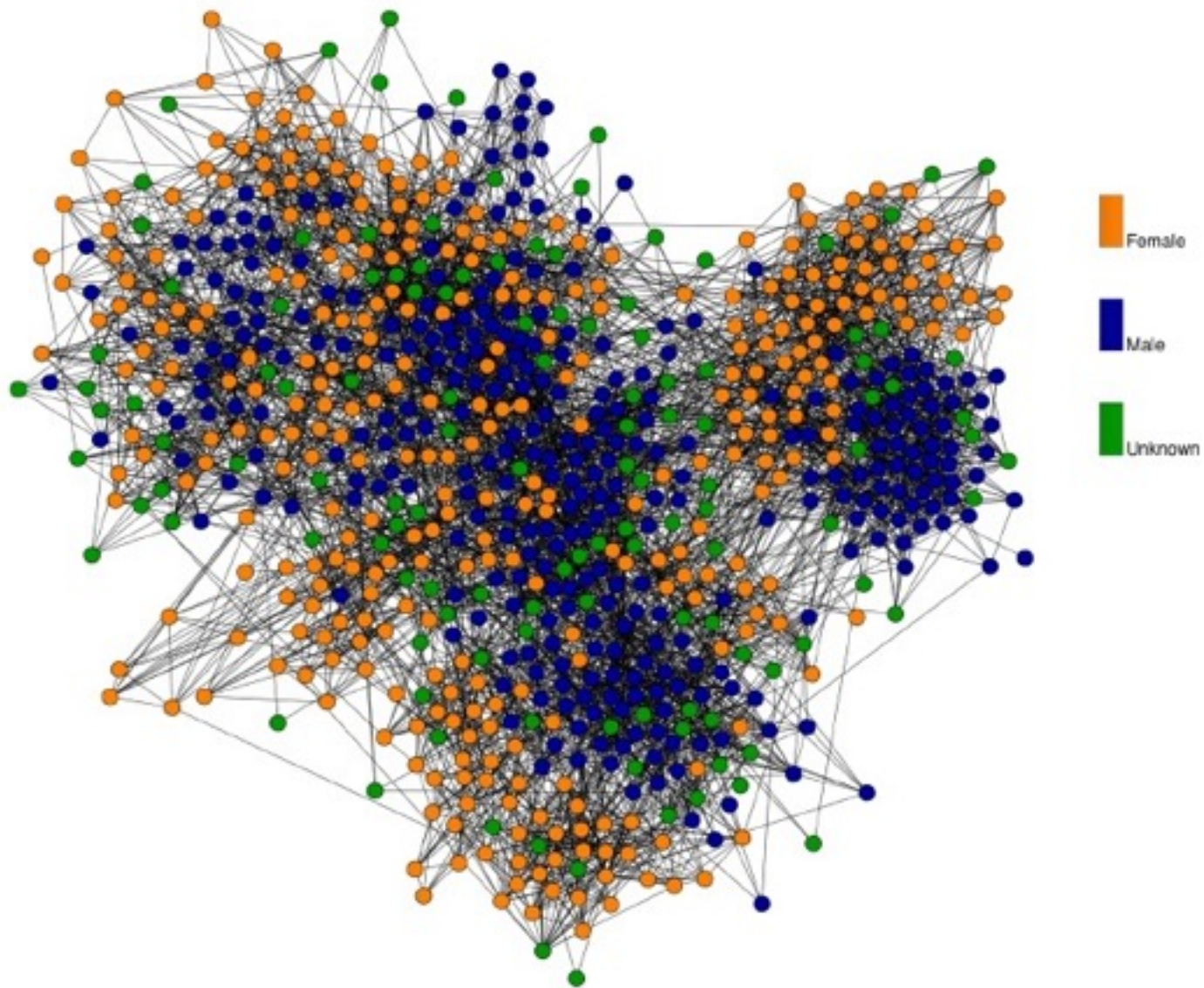
<http://www2.research.att.com/~yifanhu/TOL/>

# ToL Using Walrus



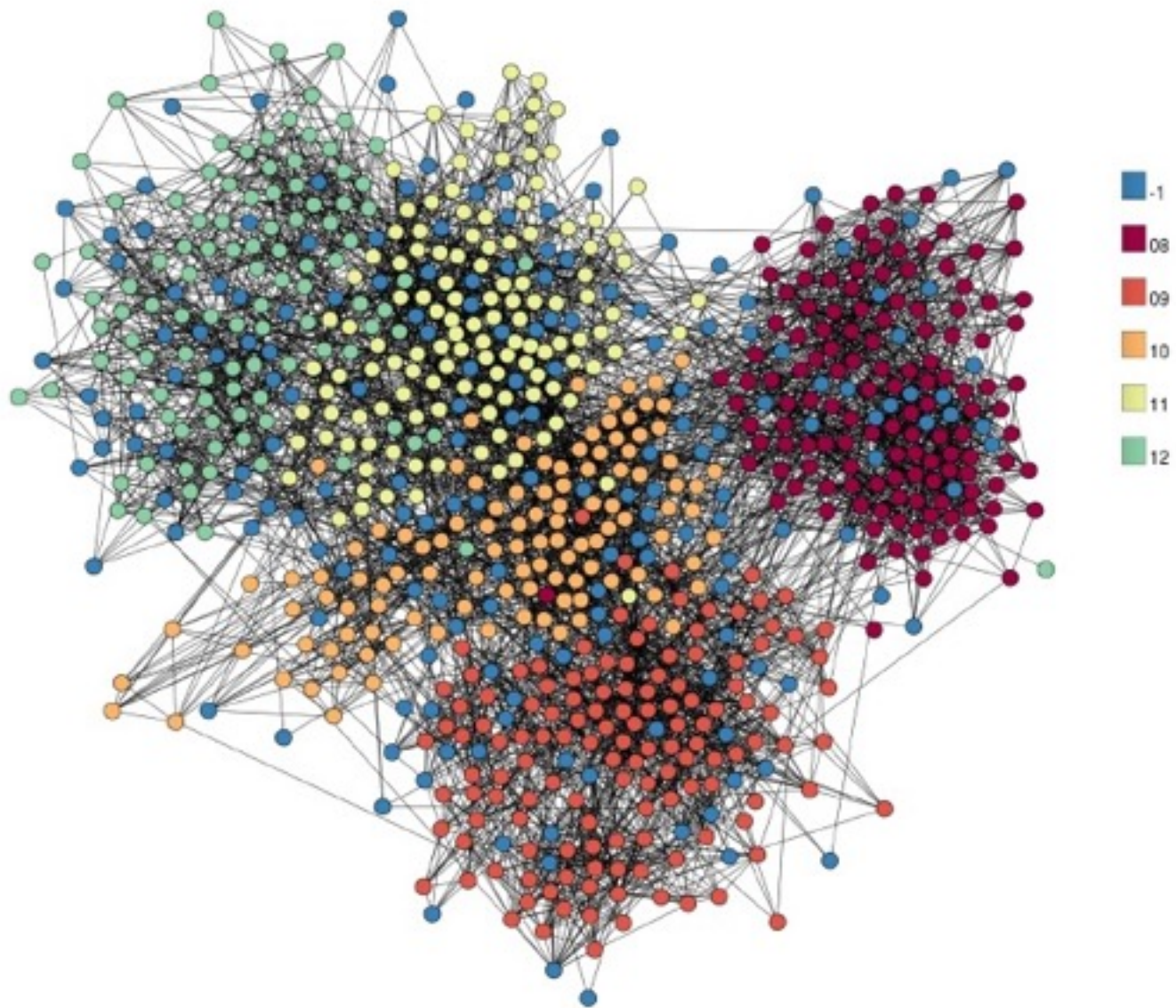
<http://digitised.info/content/view/20/51/>

# **GRAPH VISUALIZATION MOTIVATION**

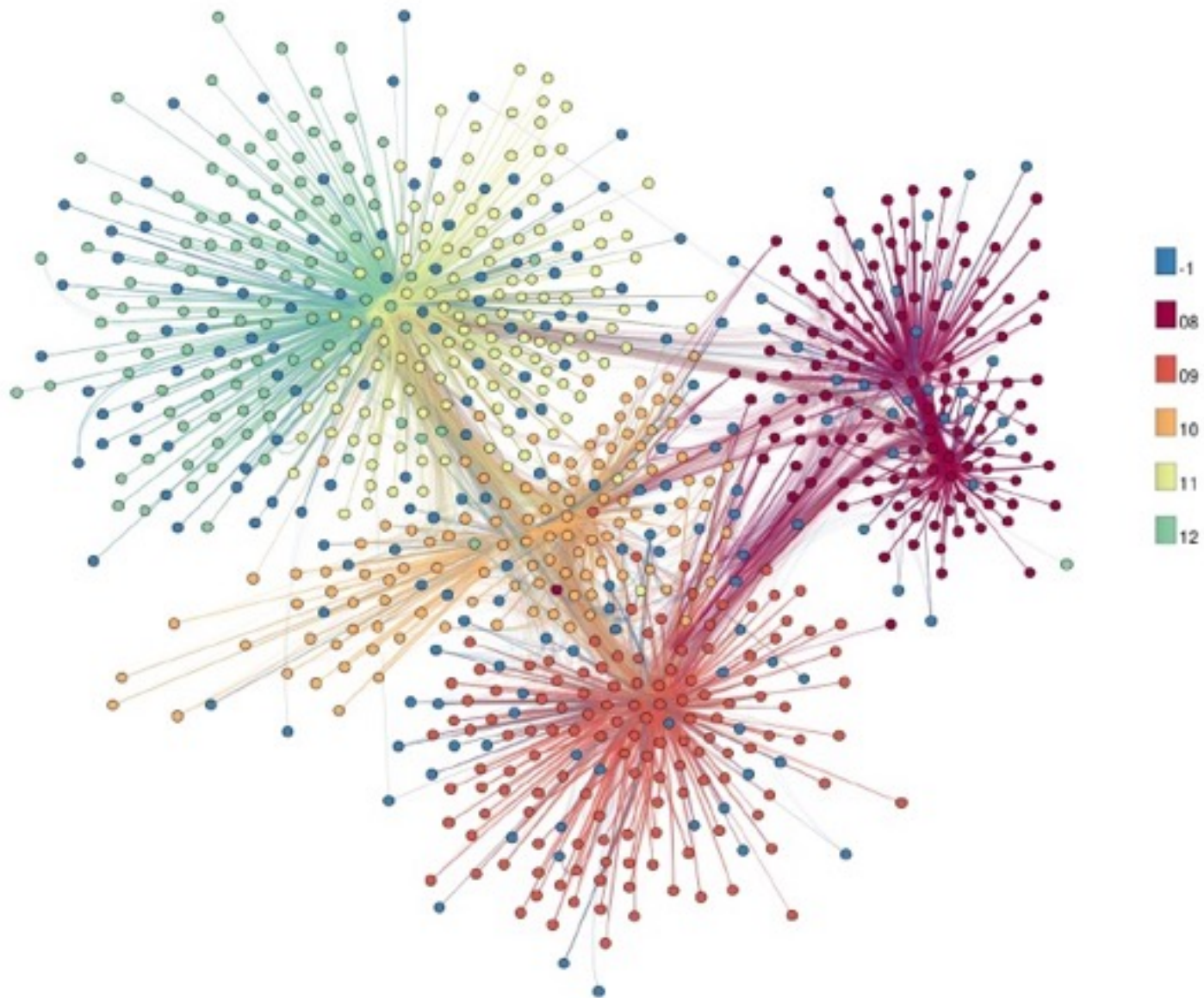


<http://vidi.cs.ucdavis.edu/projects/AggressionNetworks/>

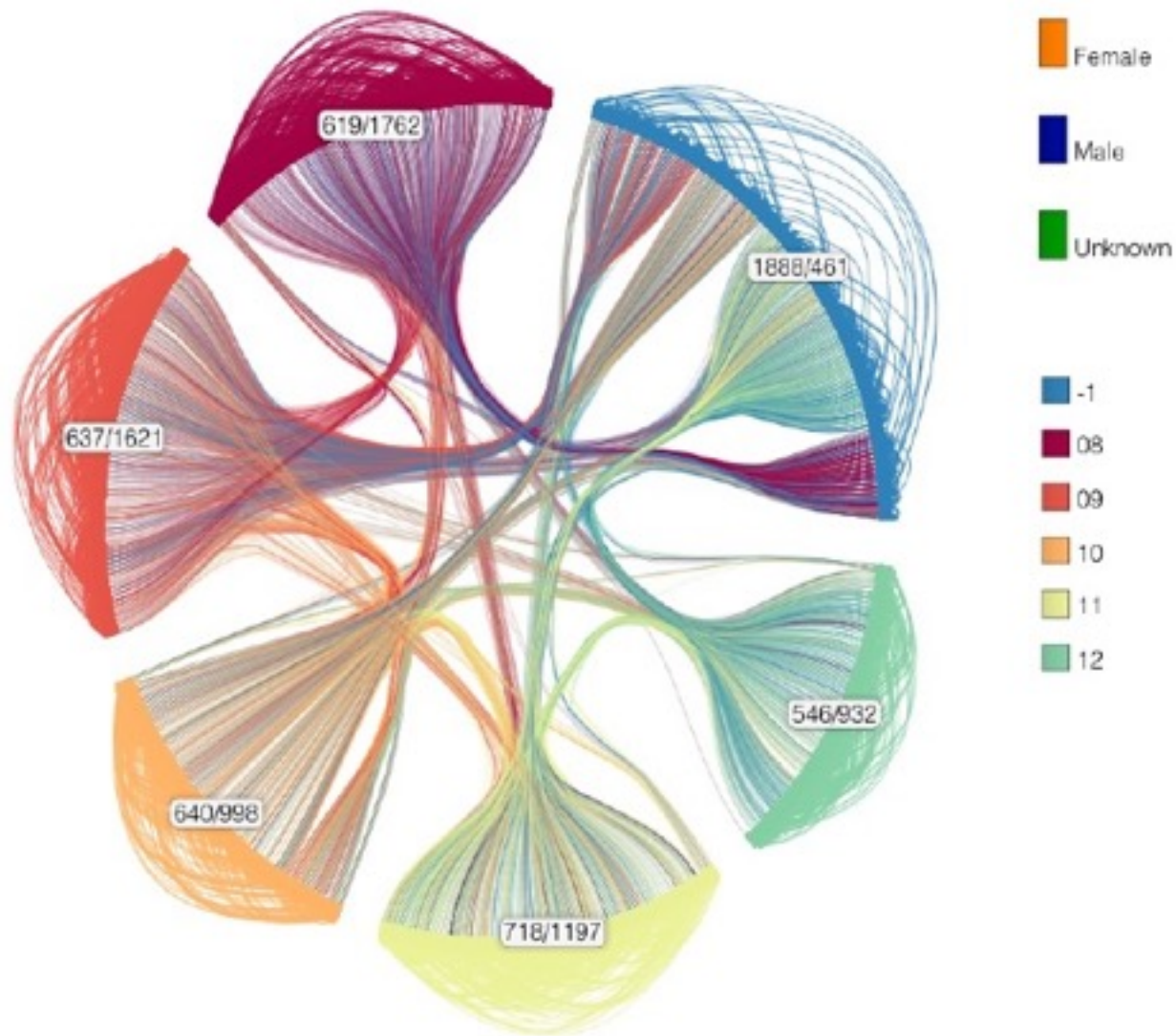




<http://vidi.cs.ucdavis.edu/projects/AggressionNetworks/>



<http://vidi.cs.ucdavis.edu/projects/AggressionNetworks/>

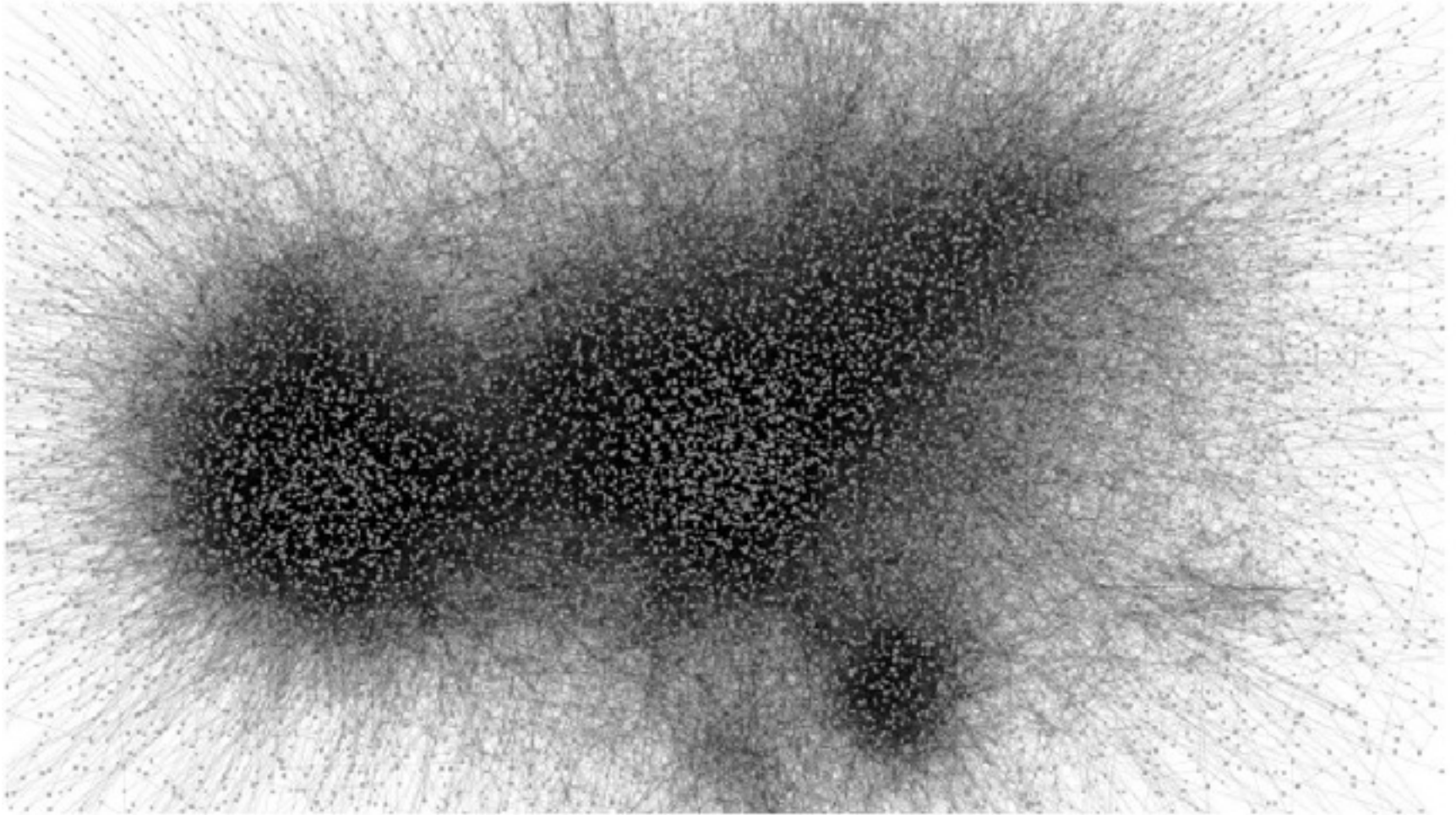


<http://vidi.cs.ucdavis.edu/projects/AggressionNetworks/>

What considerations should we make when visualizing graphs?



# Hairballs



<http://www.michelecoscia.com/?p=171>

# Hairballs



<http://www.nytimes.com/imagepages/2008/11/20/science/20mammoth.ready.html>

# Considerations

- Node Layout
  - Place randomly?
  - Place on grid?
  - Place by metric?
  - Place using physics?
- Node Attributes
  - Color?
  - Size?
  - Shape?
- Edge Layout
  - Straight edges?
  - Curved edges?
  - Edge crossings?
  - Edge bundling?
- Edge Attributes
  - Color?
  - Width?
  - Arrows?

# Considerations

- Non overlapping nodes?
- Visible labels?
- Minimize edge crossings?
- Minimize distance between nodes?
- View overall structure?
- View connections and connectivity?
- View detailed subgraphs?



# MATRIX DIAGRAMS

# Matrix Diagrams

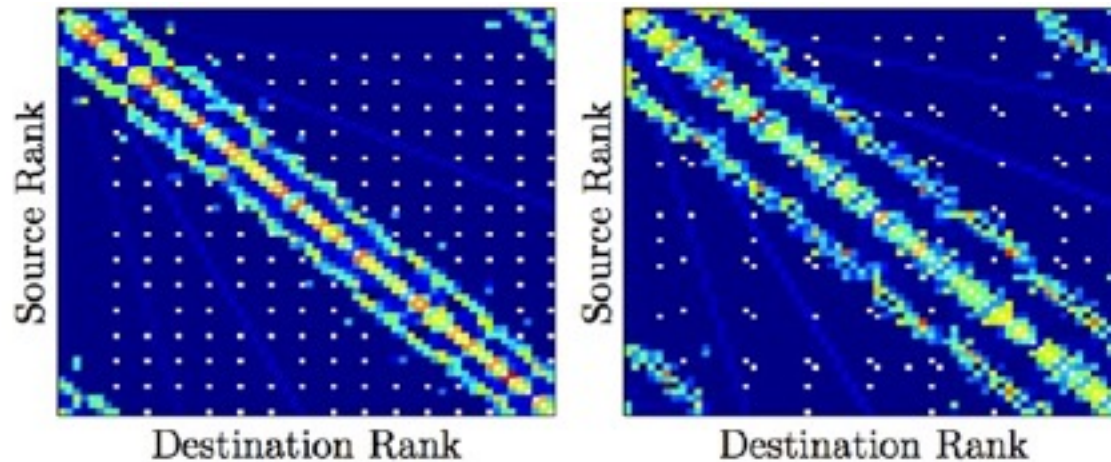
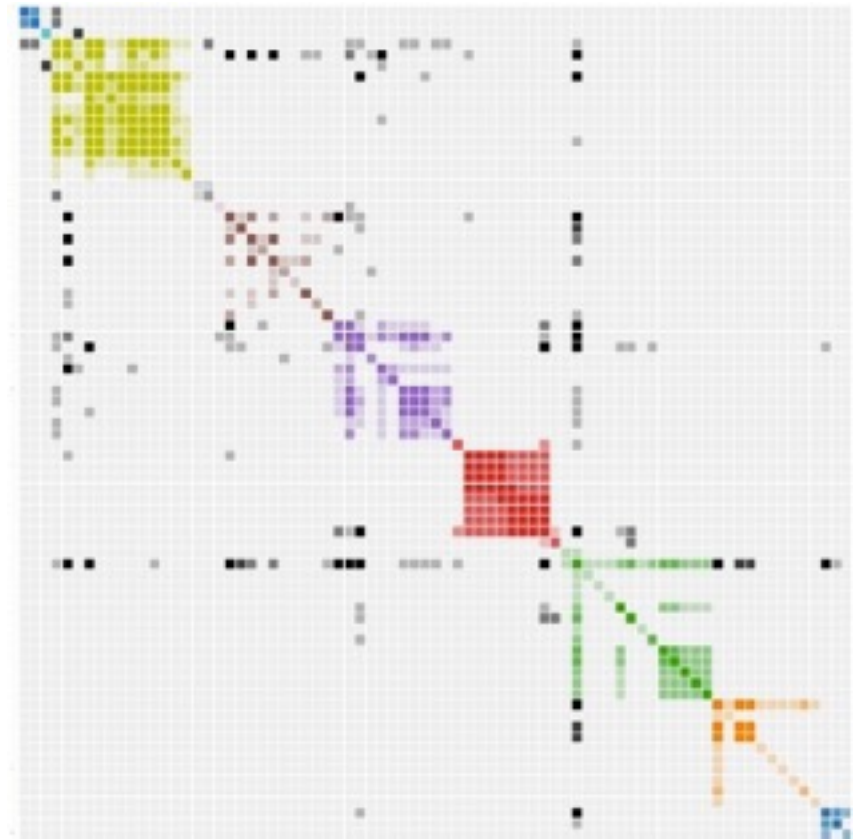


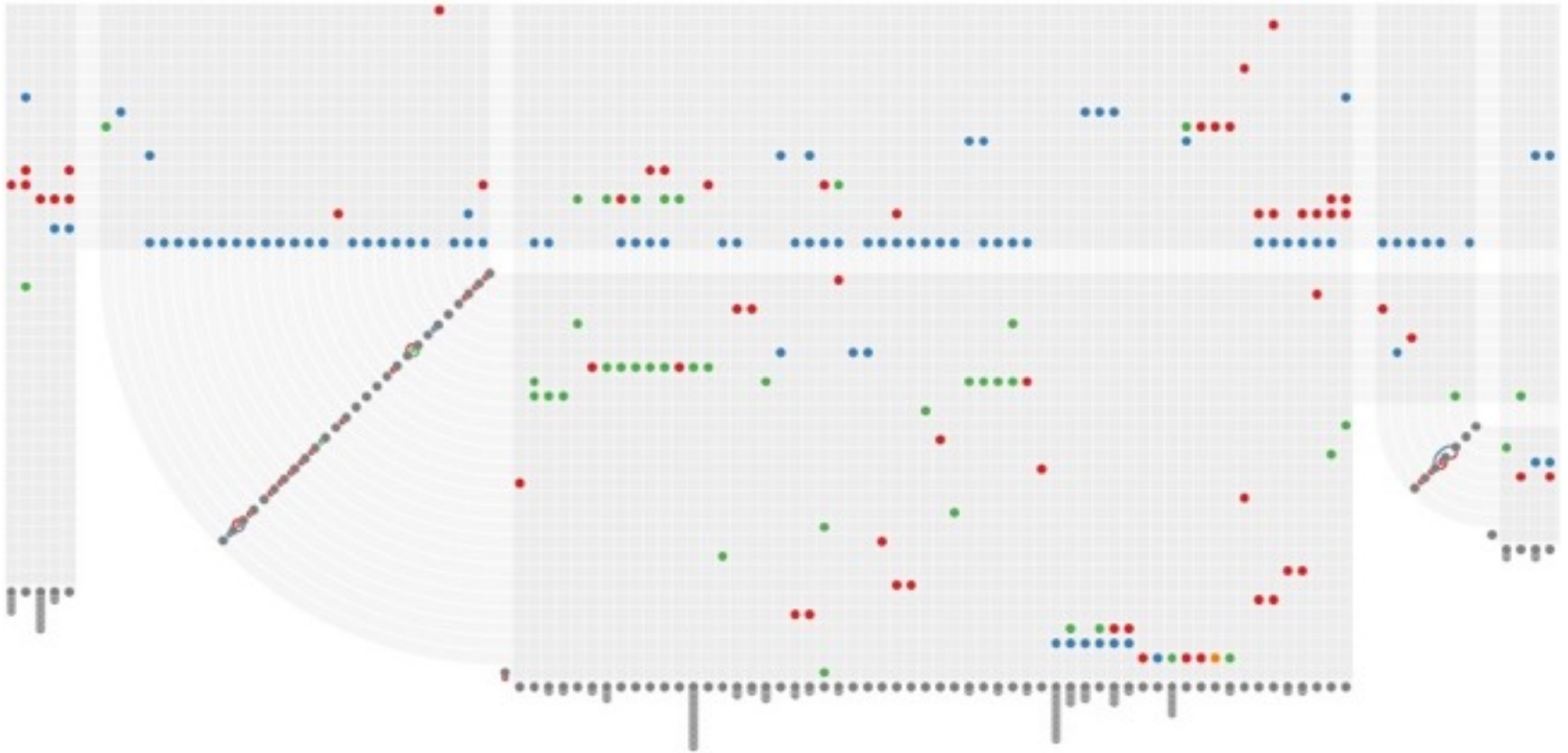
Figure 3: Data dependent topology demonstrated by molecular dynamics simulator NAMD under different molecular arrangements. The number of bytes sent between ranks is linearly mapped from dark blue (lowest) to red (highest), with white indicating an absence of communication.

# Les Misérables Co-Occurrence



<http://bost.ocks.org/mike/miserables/>

# Compressed Adjacency Matrix



<http://www.computer.org/csdl/trans/tg/2012/12/ttg2012122457-abs.html>

# **NODE LAYOUT**

# Common Graph Layouts

- Arc Diagrams
- Circle Layout
- Spring and Force-Directed Layouts
- Self-Organizing Map Layout
- Fruchterman Reingold Layout
- Kamada Kawai Layout
- Hive Plots
- Multi-Level Layouts



# Arc Diagram



<http://www.turbulence.org/Works/song/method/method.html>

# Arc Diagram

THE SHAPE OF SONG

[What the diagrams mean](#) | [Image gallery](#) | [Home](#) | [Contact](#)

Repertoire (640 pieces)

Composer	Title
Alfred Nobe	Canzò
Astor	Moments in ...
	Adagio
	For Tebe
Lace	For Tebe
	Lace lips
Bach	✓ A Musical Of...
	A Musical Of...
Bach, J.S.	✓ Brandenburg ...
	Inw542
	Inw543
	Inw544
	Inw545
	Colap minor ...
	Fugue, D Minor
	Goldberg Vari...
	Goldberg Vari...
	Goldberg Vari...
Invention 15	
Bach, J.S.	Jesus Joy of M...
	Passacaglia ...
Bachman	I Want to That ...
Bachman	Calling You
Bachman	Informal
Bachman	s
Bachman	c
Bachman	c
Bachman	entre go
Bachman	Just a Toy
Bachman	just a Toy
Bachman	pan's concert...

Brandenburg Concerto 2. Back. Viewing track 1 of 9.

1 2 3 4 5 6 7 8 9

Play (all tracks)

You can add any MIDI file on the web to the repertoire.

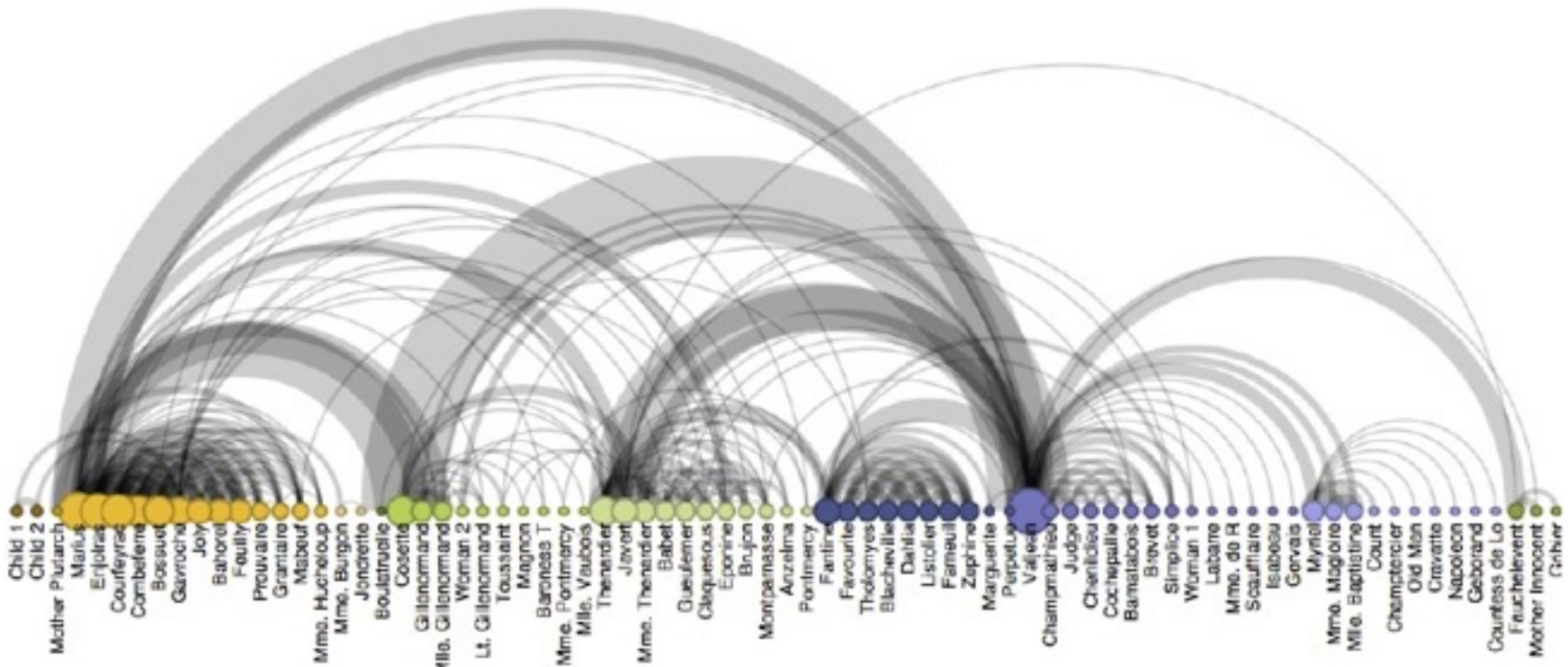
URL

Title  Composer

Enter the URL of a MIDI file and the title of the piece. Composer is optional but nice.

<http://www.turbulence.org/Works/song/mono.html>

# Arc Diagram in Protovis



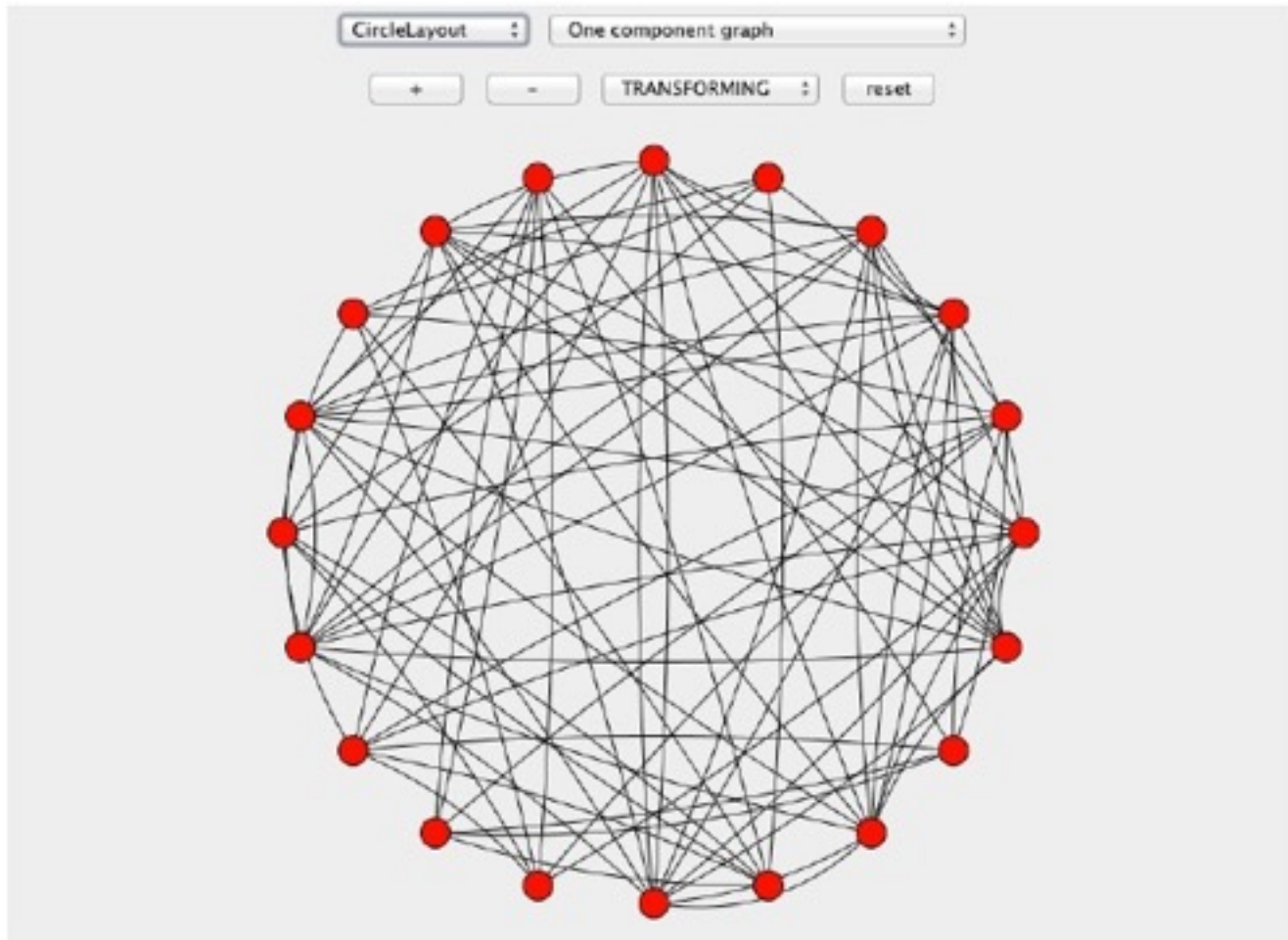
<http://mbostock.github.io/protovis/ex/arc.html>

# Similar Diversity



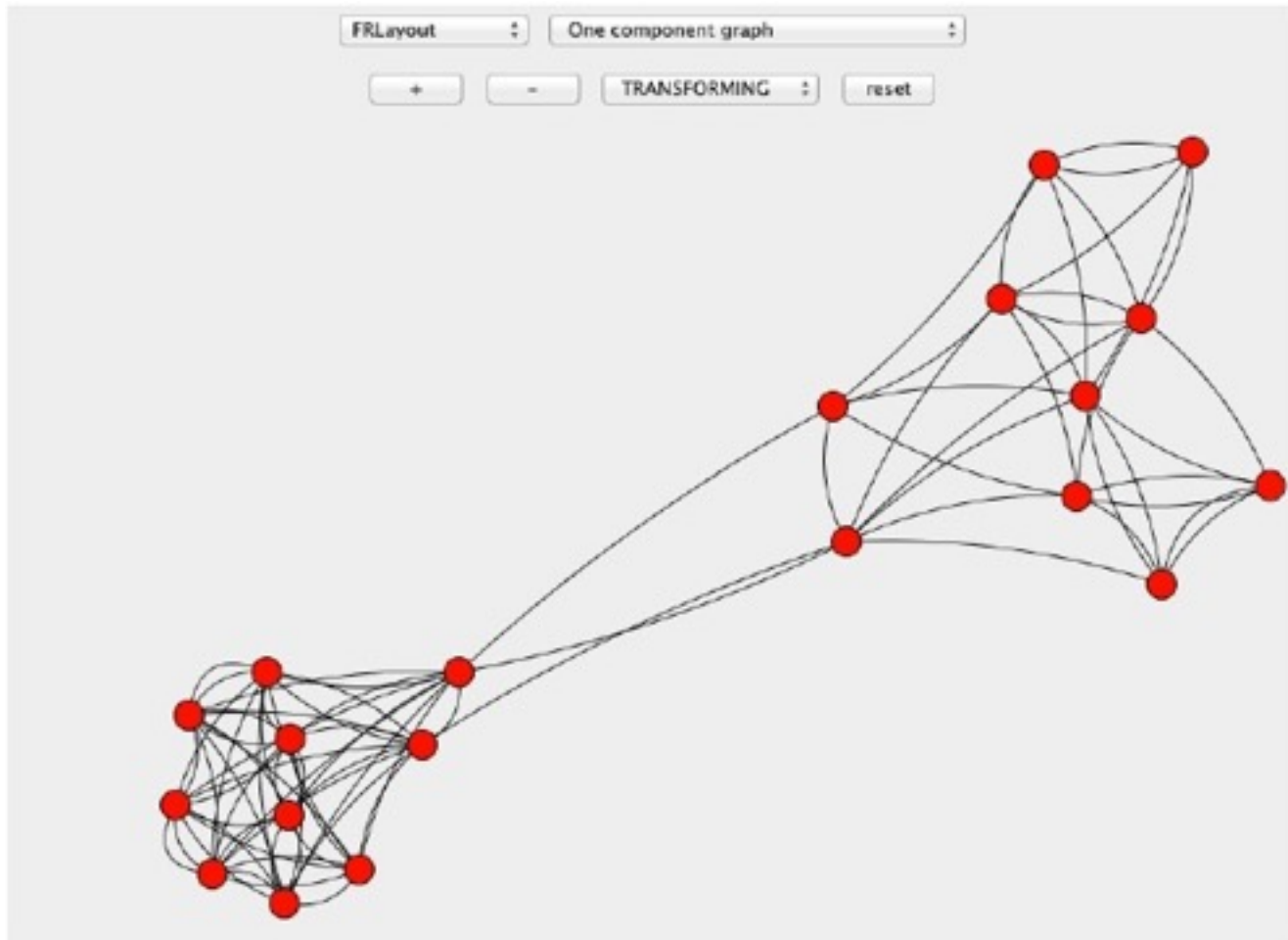
<http://similaritydiversity.net/about/>

# JUNG Layouts



<http://jung.sourceforge.net/applet/showlayouts2.html>

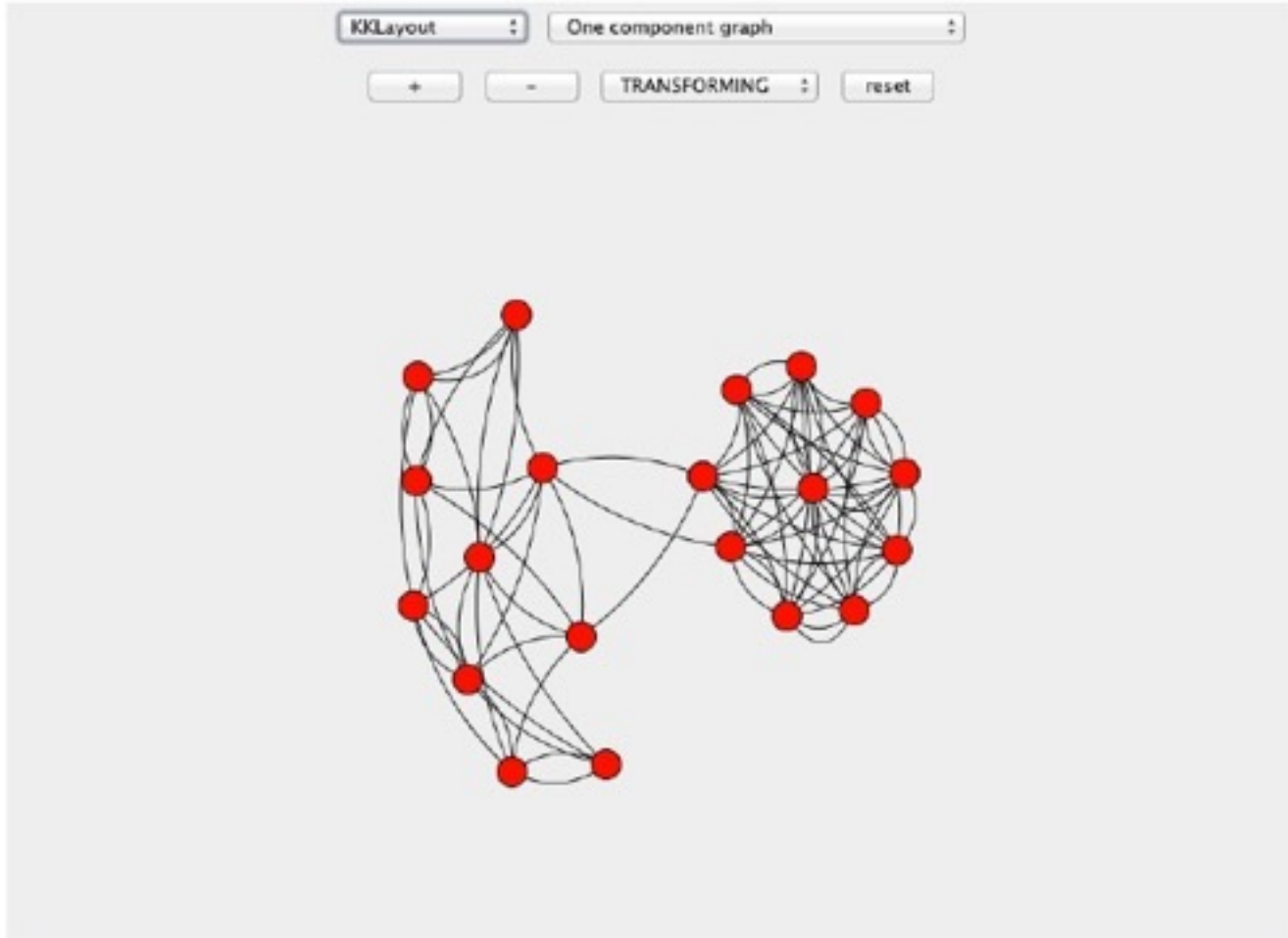
# JUNG Layouts



<http://jung.sourceforge.net/applet/showlayouts2.html>

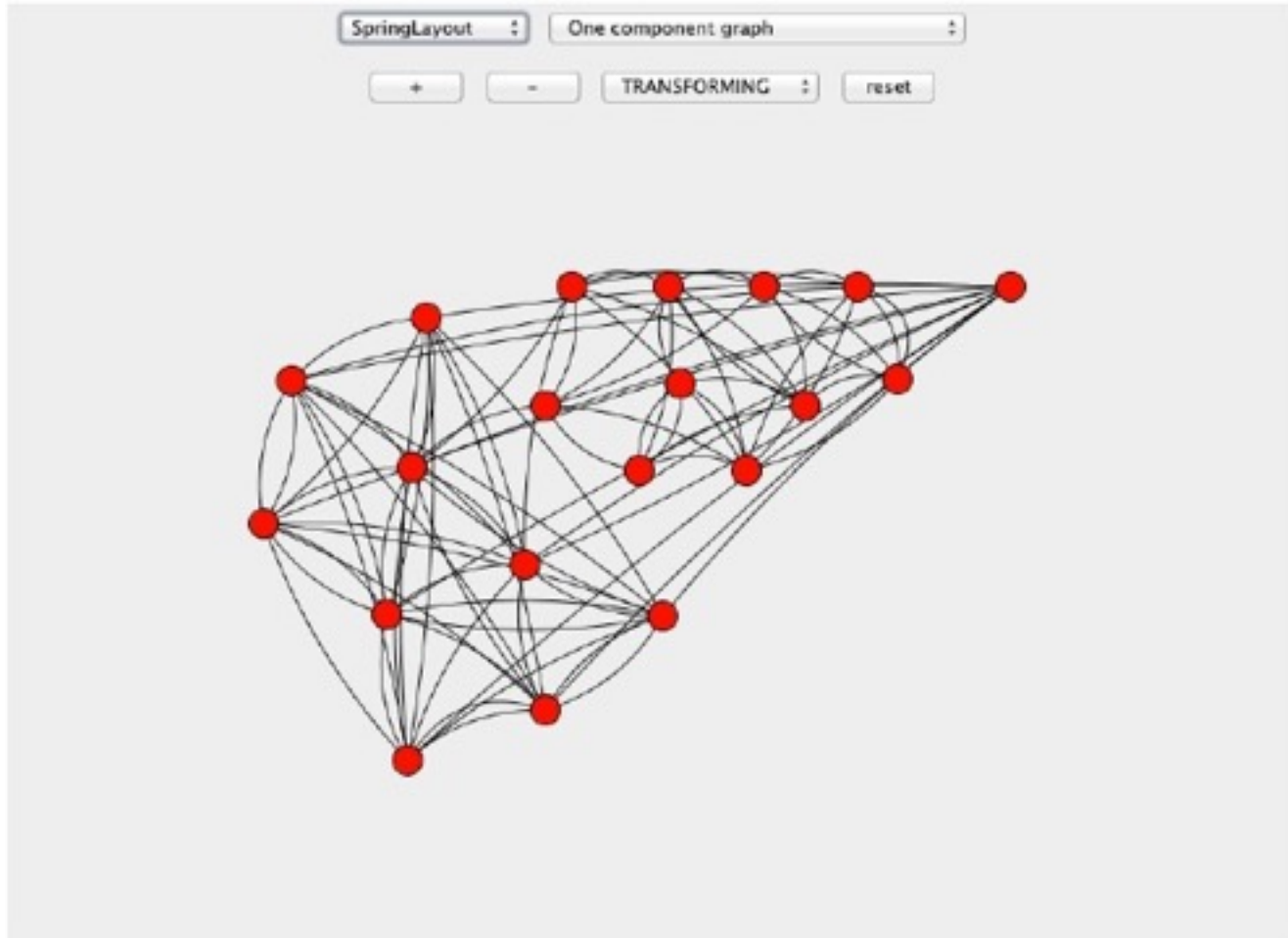


# JUNG Layouts



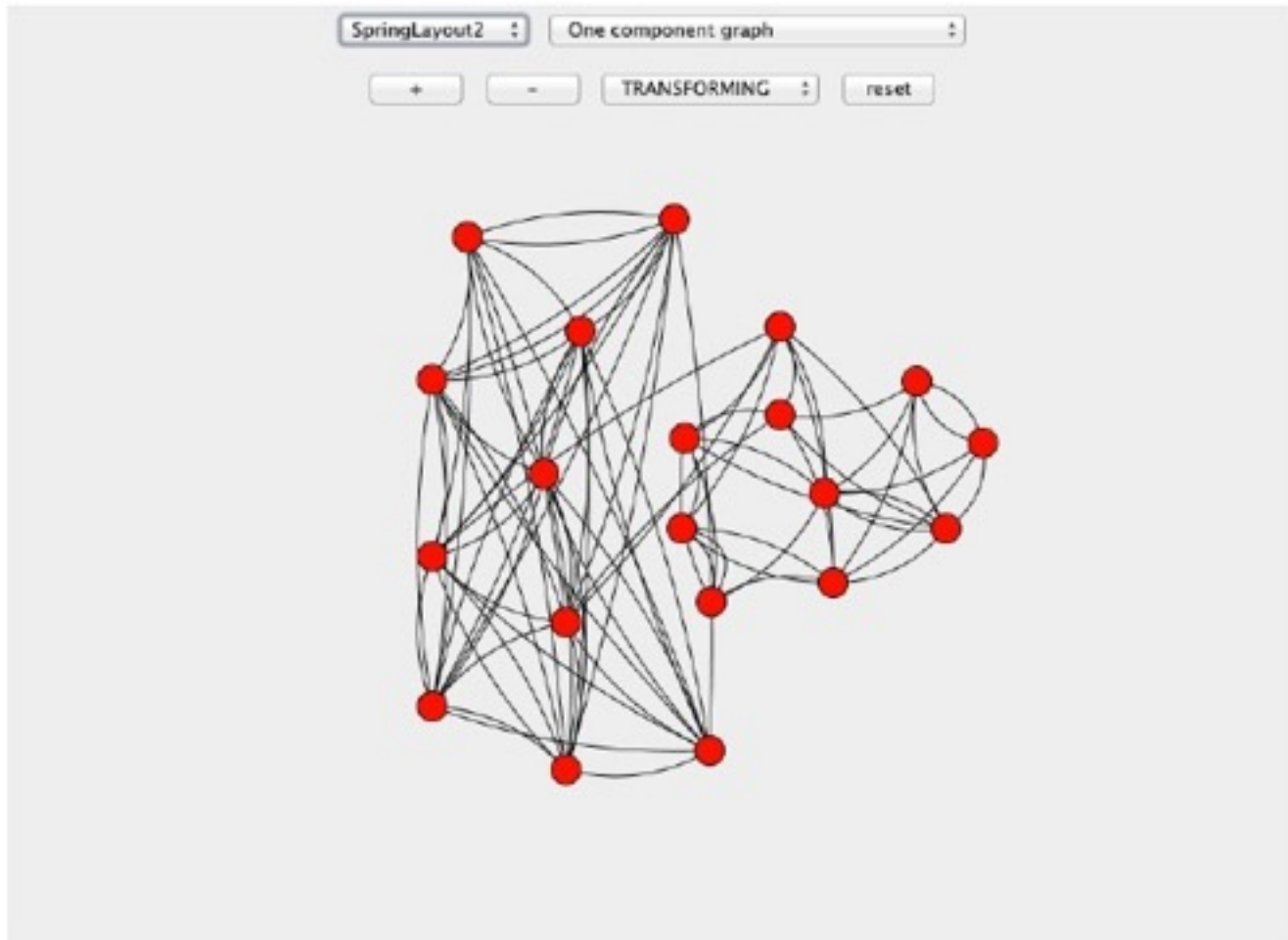
<http://jung.sourceforge.net/applet/showlayouts2.html>

# JUNG Layouts



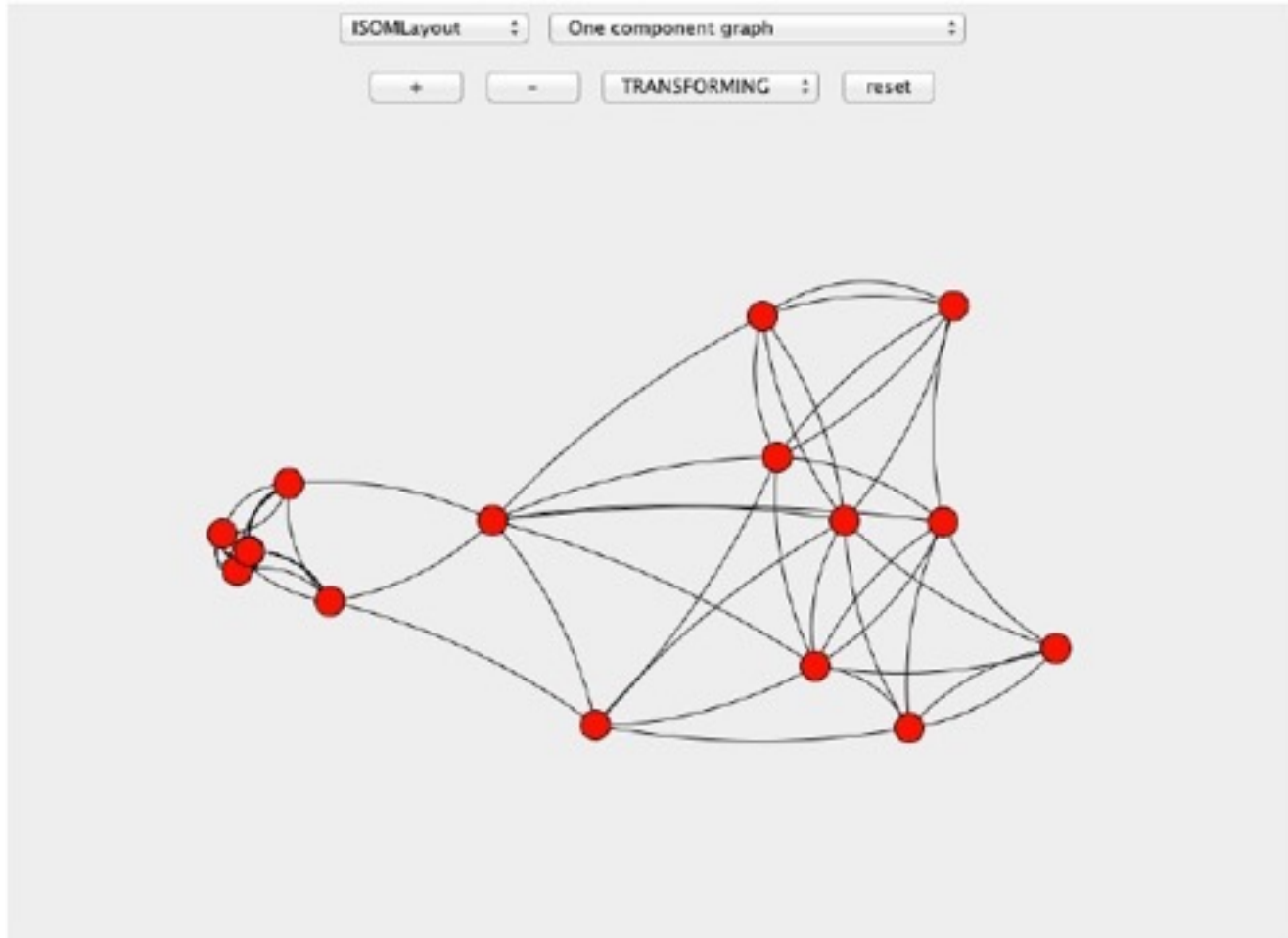
<http://jung.sourceforge.net/applet/showlayouts2.html>

# JUNG Layouts



<http://jung.sourceforge.net/applet/showlayouts2.html>

# JUNG Layouts



<http://jung.sourceforge.net/applet/showlayouts2.html>

# aNETmation

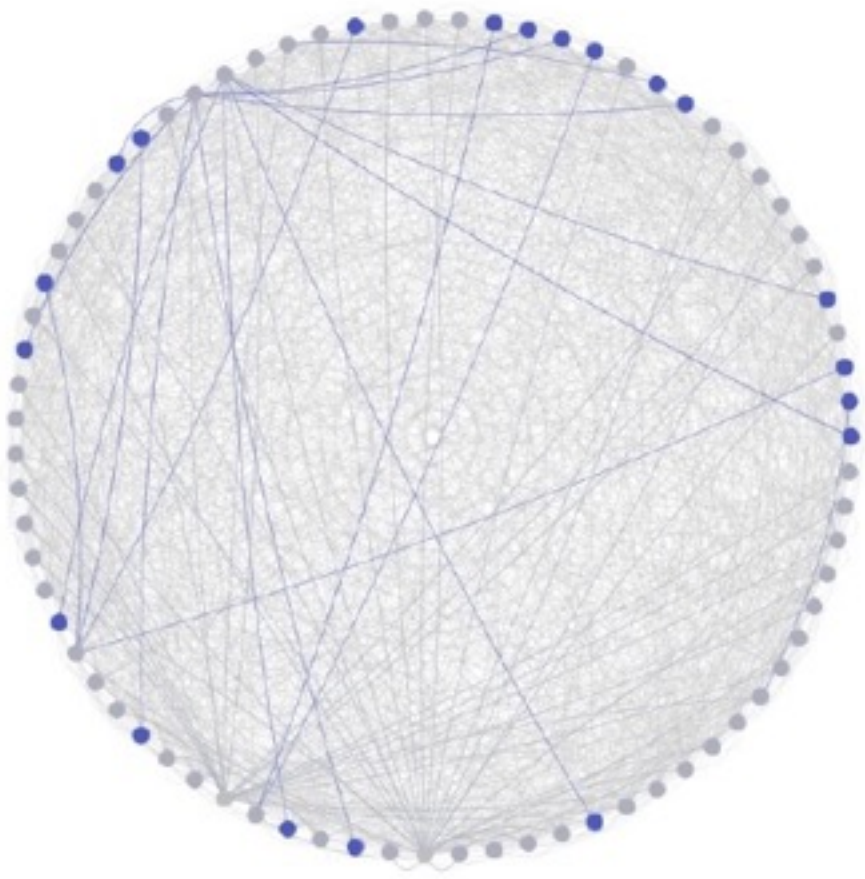
Random Network Generator:

Parameters:  
Iterations:   
Number of Nodes:   
Number of Edges:   
Edge Attach Rate:   
Connection Pr:

Graph Layout:

aNETmation Visualization:

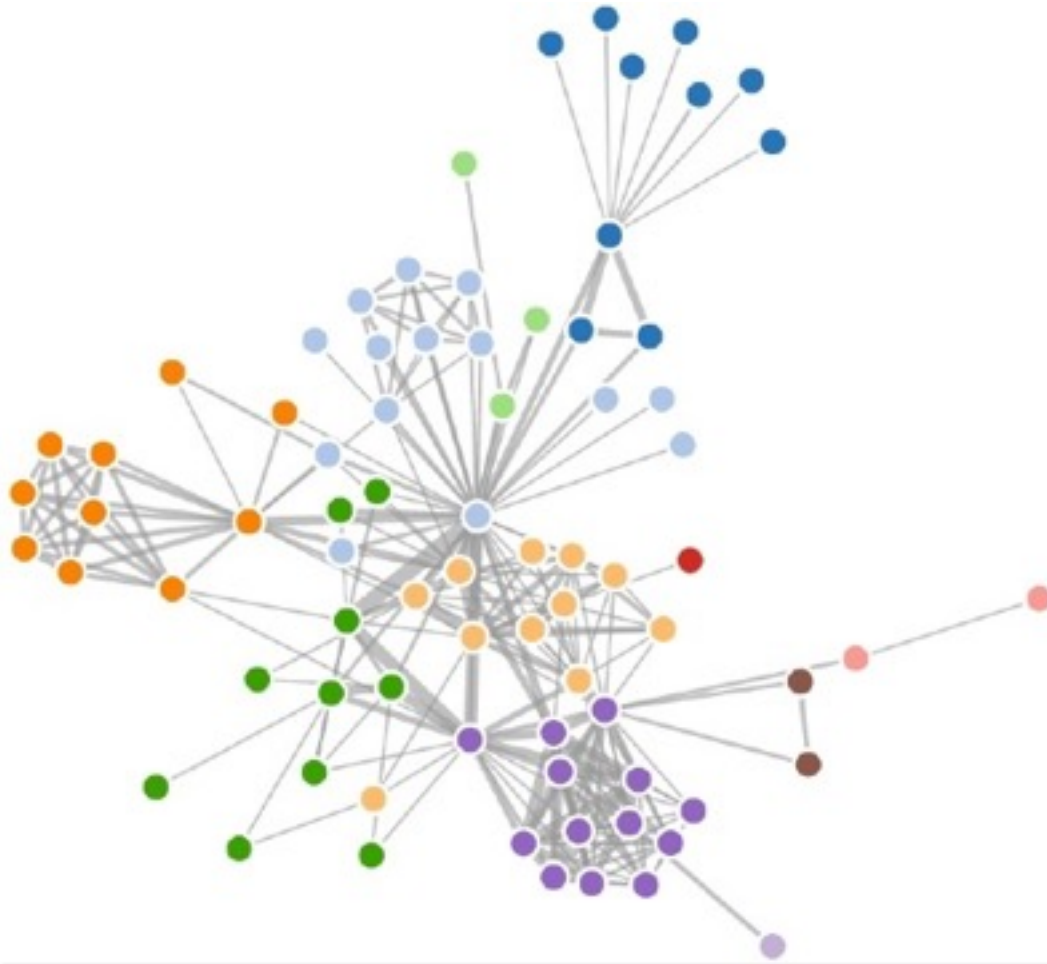
Parameters:  
Number of Seeds:



Stopping Random Spider visualization. Click "Start Visualization" to restart.

<http://www.phien.org/ucdavis/grad/projects/anetmation/>

# Force Directed Layout in D3



<http://bl.ocks.org/mbostock/4062045>



# HIVE PLOTS

# Hive Plots

- What are hive plots?
  - Network layout algorithm using per-node network properties for no displacement
  - A radially-arranged parallel coordinate plot
- Why use hive plots?
  - Repeatable, comparable network layouts
  - Shows network properties with topology

# Motivation

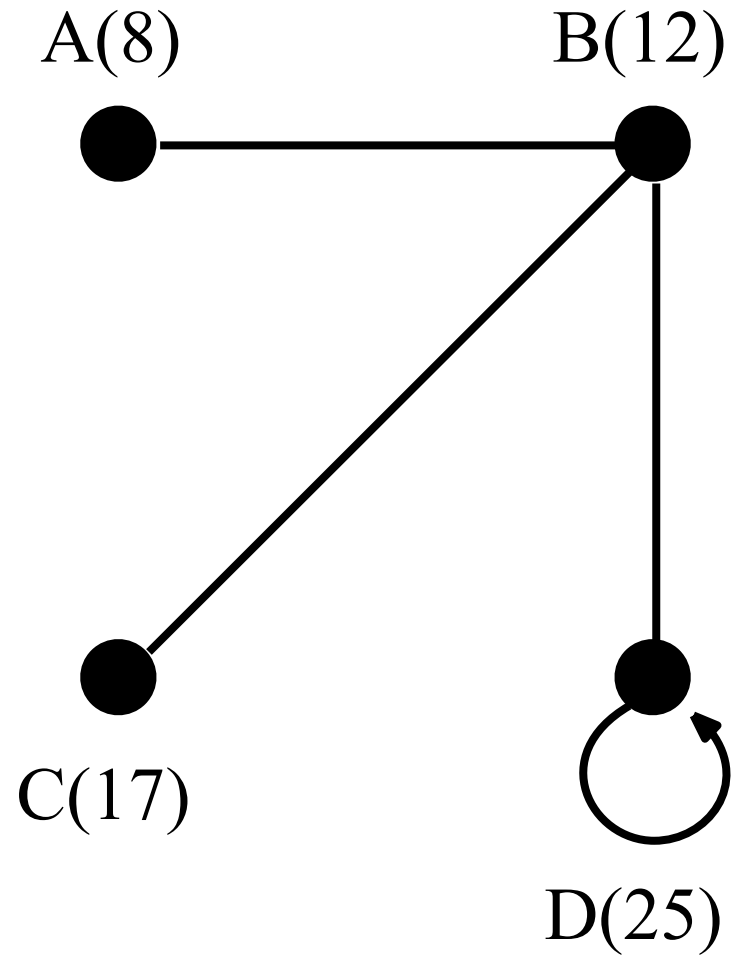


Subset of the human protein-protein interaction network rendered by Cytoscape. Each visualization uses the same layout (spring embedded), using the previous as a starting point.

Rual et al., *Nature* **437**(7062):1173-8.

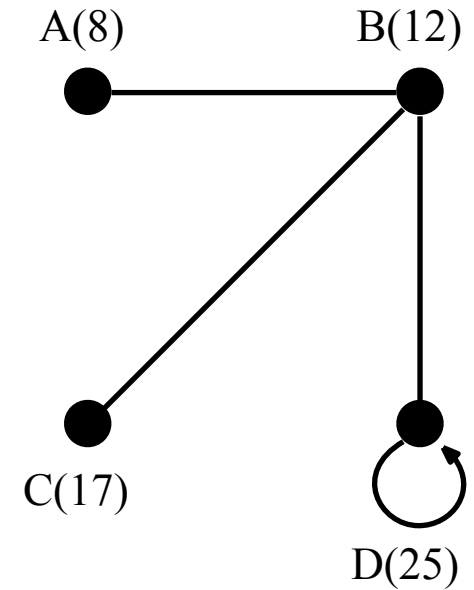
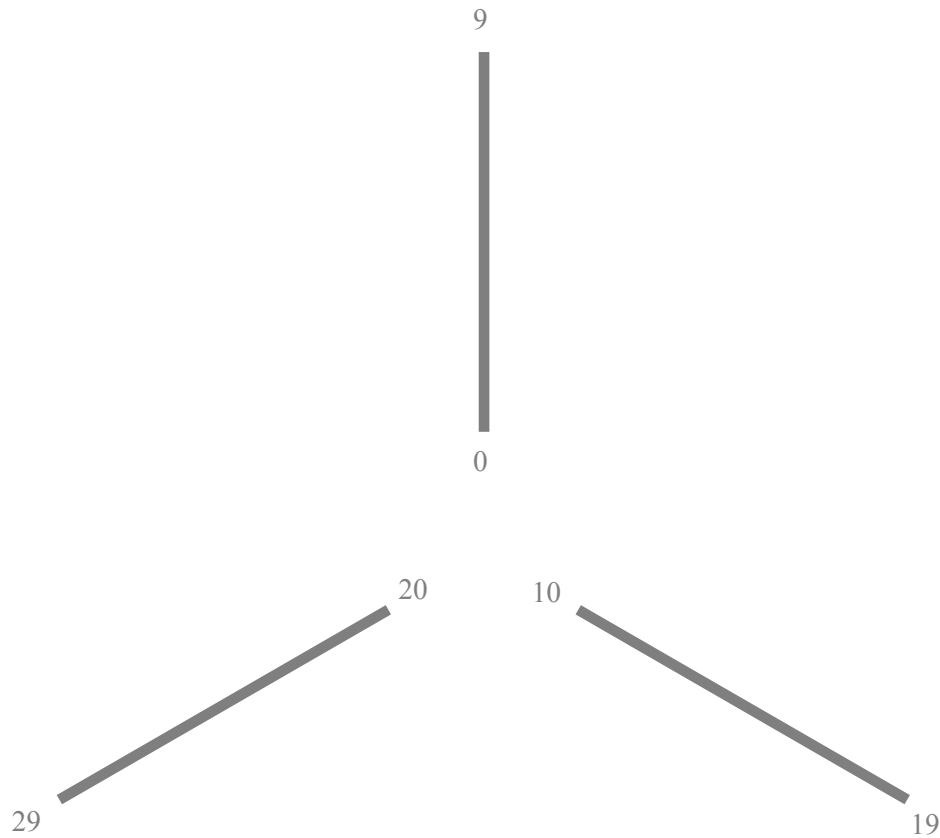
<http://www.hiveplot.net/talks/hive-plot.pdf>

# Initial Network



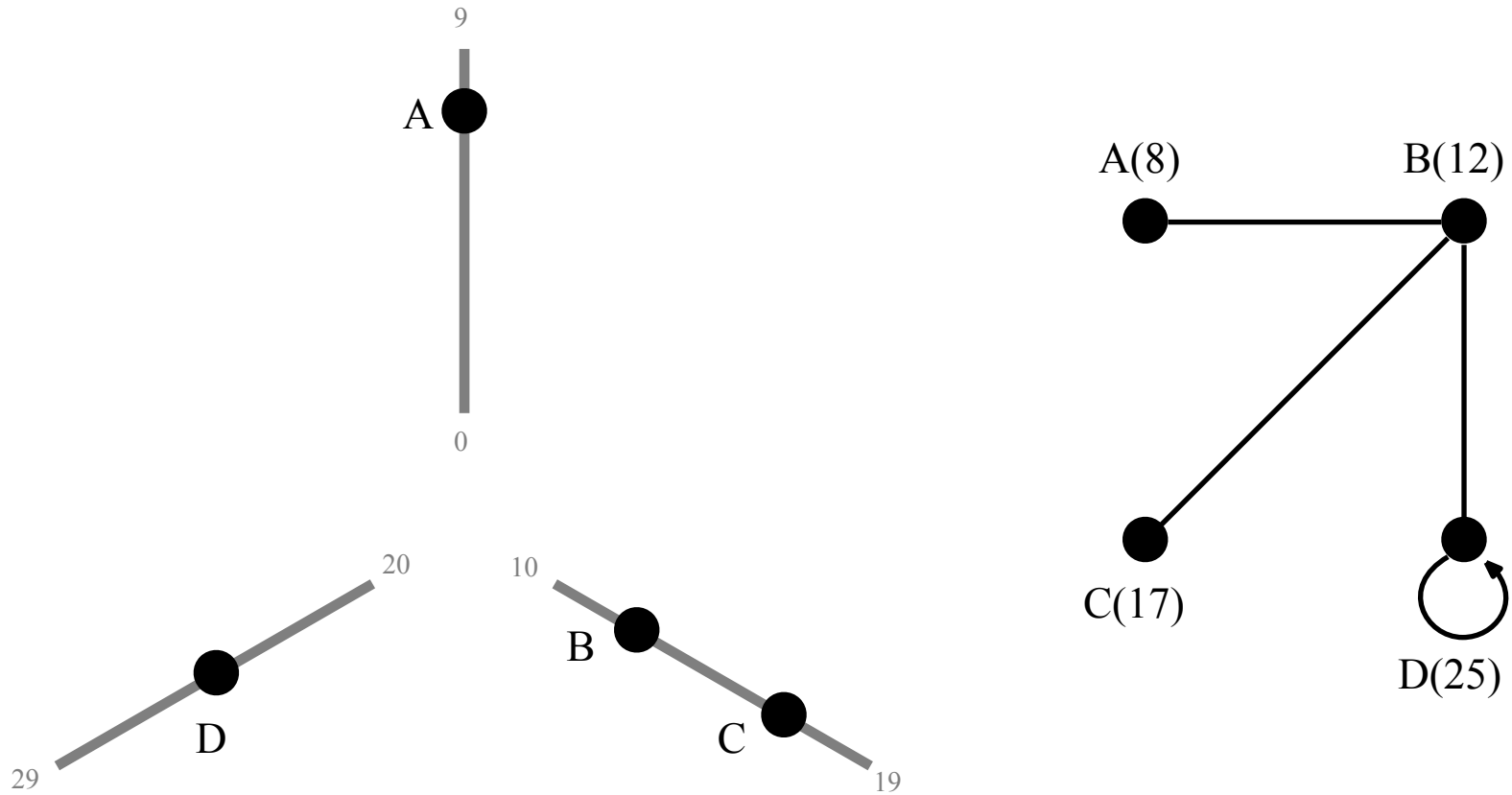
Simple network with node weights and a self-loop.

# Axis Layout



Three axis bars guarantee no edge crossings across axes. Divide node weight range between axes.

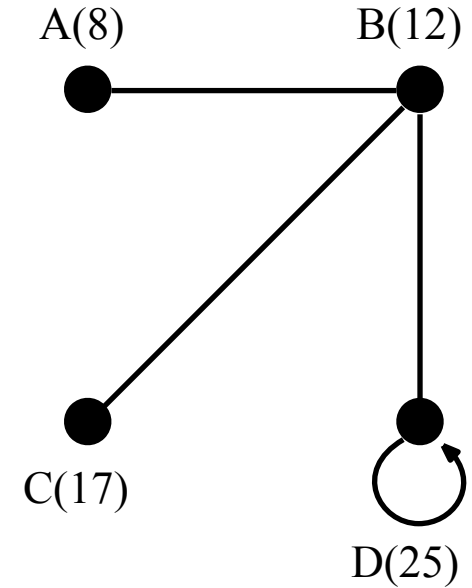
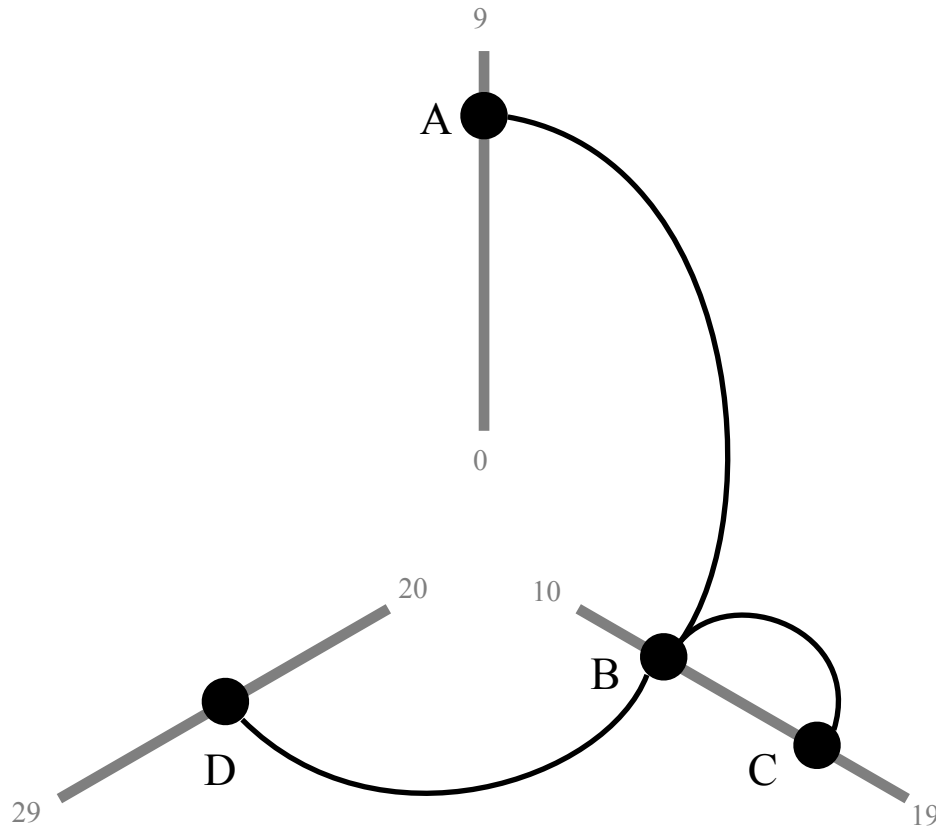
# Node Layout



Place nodes on axis lines according to weight.

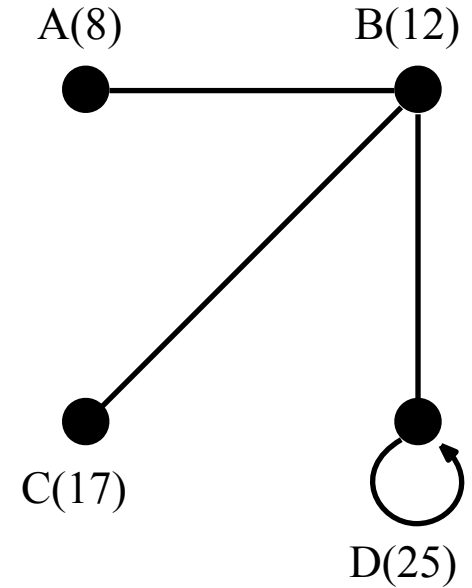
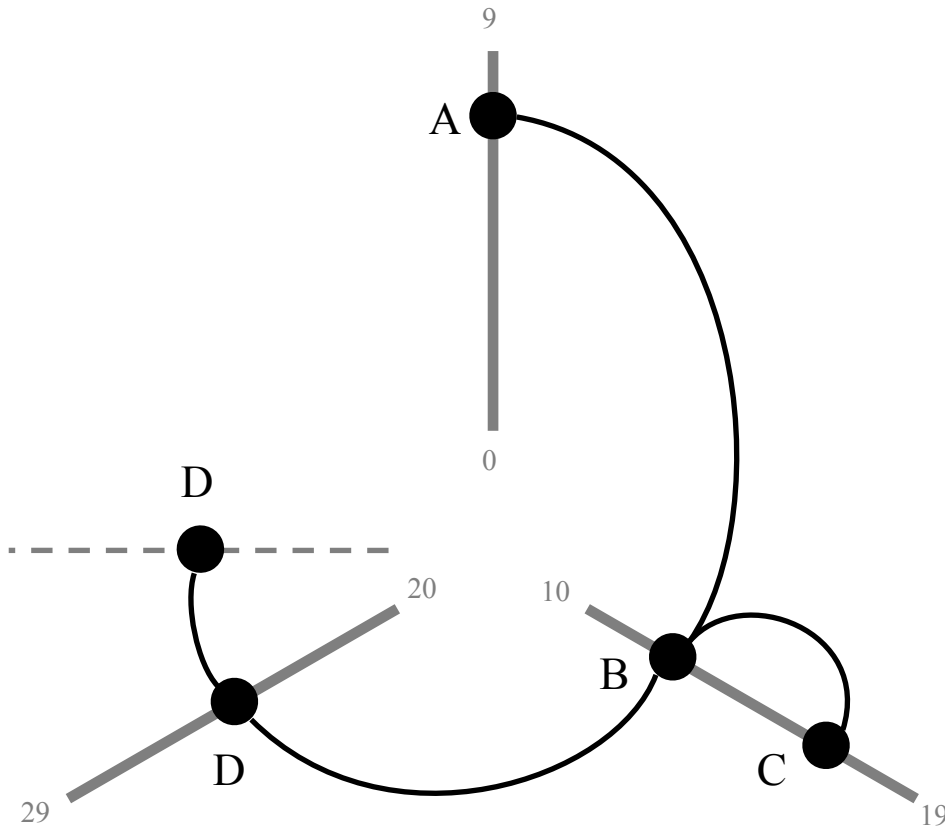


# Edge Layout



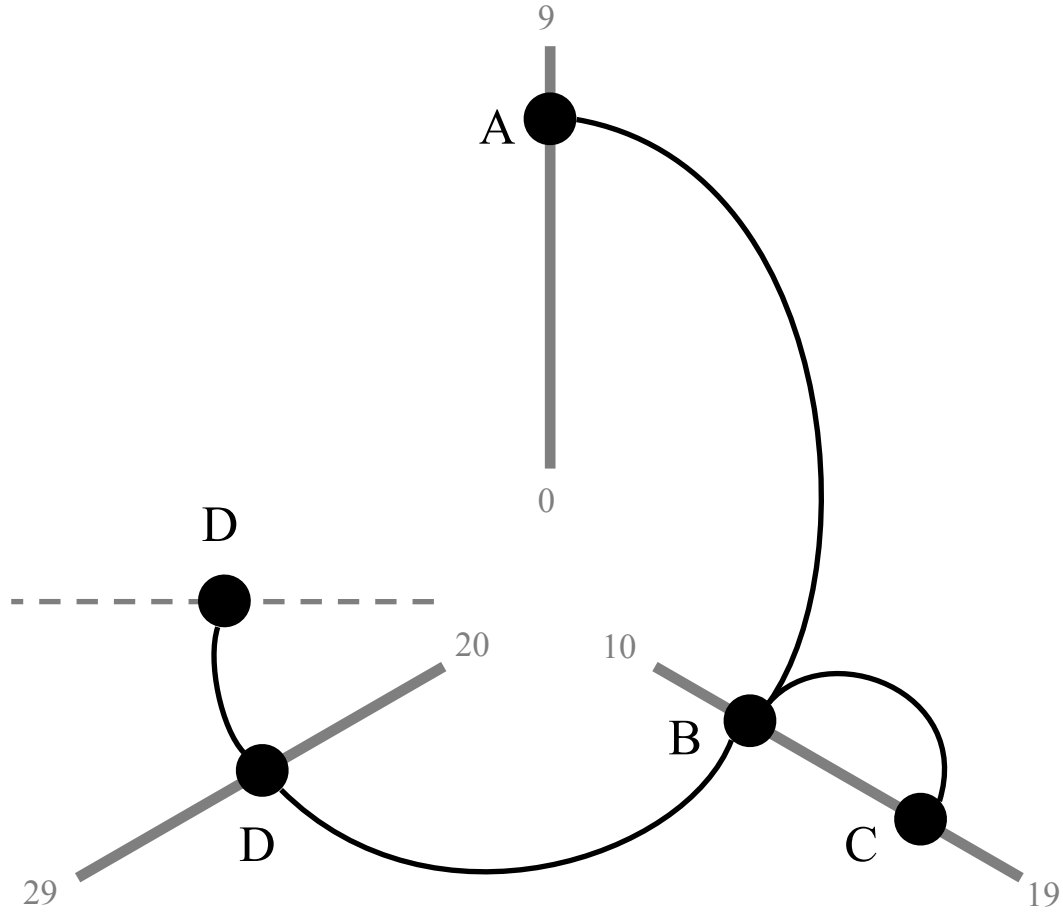
Connect nodes together accordingly.

# Self Loops

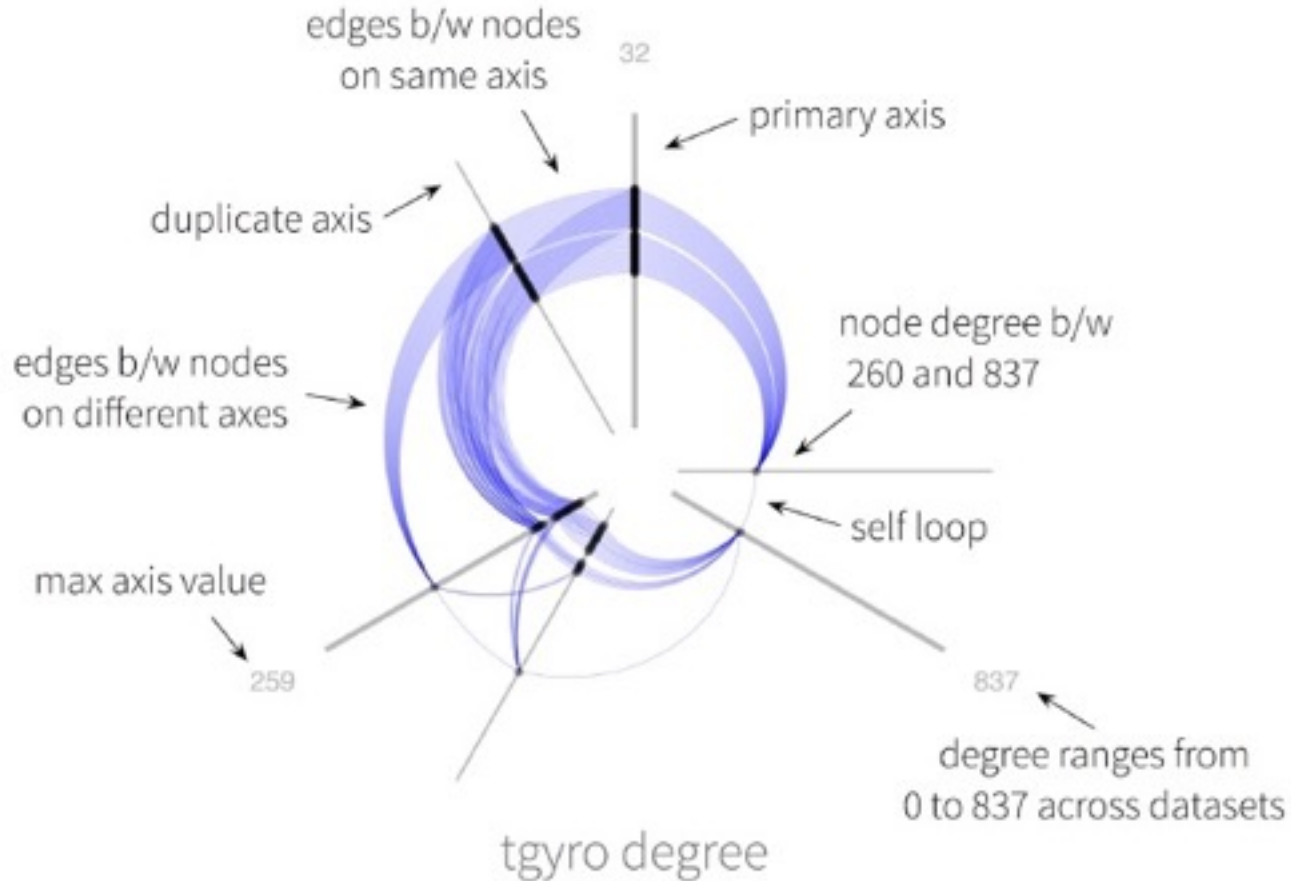


Clone axis lines to show self-loops in network.

# Final Layout

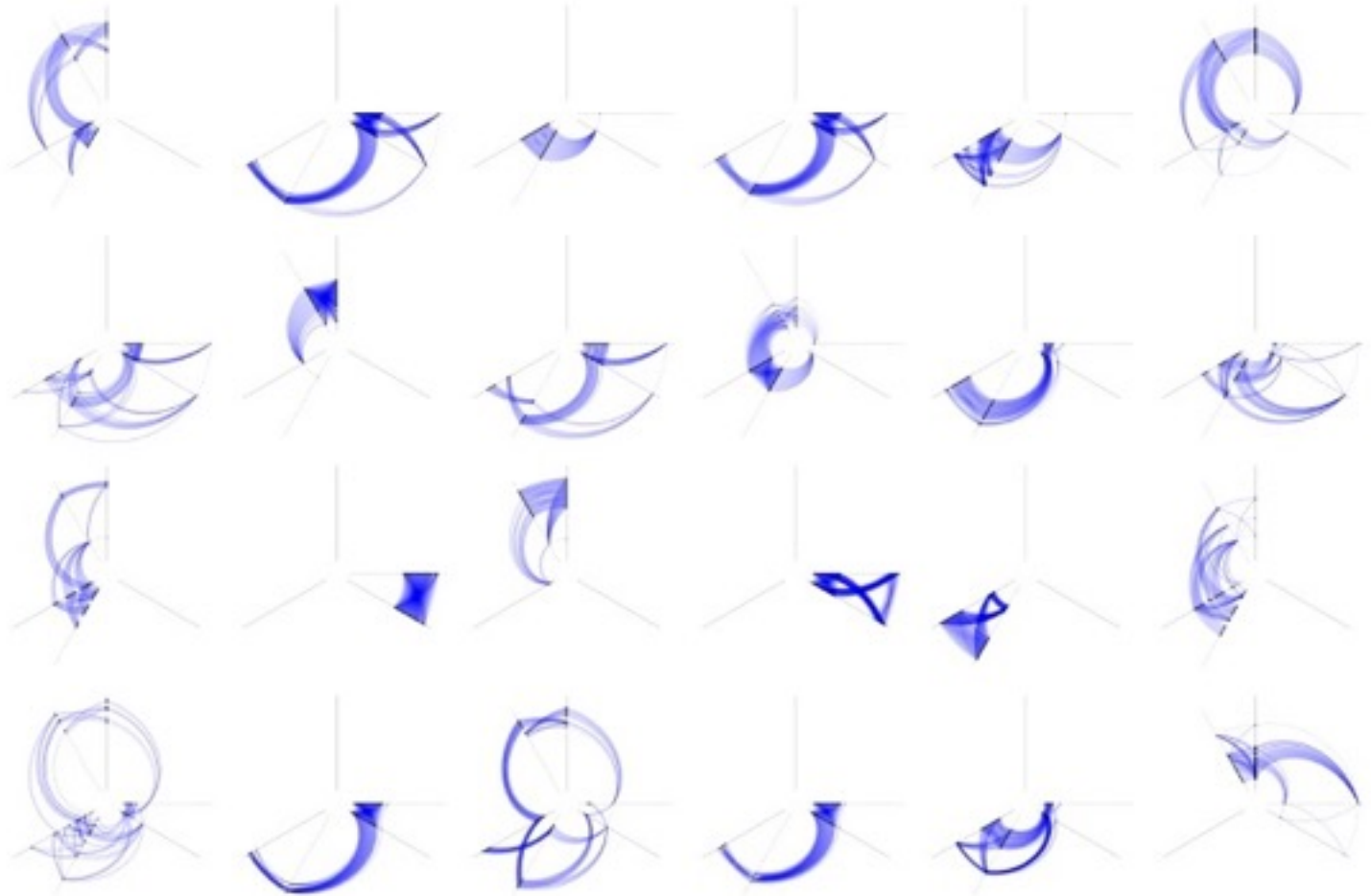


# Hive Plots



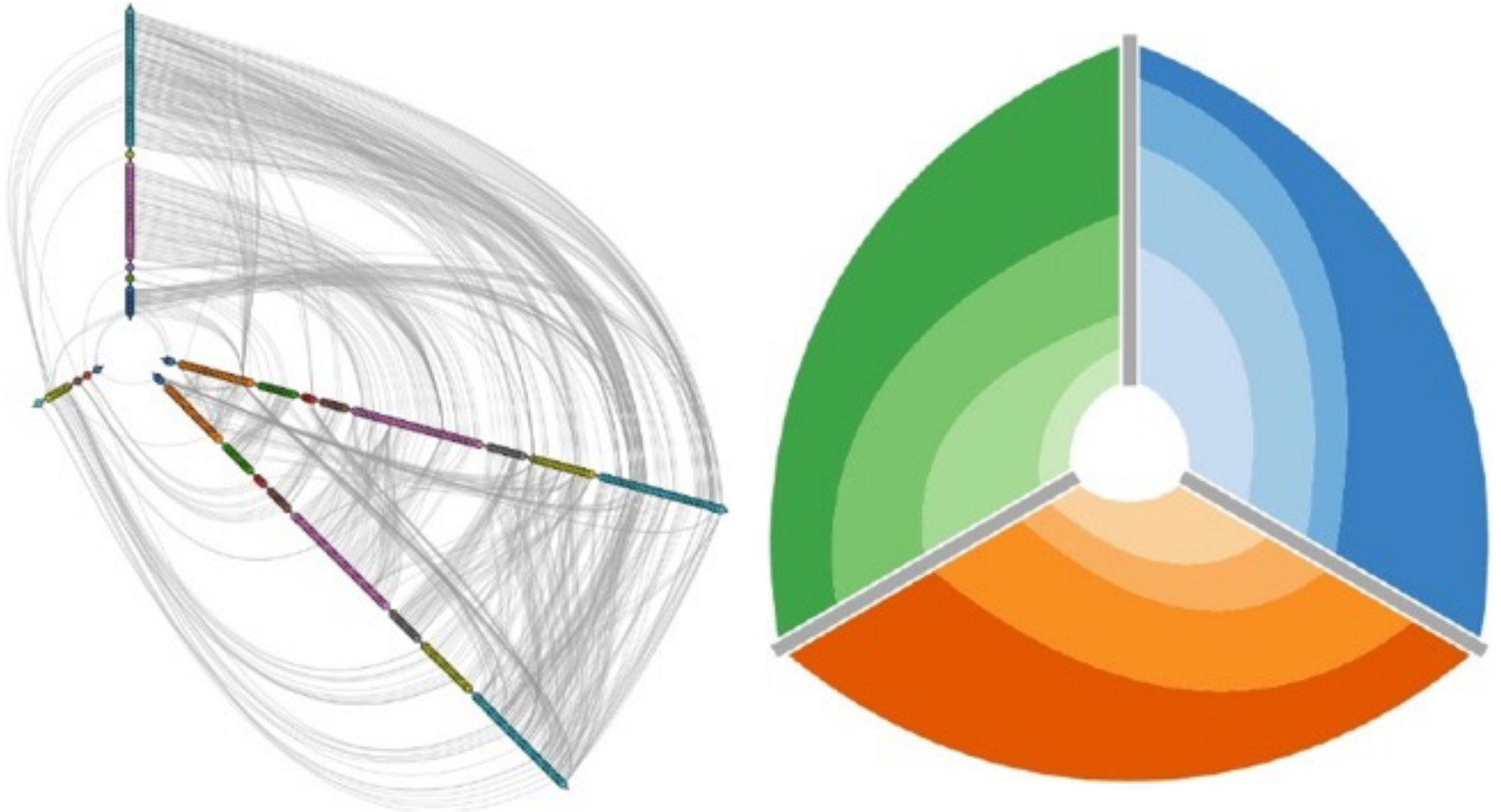
<http://dl.acm.org/citation.cfm?id=2379698>

# Hive Panels



<http://dl.acm.org/citation.cfm?id=2379698>

# Hive Plots in D3



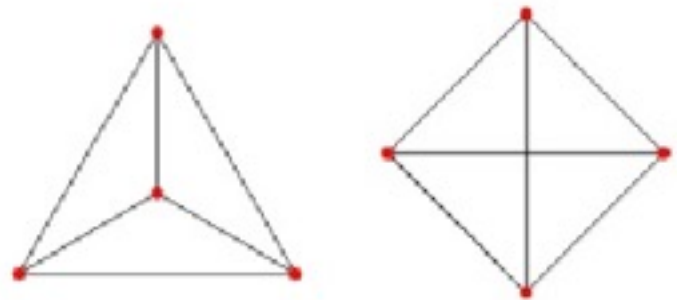
<http://bost.ocks.org/mike/hive/>



# EDGE LAYOUT

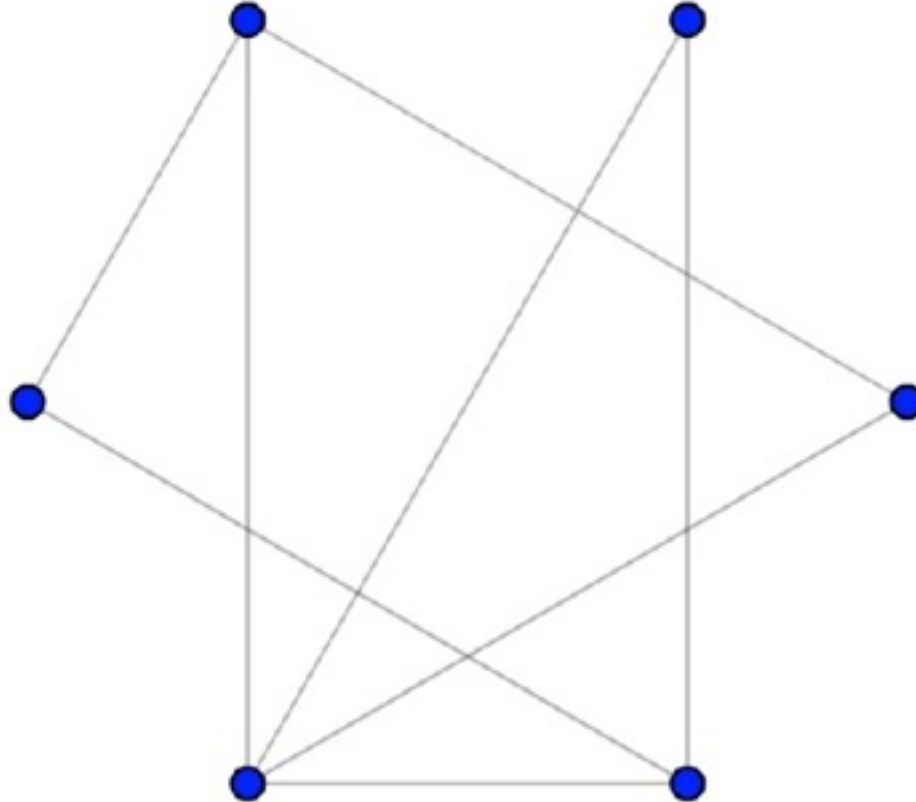
# Edge Crossings

- Planar Graph
  - "A graph is planar if it can be drawn in a plane without graph edges crossing."
- If the graph is not planar, it is impossible to draw without edge crossings.
- Trees are planar graphs.



# Planarity Game

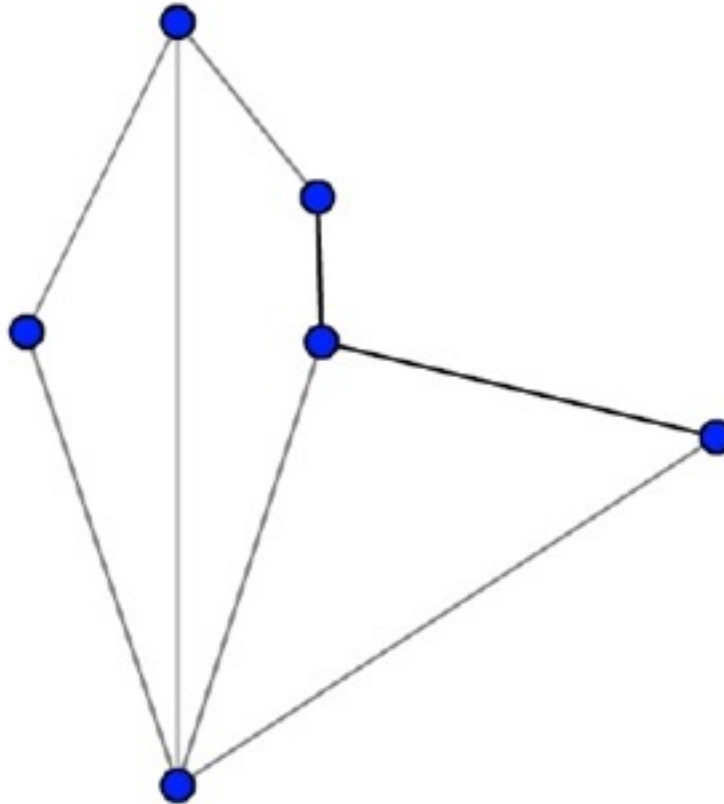
Score: 0  
Level: 1



<http://www.planarity.net/>

# Planarity Game

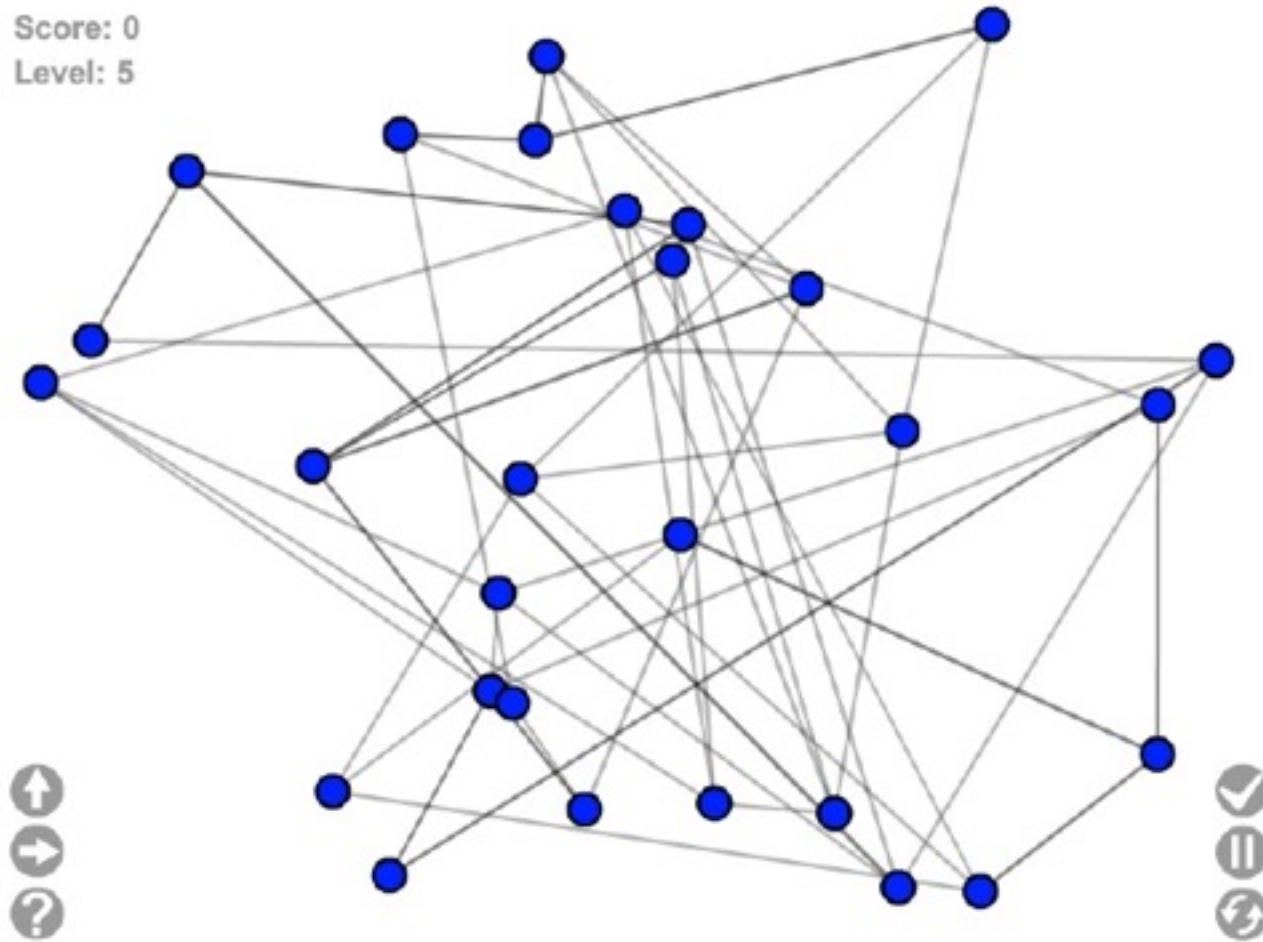
Score: 0  
Level: 1



<http://www.planarity.net/>

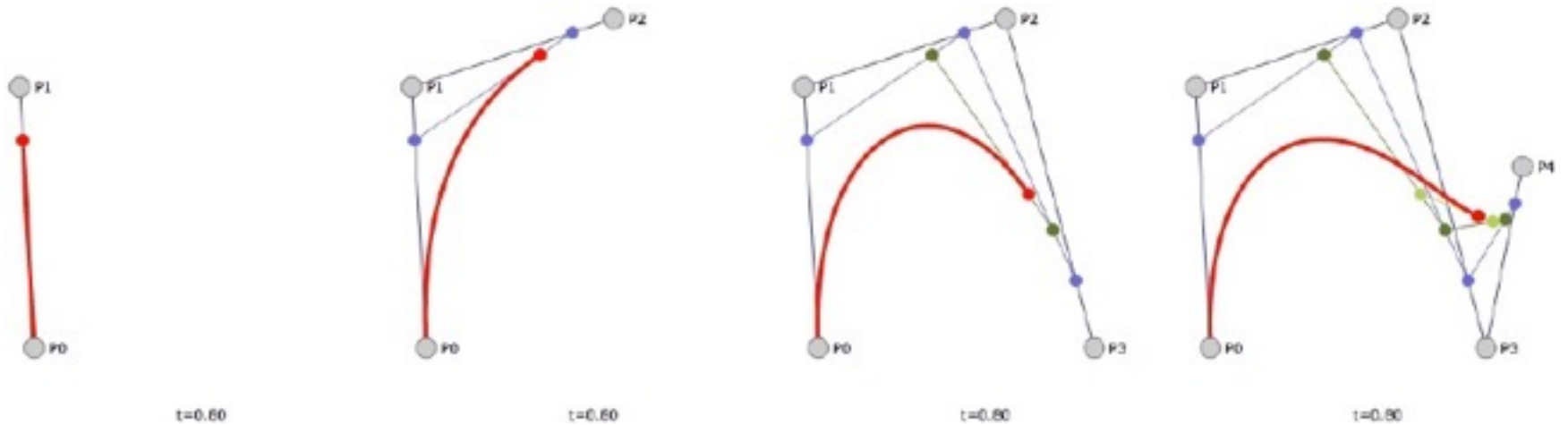
# Planarity Game

Score: 0  
Level: 5



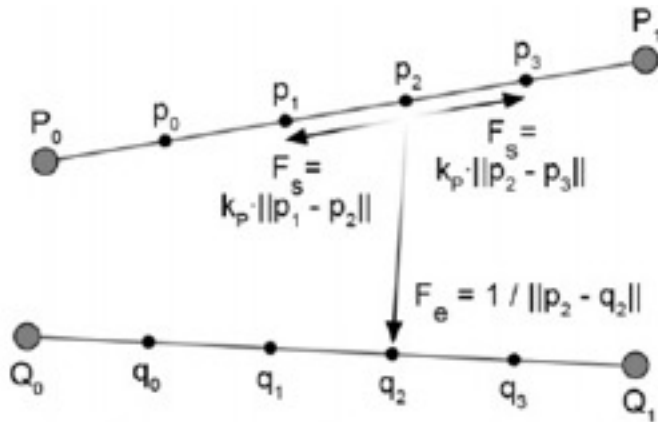
<http://www.planarity.net/>

# Curved Edges

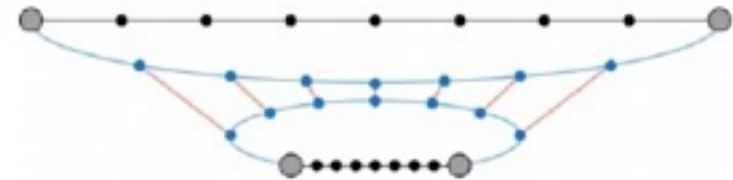


<http://www.jasondavies.com/animated-bezier/>

# Edge Bundling



**Figure 1:** Two interacting edges  $P$  and  $Q$ . The spring forces  $F_s$  and the electrostatic force  $F_e$  that are exerted on subdivision point  $p_2$  by  $p_1$ ,  $p_3$ , and  $q_2$  are shown.

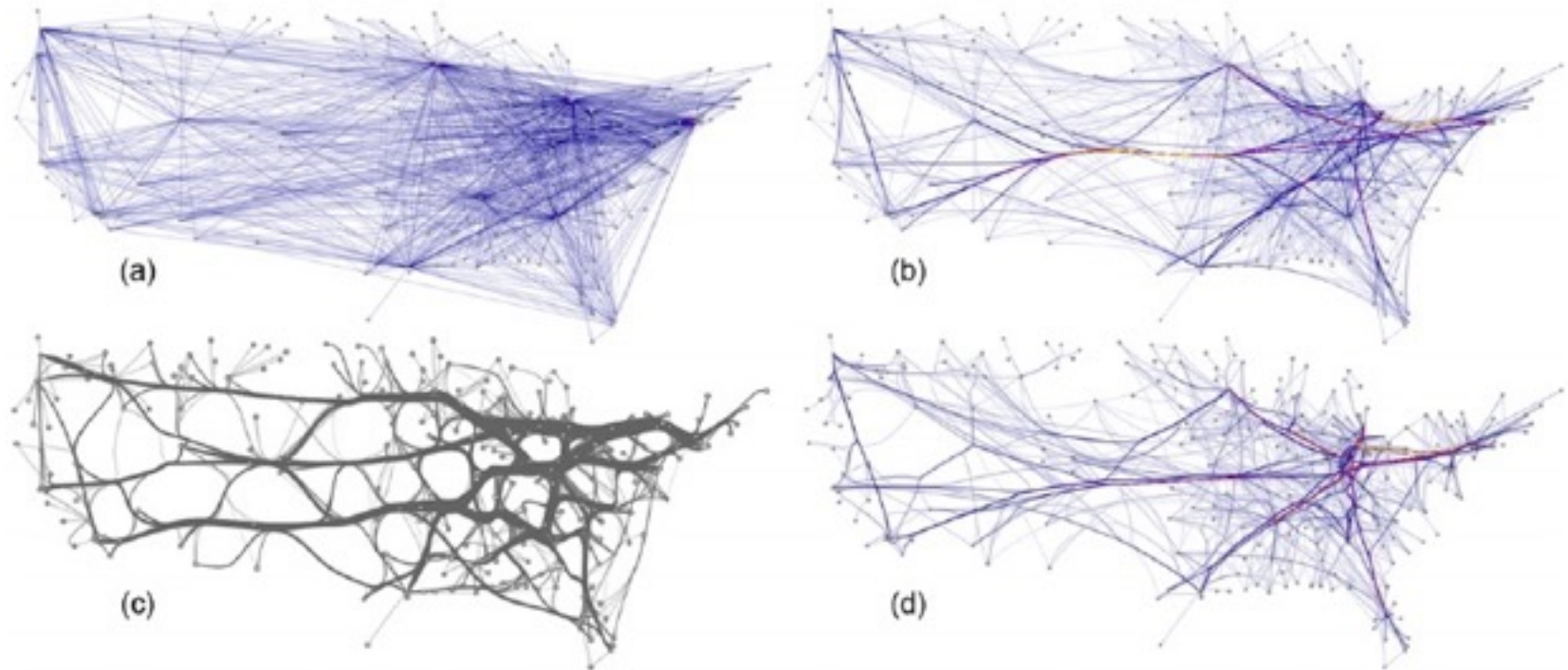


**Figure 4:** Bundling edges that differ considerably in length can result in noticeable stretching and curving of short edges. Original edges, curved edges and attracting forces are shown in black, blue, and red, respectively.



# Edge Bundling

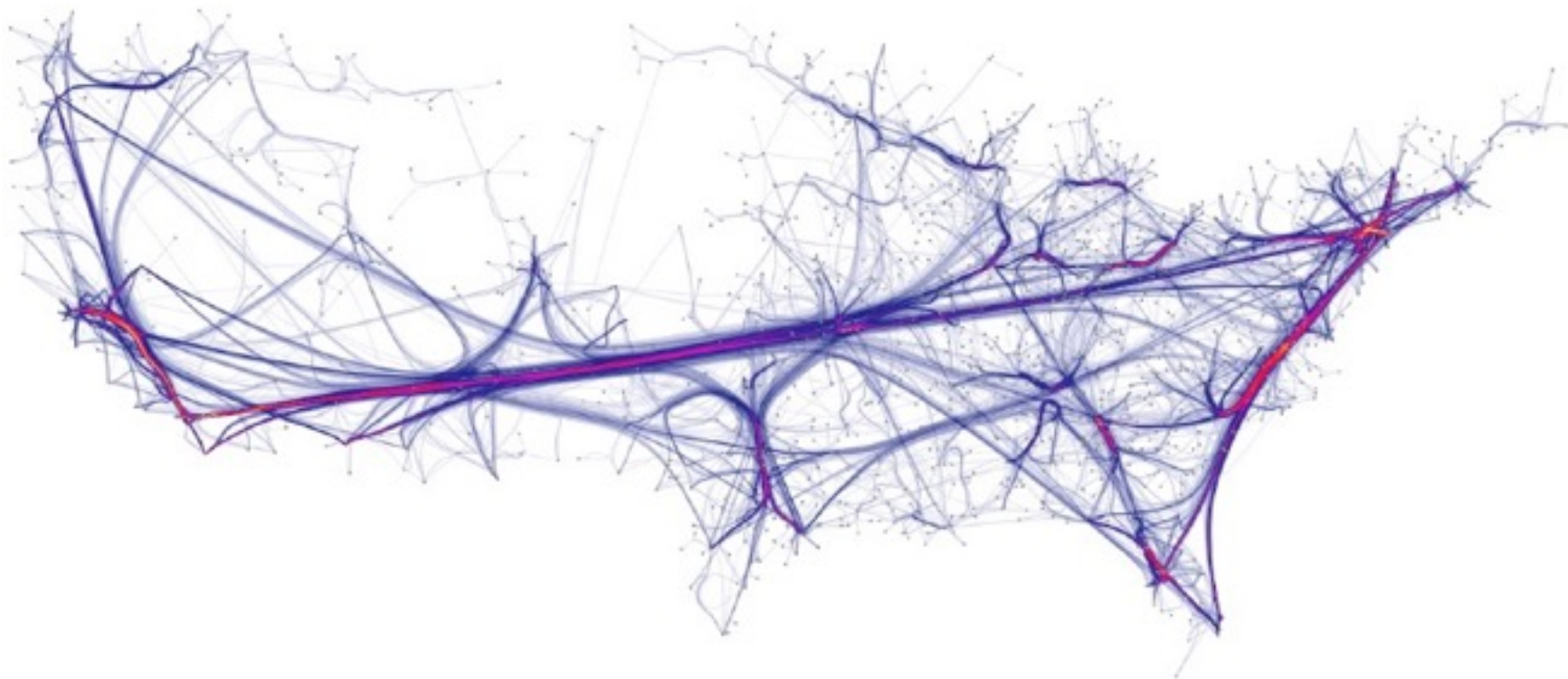
*Danny Holten & Jarke J. van Wijk / Force-Directed Edge Bundling for Graph Visualization*



**Figure 7:** US airlines graph (235 nodes, 2101 edges) (a) not bundled and bundled using (b) FDEB with inverse-linear model, (c) GBEB, and (d) FDEB with inverse-quadratic model.

[https://www.win.tue.nl/vis1/home/dholten/papers/forcebundles\\_eurovis.pdf](https://www.win.tue.nl/vis1/home/dholten/papers/forcebundles_eurovis.pdf)

# Edge Bundling

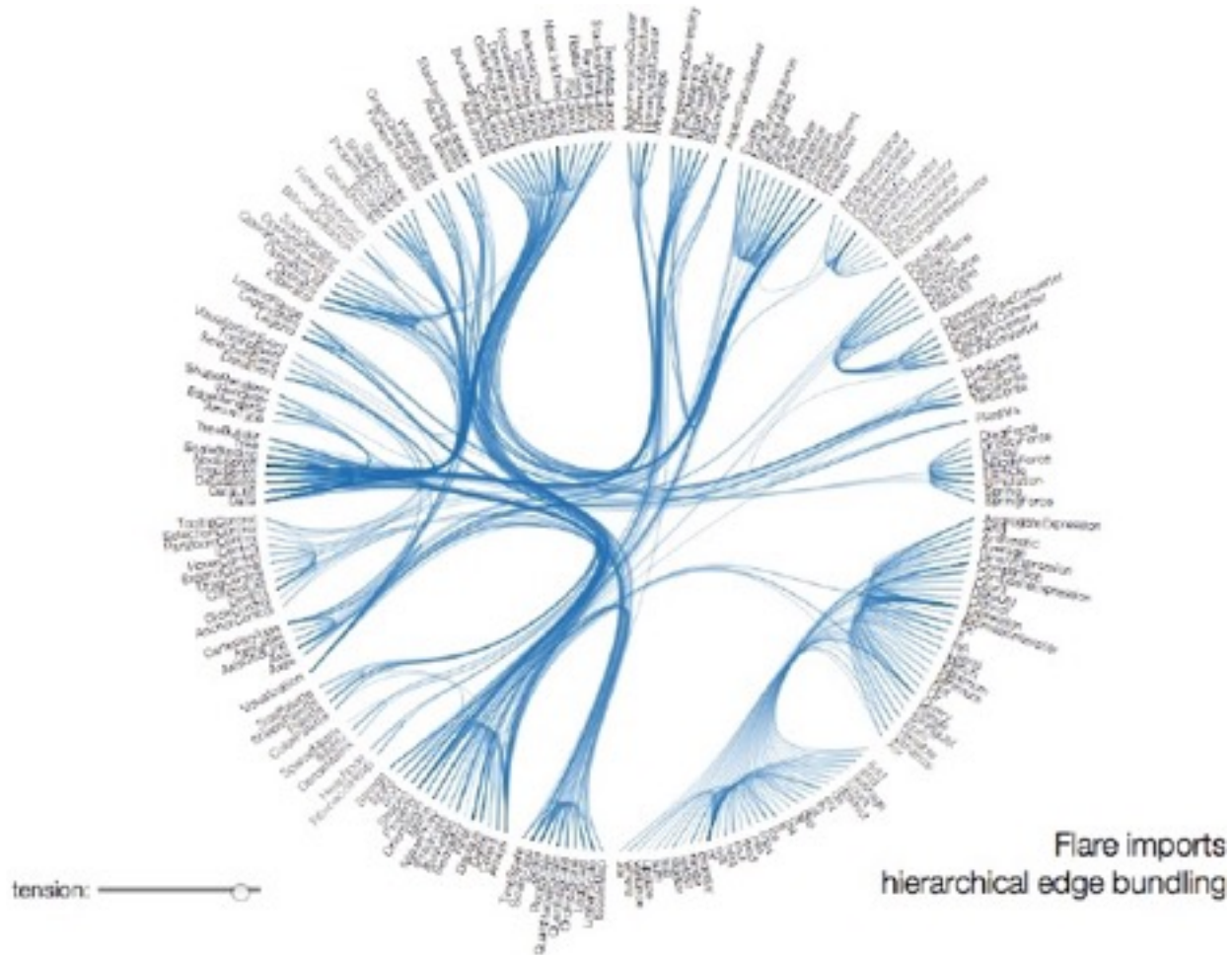


# Edge Bundling



<http://mbostock.github.io/d3/talk/20111116/bundle.html>

# Edge Bundling



<http://mbostock.github.io/d3/talk/20111116/bundle.html>

**QUESTIONS?**

*Thanks to  
Sophie J. Engle  
San Francisco University*

*for ideas, suggestions, slides, links, and much other stuff*